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A new physical barrier system for seawater intrusion control

Antoifi Abdoulhalik, School of Natural and Built Environment, Queen’s University Belfast,
David Keir Building, Stranmillis Road, Belfast, BT95AG, UK

Ashraf Ahmed, School of Natural and Built Environment, Queen’s University Belfast, David
Keir Building, Stranmillis Road, Belfast, BT95AG, UK

G.A. Hamill, School of Natural and Built Environment, Queen’s University Belfast, David
Keir Building, Stranmillis Road, Belfast, BT95AG, UK

Corresponding author: Ashraf Ahmed (a.ahmed@qub.ac.uk)

23 **ABSTRACT**

24 The construction of subsurface physical barriers is one of various methods used to control
25 seawater intrusion (SWI) in coastal aquifers. This study proposes the mixed physical barrier
26 (MPB) as a new barrier system for seawater intrusion control, which combines an impermeable
27 cutoff wall and a semi-permeable subsurface dam. The effect of the traditionally-used physical
28 barriers on transient saltwater wedge dynamics was first explored for various hydraulic
29 gradients, and the workability of the MPB was thereafter thoroughly analysed. A newly
30 developed automated image analysis based on light-concentration conversion was used in the
31 experiments, which were completed in a porous media tank. The numerical code SEAWAT
32 was used to assess the consistency of the experimental data and examine the sensitivity of the
33 performance of the barriers to various key parameters. The results show that the MPB induced
34 a visible lifting of the dense saline flux upward towards the outlet by the light freshwater. This
35 saltwater lifting mechanism, observed for the first time, induced significant reduction to the
36 saline water intrusion length. The use of the MPB yielded up to 62% and 42% more reduction
37 of the saltwater intrusion length than the semi-permeable dam and the cutoff wall, respectively.
38 The performance achieved by the MPB with a wall depth of 40% of the aquifer thickness was
39 greater than that of a single cutoff wall with a penetration depth of 90% of the aquifer thickness
40 (about 13% extra reduction). This means that the MPB could produce better seawater intrusion
41 reduction than the traditionally used barriers at even lower cost.

42 **Keywords:** Physical barriers; Saltwater intrusion mitigation; Salinization; Management of
43 coastal aquifers.

44 **1. Introduction**

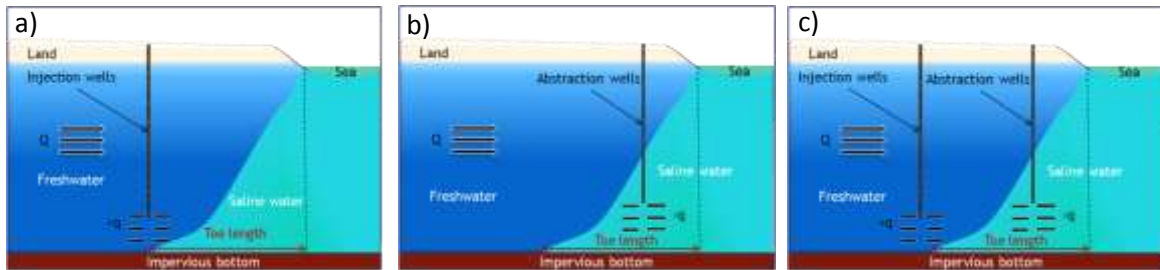
45 Seawater intrusion (SWI) has occurred in many coastal regions around the world (Bear et al.,
46 1999). With the rise of sea levels and uncontrolled freshwater extraction from coastal regions,

47 saltwater may advance further inland and contaminate the available groundwater supply (Oude
48 Essink, 2001; Fergusson and Glesson, 2012). For water resources managers, today's challenge
49 is to establish effective measures to control SWI and enable an optimal exploitation of
50 groundwater resources. Previous studies in the literature have proposed several
51 countermeasures to prevent or mitigate SWI; among these has been the installation of
52 subsurface barriers, which can be of hydraulic or physical nature (Abarca, 2006; Oude Essink,
53 2001).

54 Hydraulic barriers can be divided into three types: positive, negative, and mixed barriers. In
55 positive barriers (Fig 1a), freshwater is injected into the aquifer to raise the water table, which
56 impedes the inland motion of the saltwater. The water is often injected through recharge wells
57 installed in series along the coastline to create a freshwater ridge. Although the effectiveness
58 of positive barriers has been argued in some studies (Abarca et al., 2006), recent studies have
59 shown that an effective saltwater repulsion could only be achieved if the water is injected at
60 the toe of the saltwater wedge (Botero-Acosta and Donado, 2015; Luyun et al., 2011). This
61 highlights a significant limitation of positive barriers, considering that the saltwater wedge is
62 never completely stationary in real-world scenarios but moves back and forth with seasonal
63 oscillations (Luyun et al., 2009).

64 Negative barriers (Fig 1b) involve the interception of the intruding saltwater by pumping near
65 the coast. Although the landward motion of the saltwater could be slowed, it was found that
66 these barriers extract more freshwater than saltwater which eventually leads to a decrease of
67 the available groundwater resources (Pool and Carrera, 2010). In addition, this method is only
68 effective if the saltwater abstraction rate exceeds the freshwater pumping rate, thus involving
69 a considerable and continuous amount of energy (Sriapai et al., 2012). The disposal of the
70 abstracted saline groundwater could also be a source of concern (Kumar, 2006). A mixed
71 hydraulic barrier (Fig 1c) combines a positive barrier and a negative barrier. Freshwater is

72 injected inland to repulse the saltwater wedge, while saltwater is extracted near the shore to
 73 slow its encroachment (Basdurak et al., 2007; Pool and Carrera, 2010). In addition to the
 74 limitations mentioned above, this measure would require significant operational and
 75 maintenance costs due to the high risk of clogging and reduction of filtering area of the screen
 76 generally involved in the use of wells (Bear, 1979).



77

78 **Figure 1 Simplified diagrams showing the various hydraulic barriers; a) Positive barrier, b) Negative**
 79 **barrier and c) Mixed hydraulic barrier.**

80 The use of physical barriers as a SWI control method has been the focus of several studies
 81 (Archwichai et al., 2005; Sugio et al., 1987; Mundzir, 2001; Anwar, 1983; Kaleris and Ziogas,
 82 2013; Luyun et al., 2009, 2011; Strack, 2016) . Physical barriers are subsurface impermeable
 83 or semi-permeable structures constructed parallel to the coast. Two types of physical barriers
 84 are described in the literature: the subsurface dams and the cutoff walls. The subsurface dam
 85 is embedded at the impervious bottom layer of the aquifer and obstructs its lower part only,
 86 leaving an opening above it to allow the natural discharge of freshwater to the ocean. This
 87 method has met great success in Japan, where seven out of fifteen subsurface dams were
 88 specifically designed to prevent landward incursion of saltwater and preserve fresh
 89 groundwater storage (Luyun et al., 2009; Japan Green Resources Agency, 2004). In Luyun et
 90 al. (2009), it was demonstrated that subsurface dams with smaller height could achieve faster
 91 removal of inland residual saltwater as well as more reduction of the expected increase of the
 92 saltwater wedge height along the coastline boundary than higher dams. The dam height only
 93 needs to exceed the height of the saltwater wedge at the desired construction location.

94 The second type of physical barrier is cutoff walls, which extend from the top of the aquifer to
95 a predefined depth. The effectiveness of cutoff walls increases when they are closer to the
96 coastline and have greater penetration depth (Luyun et al., 2011). The closer the cutoff wall is
97 installed to the coast, the larger the fresh groundwater volume would be. Kaleris and Ziogas
98 (2013) found that the performance of cutoff walls located at distances from the coastline of the
99 order of half of the aquifer height depends not only on the penetration depth, but also on the
100 ratio of the groundwater inflow velocity over the density driven saltwater velocity.

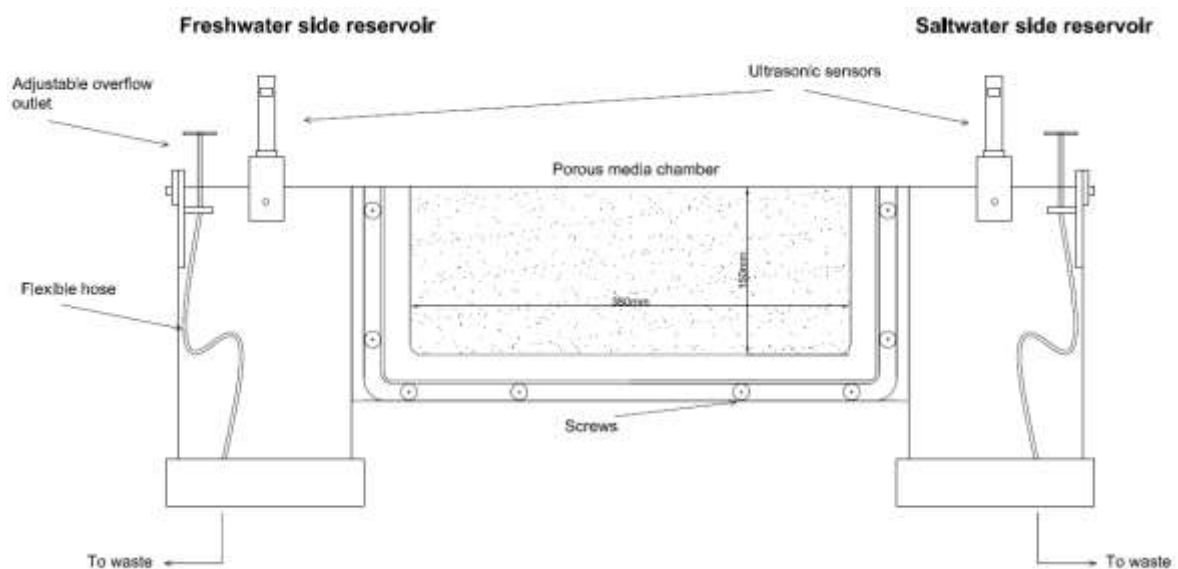
101 Controlling the velocity ratio would not only better help to repulse saltwater intrusion, but it
102 would also allow an increased freshwater storage for a more optimal exploitation of the
103 available freshwater resource. This concept of combined actions on saltwater intrusion has
104 never been applied to physical barriers before. To address this point, this paper proposes the
105 mixed physical barrier (MPB), which combines an impermeable cutoff wall located close to
106 the shore, and a short semi-permeable subsurface dam placed at the seaward side of the cutoff
107 wall. The aim of the new MPB system is to increase the velocity ratio, and hence further
108 enhance the capability of repulsing the seawater wedge.

109 The main objectives of this study are therefore 1) to investigate the effect of semi-permeable
110 dams and cutoff walls on transient saltwater intrusion dynamics and 2) to assess the viability
111 of MPB as a new SWI control method. To the best of our knowledge, these objectives have
112 never been investigated in previous studies. Experimental automated image analysis technique
113 (Robinson et al., 2015) was used here to quantify the main SWI parameters. The methodology
114 allowed quantitative analysis of the effect of the barriers on the toe length under transient
115 conditions with high spatial and temporal resolution. The numerical model SEAWAT was used
116 to assess the consistency of the experimental results with the numerical predictions. A
117 sensitivity analysis was then performed to evaluate the dependency of the effectiveness of each
118 barrier on some key design variables.

119 **2. Experimental approach**

120 **2.1 Description of the experimental set-up**

121 The experiments were completed in a flow tank of dimension 0.38 x 0.15 x 0.01 m (Fig 2). The
122 narrowness of the tank enabled the simulation of a two dimensional system representing a cross
123 section of an unconfined coastal aquifer. The tank was composed of a porous media chamber
124 and two side reservoirs. The porous media chamber was filled with glass beads of mean
125 diameter 1.1 mm. The beads were packed under saturated conditions to avoid risk of air
126 entrapment. The beads were packed in three layers of similar thickness and each layer was
127 carefully compacted. The resulting porous domain was assumed to satisfy homogeneous
128 isotropic conditions. Two fine mesh acrylic screens were used to separate the porous media
129 chamber from the side reservoirs.

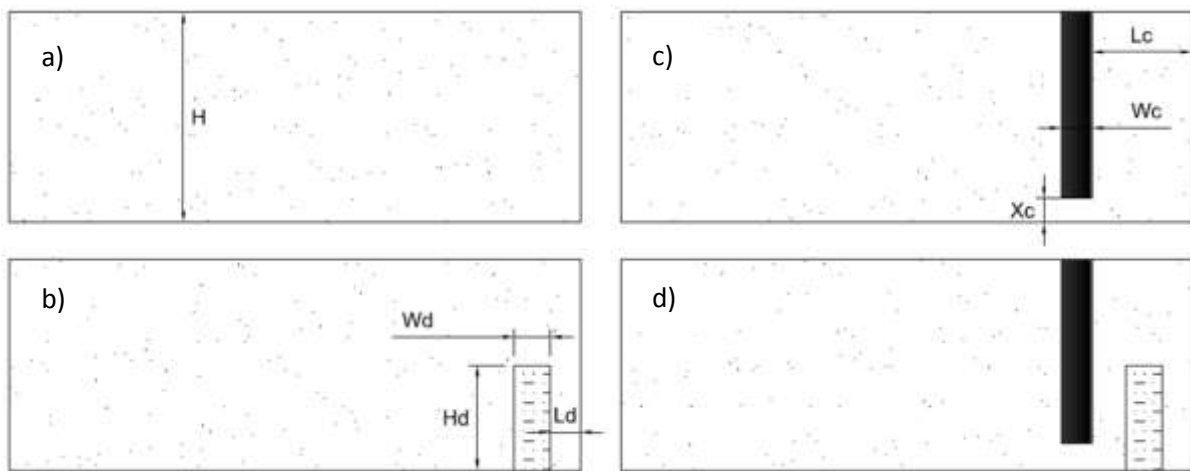


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131 **Figure 2 Schematic diagram of the porous media tank**

132 The left side reservoir was used to feed freshwater flow to the system, and the right side
133 reservoir was filled with saltwater. The hydraulic conductivity of the system was measured in
134 situ using similar methods described in Oostrom et al. (1992) without considering the capillary
135 fringe. The average hydraulic conductivity value of the porous media was estimated at 0.014

136 m/s. A 200l saltwater solution was prepared prior the experiments by dissolving commercial
 137 salt into freshwater at a concentration of 36.16 g/l to achieve a density of 1025 kg/m³. The
 138 density was measured using a hydrometer (H-B Durac plain-form polycarbonate) and also
 139 manually using mass/volume ratio. To distinguish the saltwater from the freshwater, red dye
 140 (food colour) was added to the saltwater solution at a concentration of 0.15 g/l. In all the
 141 experiments, the saltwater solution was sourced from the 200l batch to ensure uniformity of
 142 density and colour between the experiments.



143

144 **Figure 3 Investigated cases: a) baseline case; b) subsurface dam case; c) cutoff wall case; d) MPB**
 145 **case. The freshwater flows from left to right.**

146 Fig 3 presents the various experimental cases investigated herein. The height of the synthetic
 147 aquifer (saturated thickness) was $H=136$ mm in all the experiments. The barriers were placed
 148 ahead of the packing of the beads. To form the semi-permeable dam, two dividers were inserted
 149 into the porous media chamber at the desired location, and fine beads of mean diameter 0.3
 150 mm were siphoned into the spacing between them until the desired height. On completion of
 151 the packing, the dividers were carefully removed. The average hydraulic conductivity of the
 152 dam was also obtained by in situ measurement on the experimental flow tank (using finer mesh
 153 screens on both sides) and was found $K_d = 0.0017$ m/s. In field applications, typical grouting
 154 materials include soil–cement–bentonite that could exhibit hydraulic conductivities as low as
 155 10^{-9} m/s are used (Kaleris and Ziogas, 2013).

156 The cutoff wall was made of impermeable material (plasticine). Cutoff walls are generally
 157 located at distances from the coastline less than or equal to twice the aquifer height (Allow,
 158 2012; Japan Green Resources Agency, 2004) and should be located within the area of the
 159 saltwater wedge to be effective (Luyun et al., 2011). To meet these conditions, the cutoff wall
 160 was placed at a distance in the order of half of the aquifer height in our investigations. It was
 161 ensured that the cutoff wall was located within the saltwater wedge area by first analysing the
 162 saltwater wedge extent in a synthetic aquifer free of barrier (base case), as described below.
 163 The cutoff wall depth was adjusted such that an opening smaller than 40% of the aquifer height
 164 from the bottom of the tank was left to ensure effective reduction of the saltwater intrusion
 165 length (Kaleris and Ziogas, 2013). Note that the maximum wall depth of construction
 166 applicable in real field aquifers is up to 100 m (Kaleris and Ziogas, 2013). Table 1 presents a
 167 summary of the dimensions and location of the dam and cutoff wall barriers. For the MPB
 168 experiment, the cutoff wall and the semi-permeable dam were both placed in same positions as
 169 in the other experiments.

170 **Table 1 Values of the design variables**

Variable	Symbol	Values
Subsurface dam		
Distance from seawater boundary	L_d	20 mm
Height	H_d	70 mm
Width	W_d	24 mm
Hydraulic conductivity	K_d	0.0017 m/s
Cutoff wall		
Distance from seawater boundary	L_c	66 mm
Opening	X_c	16 mm
Width	W_c	20 mm

171

172 2.2 Experimental procedure

173 All the experiments were recorded using a high speed camera (IDT Motion Pro X – series).
 174 Prior to each experiment, a calibration method was implemented to correlate the light intensity

175 of the recorded images to the salt concentration. The calibration method included the flushing
176 of the domain with saltwater solutions at various concentrations, and the light intensity of every
177 concentration for every single pixel was recorded, as detailed in Robinson et al. (2015). A
178 MATLAB code was used to obtain the intensity-concentration parameters and then analyse all
179 the experimental images. The light intensity-concentration conversion allowed the
180 determination of key SWI intrusion parameters under transient conditions.

181 At the start of each experiment, freshwater was injected at constant rate from a large tank
182 located above the left side reservoir and the freshwater level was set high enough to allow the
183 entire porous media to remain fully saturated with freshwater. Freshwater flux transited through
184 the system from the inland boundary and exited at the coastal boundary without overflowing.
185 On the saltwater reservoir, the overflow outlet was adjusted to maintain a constant head of
186 129.7 mm. Excess amount of saltwater was supplied from another large tank into the right
187 reservoir to ensure the flushing out of any freshwater floating at the surface, until the density
188 measurement became stable. Ultrasonic sensors (Microsonic - mic+25/DIU/TC) were used to
189 monitor all the head values with +/- 0.2mm accuracy.

190 The simulation of groundwater fluctuations was achieved by varying the freshwater level. For
191 each experiment, two different heads were successively forced at the freshwater boundary,
192 namely 135.7mm and 133.7mm, yielding a head differences of $dh=6\text{mm}$ (135.7-129.7) and
193 $dh=4\text{ mm}$ (133.7-129.7), each for 50 minutes to allow the system to reach a quasi-steady state
194 condition. The head differences $dh=6\text{mm}$ and $dh=4\text{mm}$ corresponded to hydraulic gradients of
195 0.0158 and 0.0105, respectively, which is consistent with previous laboratory studies using
196 similar experimental set up (Robinson et al, 2015, 2016; Goswami and Clement, 2007; Chang
197 and Clement, 2012) and within the range of hydraulic gradient measured at some field sites
198 (e.g. Ferguson and Gleesson, 2012; Attanayake and Michael, 2007). The initial condition was
199 set by forcing a head of 135.7 mm at the freshwater boundary ($dh=6\text{mm}$). The denser saltwater

200 was allowed to intrude into a fully fresh aquifer, until the system reached the first quasi-steady
201 state condition. The freshwater level was then decreased to 133.7 mm ($dh=4\text{mm}$), allowing the
202 saltwater wedge to migrate further inland. The freshwater head was then returned to the initial
203 value of $dh=6$ mm, which forced the saltwater wedge to recede toward the seawater boundary.
204 The use of the same head difference $dh=6\text{mm}$ as that used to set the initial condition was also
205 to check if any hysteresis occurs over the course of the experiment.

206 To assess the effectiveness of the different barriers, a baseline case with no barrier installed
207 was first studied to be used as a benchmark for the barrier cases investigated. The effectiveness
208 of the barriers was characterised by the percentage of reduction $R = (TL_0 - TL_b)/TL_0$, where
209 TL_0 and TL_b are the intrusion length before and after the installation of the barrier, respectively.

210 **3. Description of the numerical model and procedure**

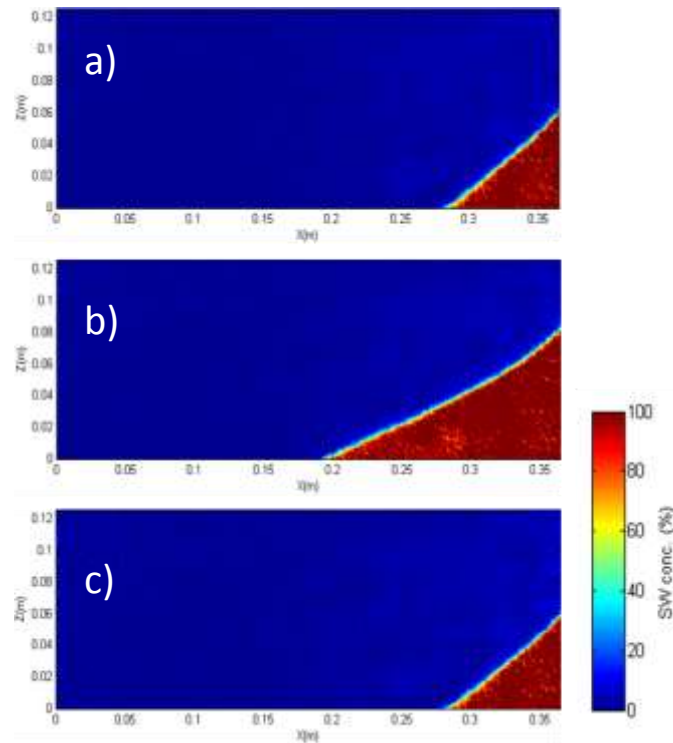
211 The MODFLOW family variable density flow code SEAWAT (Guo and Langevin, 2002) has
212 been widely used to solve various variable density benchmark problems (Goswami and
213 Clement, 2007; Johannsen et al., 2002; Chang and Clement, 2012, 2013), including saltwater
214 experiments involving freshwater head boundary variations. The domain was evenly
215 discretised with a grid size of 0.2 cm. The longitudinal dispersivity was estimated after trial
216 and error process and was eventually estimated at 0.1 cm and the transverse dispersivity was
217 0.05 cm, which is within the range of dispersivity values reported in Abarca and Clement
218 (2009). The spatial discretization satisfies the criterion of numerical stability, i.e. grid Peclet
219 number is less or equal to four (Voss and Souza, 1987). The molecular diffusion was neglected
220 in all the numerical experiments. The specific storage was set at 10^{-6} cm^{-1} . Densities of the
221 freshwater and saltwater were 1000 kg/m^3 and 1025 kg/m^3 , respectively. A concentration of
222 36.16 g/l was used for the seawater boundary, corresponding to the amount of salt required to
223 prepare the saltwater solution.

224 To simulate the transient saltwater intrusion, three stress periods were applied. Each stress
225 period lasted 50 minutes, which corresponds to the duration required for the system to reach
226 approximate steady state condition observed in the physical model. The time step was set to 30
227 sec. A variable-head boundary condition was set on the freshwater side ($C=0$ g/l), where it
228 varied from 135.7 to 133.7 mm, and a constant-head of 129.7 mm was set on the saltwater side
229 ($C=36.16$ g/l). The initial condition of the numerical model corresponded to a fully freshwater
230 aquifer. The boundary conditions were forced on both sides and the system was allowed to
231 reach the first quasi-steady state condition. The head and concentration resulting in each cell
232 at the end of each stress period were used as initial condition for the following transient period.
233 The subsurface dam was simulated into the numerical model by assigning the hydraulic
234 conductivity $K_d = 0.0017$ m/s to the cells of interest, which correspond to the value measured
235 in the setup, while the cutoff wall was assumed to be impermeable.

236 **4. Results and discussion**

237 **4.1 Baseline case**

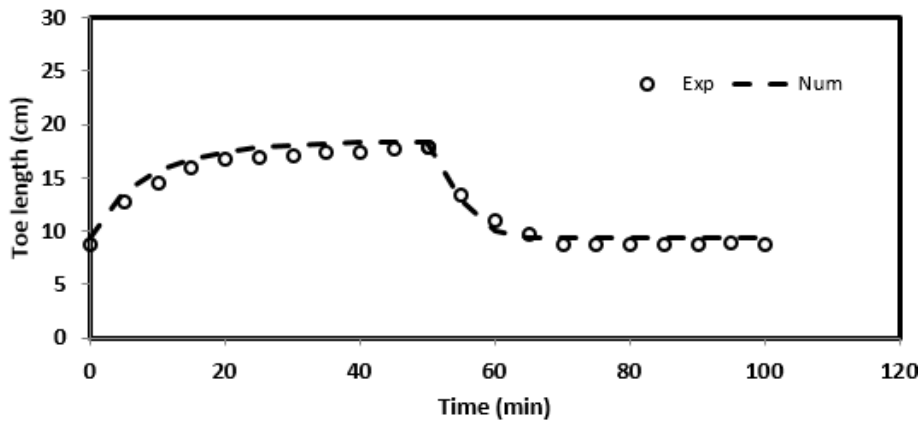
238 In the following discussion, the toe length (TL) refers to the distance that the 50% saltwater
239 concentration isoline has penetrated the aquifer from the coastal boundary. Moreover, a steady
240 state here does not refer to complete steady state as defined in fluids flow; it refers to quasi-
241 steady state where the wedge becomes stable with no further intrusion or retreat albeit very
242 slight forward/backward movement may happen due to tiny boundary head fluctuations and
243 this will be shown in the figures.



244

245 **Figure 4 Steady-state experimental saltwater wedge in the base case; a) $t = 0$ min (initial**
 246 **condition); b) at $t = 50$ min ($dh=4$ mm); c) at $t = 100$ min ($dh=6$ mm)**

247



248

249 **Figure 5 Transient experimental and numerical toe length results of the base case**

250

251 Fig 4 presents the concentration colour maps of the base case, showing the intrusion of the
 252 saltwater wedges at the various steady state conditions observed in the experiment. The
 253 horizontal extent of the saltwater wedge was 8.8 cm in the physical model, at the end of the
 254 first time period. The end of time period 1 will hereafter be regarded as the zero time because

255 the hydraulic gradient in time periods 1 and 3 was the same and results showed no difference
256 in the length of the wedge between both time periods. Therefore, figures showing the transient
257 *TL* will present only time period 2 (advancing wedge; $dh=4\text{mm}$) and time period 3 (receding
258 wedge; $dh=6\text{mm}$).

259 The transient experimental and numerical *TL* data are presented in Fig 5. The numerical model
260 matched well the experimental data and was able to reproduce the movement of the toe for the
261 two hydraulic gradients considered. After reducing the head difference to $dh= 4\text{mm}$, the
262 saltwater *TL* extended to 17.9 cm and 18.41 cm in the experimental and numerical,
263 respectively. At time $t=50$ min, the head difference was increased to $dh=6\text{mm}$ which forced the
264 wedge to retreat back to its original position. The agreement between the experimental and
265 numerical results was generally good. The shape of the saltwater wedge (transition zone and
266 *TL*) at the end of the receding phase was identical to that of the initial condition, indicating that
267 no hysteresis occurred throughout the experiment.

268 Fig 5 not only shows the reliability of the numerical model for the simulation of the remaining
269 experiments, but it also demonstrates the accuracy of the recorded *TL* data used as baseline for
270 estimating the performance of the barriers. The two TL_0 values used for the calculation of R
271 were therefore 8.8 cm and 17.9 cm. These were assumed to be the two extreme saltwater
272 intrusion scenarios for the coastal aquifer system considered.

273

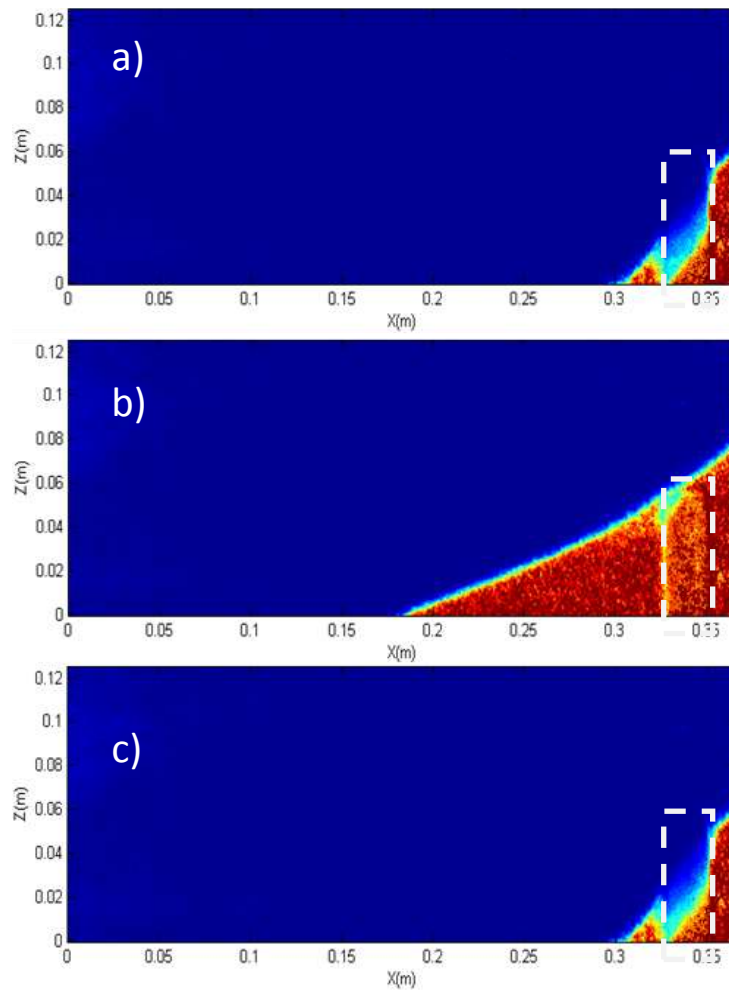
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278 **4.2 Subsurface dam case**



279

280 **Figure 6 Experimental steady-state saltwater wedge in the subsurface dam case; a) t = 0 min**
281 **(initial condition); b) at t = 50 min (dh=4mm); c) at t = 100 min (dh=6mm)**

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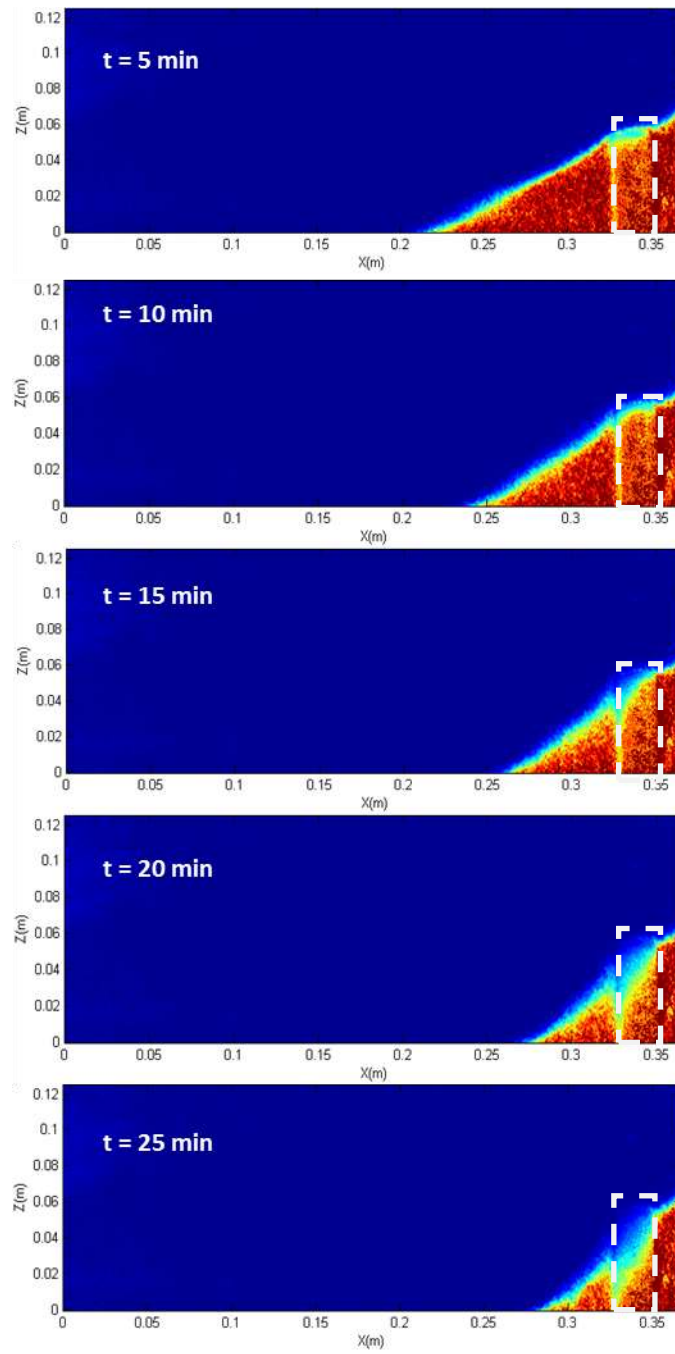
283 Fig 6 presents the experimental results of the steady state saltwater wedge for different
284 hydraulic gradients. Upon setting the initial condition with $dh=6\text{mm}$, the saltwater wedge
285 slowly penetrated into the system until the TL reached 7 cm at steady state (Fig 6a). Following
286 the application of head difference $dh=4\text{mm}$, the intrusion length extended to 18.8 cm at steady
287 state condition, which corresponds to a percentage of reduction R of -5 %. This negative
288 reduction indicates that the TL exceeded that of the baseline case. Laboratory observations
289 revealed that this extension was rather slow and occurred after the dam was almost fully
290 saturated by the saline water (Fig 6b). As the saltwater supply into the system was partially

291 disrupted by the semi-permeable dam, density difference effects caused the saline water in the
292 landward side of the dam to gently slide under the freshwater flow, thereby causing a slight
293 extension of the toe length. Similar observations were reported in Luyun et al. (2009).

294 After the head difference was reversed to $dh=6\text{mm}$ at $t=50$ min, the TL retreated and measured
295 7 cm at steady state, which corresponds to a percentage reduction R of 21%. This result
296 indicates that the semi-permeable dam could achieve noticeable reduction of the intrusion
297 length only when the hydraulic gradient is high enough to produce sufficient advective forces
298 to help maintain the saltwater wedge on the seaward side of the dam.

299 The final shape of the wedge was nearly identical to that of the initial condition, suggesting
300 that no hysteresis occurred over the course of the experiment (Fig 6a, 6c). The retreat of the
301 wedge was associated again with a noticeable widening of the transition zone as the interface
302 crosses the semi-permeable dam (Fig 6c). This can be clearly observed in Fig 7 that shows the
303 transient receding wedge after $dh=6\text{mm}$ was applied to the system. The penetration of the
304 wedge through the dam induced a substantial widening of the transition zone. The low
305 permeability material of the dam primarily slows the movement of the wedge and decreases
306 the freshwater flow velocity. The widening of the transition zone occurring in such conditions
307 is expected to be the result of enhanced separation of streamlines of the freshwater–saltwater
308 mixture induced by flow refraction within the low permeability material of the dam (Lu et al,
309 2013).

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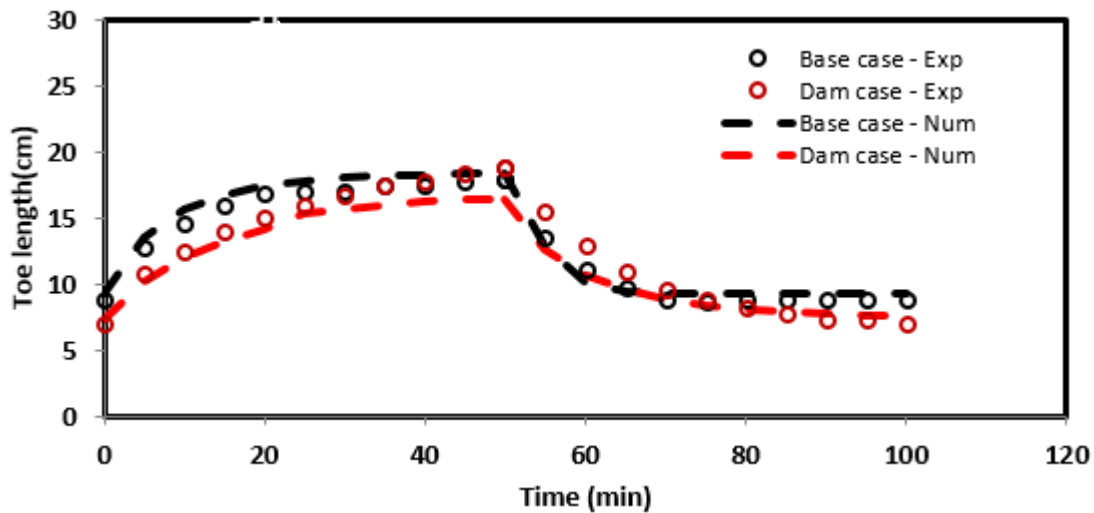


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312

Figure 7 Transient experimental receding saltwater wedge in the subsurface dam case

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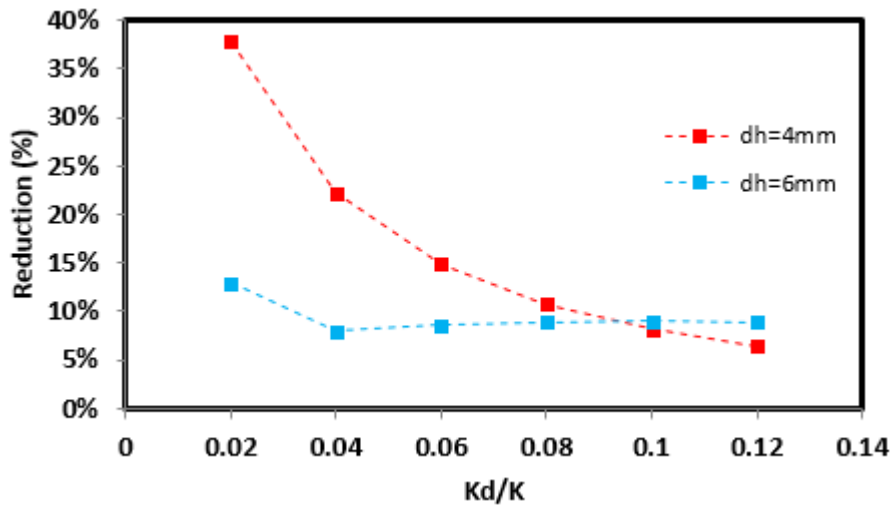
315 **Figure 8 Transient experimental and numerical toe length results of the subsurface dam case**

316

317 The transient dynamics of the saltwater wedge compared to the numerical prediction is
 318 presented in Fig 8 for both the dam and baseline cases. The numerical model reasonably
 319 replicated the transient changes of the toe position in the presence of the subsurface dam, for
 320 both hydraulic gradients. Smaller values of the *TL* were recorded in the dam case until $t=30$
 321 min in the experimental model, which suggests that the presence of the subsurface dam
 322 temporarily slowed down the rate of the intrusion at the start after which the wedge was forced
 323 to flow through the lower permeability material due to the build-up of the saline water pressure
 324 behind the dam.

325 The larger *TL* values observed in the subsurface dam case until $t=75-80$ min in both the
 326 experimental and numerical model suggest that the dam temporarily slowed the natural retreat
 327 of saltwater wedge following the increment of the head difference to $dh=6\text{mm}$ ($t=50-100$ min).
 328 This observation indicates that initially the presence of the low permeability material partially
 329 prevented the increased freshwater flow from effectively repulsing the saline water towards the
 330 boundary, after which the *TL* values became smaller than the base case. In overall, the results

331 suggest that the use of subsurface dam constructed from semi-permeable materials may not be
 332 an effective countermeasure for seawater intrusion control purposes.



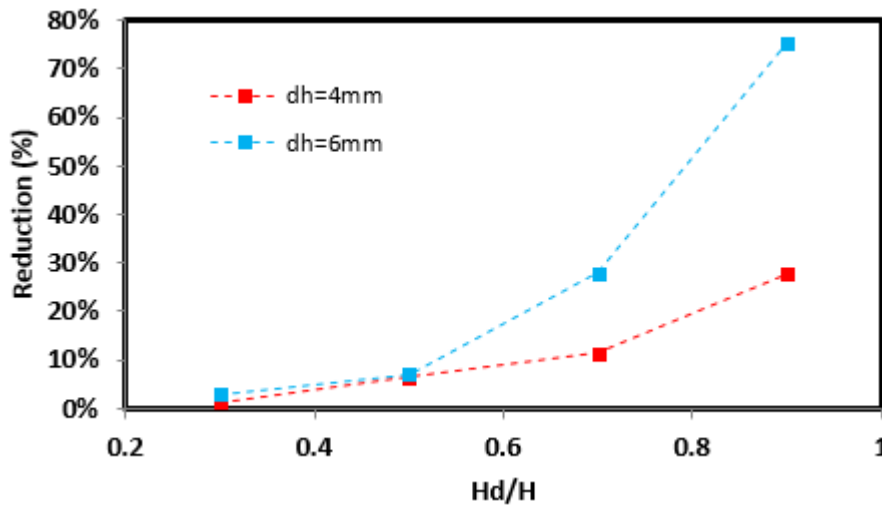
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334 **Figure 9 Sensitivity analysis of the effectiveness of the subsurface dam to the permeability ratio**
 335 **K_d/K**

336

337 Sensitivity analysis was conducted to investigate the effect of the height of the dam and its
 338 hydraulic conductivity on the intrusion length. The hydraulic conductivity of the dam was
 339 expressed relative to that of the aquifer K_d/K and ranged between 0.02 – 0.12. The dam
 340 permeability had small effect on the TL for the steeper hydraulic gradient when $dh=6\text{mm}$ (Fig
 341 9). This is attributed to the greater freshwater flow that repulses the wedge and forces it to
 342 remain on the seaward side of the wall anyway. Hence, changing the dam permeability yields
 343 little effect in the saltwater wedge reduction. By contrast, the effect of the dam permeability
 344 was greater for the smaller head difference $dh=4\text{mm}$ as the TL reduction ranged from $R=9\%$ at
 345 $K_d/K=0.12$ to $R=38\%$ at $K_d/K=0.02$. For this hydraulic gradient, the freshwater is unable to
 346 build great pressure that halts the wedge and hence in this case the dam is the primary obstacle
 347 in the way of the intruding saltwater wedge. Reducing the dam permeability in such case helps
 348 in impeding the wedge and thus yields noticeable TL reduction. As the hydraulic gradients in
 349 real field sites are sometimes lower than the smaller hydraulic gradient investigated here for

350 $dh=4\text{mm}$ ($i=0.0105$) particularly at dry seasons, this means that a dam with smaller
 351 permeability or impermeable material is an effective tool to repulse the saltwater intrusion
 352 especially under such hydrological field conditions with shallow hydraulic gradient.



353

354 **Figure 10 Sensitivity analysis of the effectiveness of the subsurface dam to the ratio H_d/H**

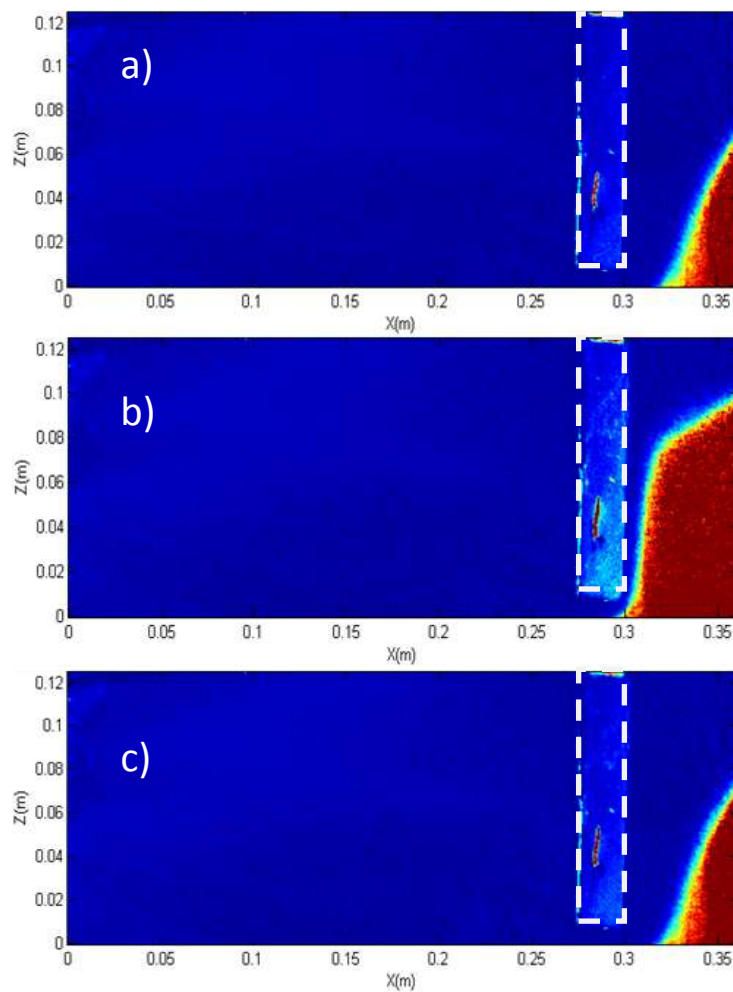
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356 The height of the dam was expressed relative to the depth of the aquifer H_d/H and was examined
 357 for a range 0.3 - 0.9 (Fig 10). The reduction values ranged from 1% to 28% for $dh=4\text{mm}$ and
 358 between 3% and 75% for $dh=6\text{mm}$ as H_d/H was varied from 0.3 to 0.9, respectively. The effect
 359 of the H_d/H ratio was pronounced in the steeper hydraulic gradient and had insignificant effect
 360 in case of $dh=4\text{mm}$. Again, this can be attributed to the insufficient freshwater pressure build-
 361 up in case of smaller head difference $dh=4\text{mm}$ to a level that makes the subsurface dam alone
 362 unable to significantly prevent the saltwater from further intrusion, regardless of how much the
 363 semi-permeable dam covers the aquifer thickness.

364 **4.3 Cutoff wall case**

365 Fig 11 presents the experimental saltwater wedge for the various hydraulic gradients for the
 366 cutoff wall case. The first steady state ($dh=6\text{mm}$) was considered as the initial condition (Fig
 367 11a), where the recorded toe was about 4.5 cm from the coastal boundary. Following the

368 application of $dh=4\text{mm}$, the TL extended to 6.7 cm, which corresponds to reduction in the
369 intrusion length of $R= 63 \%$ compared to the base case (Fig 11b). Laboratory observations
370 revealed that upon lowering the hydraulic gradient, the saltwater wedge rapidly migrated inland
371 before it promptly stopped at the wall opening. The substantial reduction achieved by the cutoff
372 wall results from the increased freshwater velocity as it flows through the reduced cross section
373 below the wall, thereby effectively repulsing the saline water and forcing it to remain in the
374 seaward side of the wall (Anwar, 1983; Kaleris and Ziogas, 2013; Luyun et al., 2011).



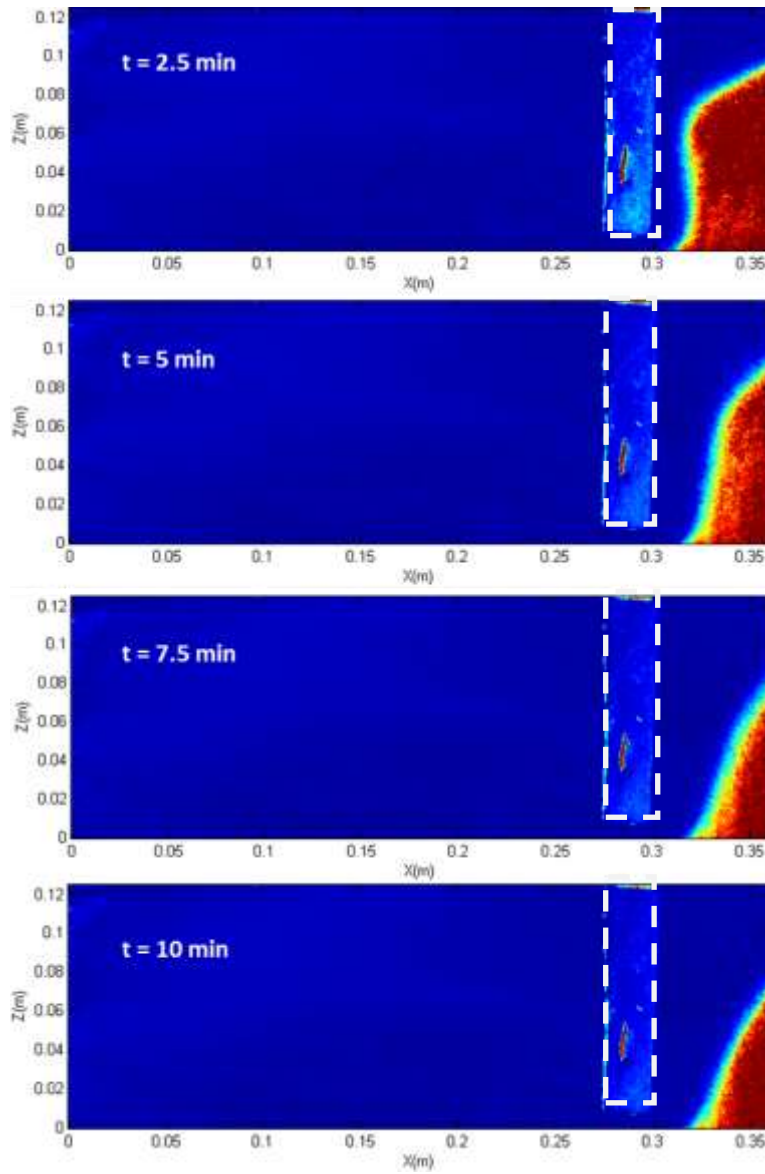
375

376 **Figure 11 Steady-state experimental saltwater wedge for the cutoff wall case; a) $t = 0$ min (initial**
377 **condition); b) at $t = 50$ min; c) at $t = 100$ min**

378

379 After increasing the head difference to $dh=6\text{mm}$ at $t=50$ min, the saltwater wedge receded
380 toward the coastal boundary and the TL was 4.5 cm at steady state, similar to the observed TL
381 at the initial condition (Fig 11c). This corresponds to a toe length reduction of 48% relative to
382 the base case. Laboratory observations reveals that the saltwater retreat was associated with a
383 distortion of the saltwater wedge ($t=2.5$ min) and a widening of the transition zone ($t=5$ and 7.5
384 min), as shown in Fig 12. This interesting observation may be the result of instantaneous
385 increase of the hydraulic gradient which caused an increase of the freshwater flow transmitted
386 to the system. The velocity of freshwater flow was sharply increased at the reduced cross
387 section below the wall, thereby inducing a rather abrupt repulsion of the saltwater wedge
388 associated with a substantial increase of the interface thickness. Such widening of the transition
389 zone was also observed in Robinson et al. (2016) who attributed this to excessive dispersion
390 occurring along the interface essentially induced by the unidirectional flow field that is
391 typically associated with saltwater water retreat (Chang and Clement, 2012).

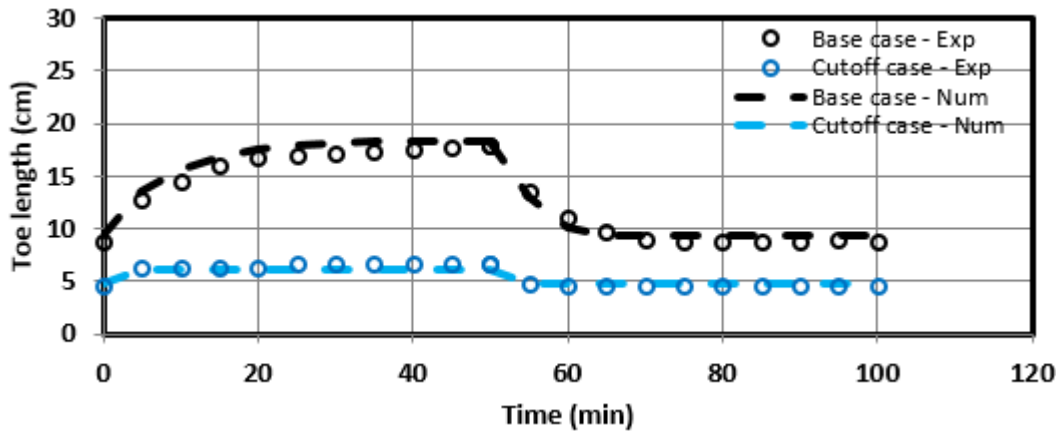
392 Numerical results of the transient toe length for the cutoff wall case are well matched with the
393 experimental data (Fig 13). The system rapidly reached a state of equilibrium within 10 minutes
394 for both hydraulic gradients. The reduction achieved by the cutoff wall was significantly
395 greater for the lower hydraulic gradient. Regardless of the extent of the saltwater wedge before
396 the barrier installation, the cutoff wall was able to maintain the wedge on the seaward side for
397 all the hydraulic gradients tested. Hence the reduction is higher for the smaller hydraulic
398 gradient which initially induced greater TL before the wall installation. This shows the long
399 term reliability of cutoff walls in effectively reducing saltwater intrusion, where the reduction
400 is more pronounced in smaller or shallower hydraulic gradients than steeper gradients. This
401 result demonstrates that the worthiness of installing cutoff walls for seawater intrusion control
402 purposes increases in shallower hydraulic gradients.



403

404

Figure 12 Transient experimental receding saltwater wedge for the cutoff wall case



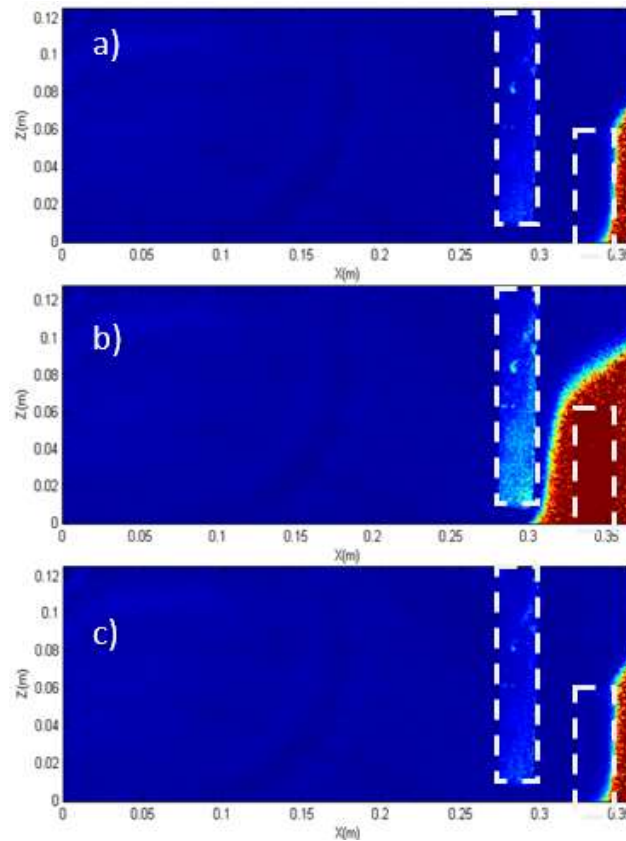
405

406

Figure 13 Transient experimental and numerical toe length results of the cutoff wall case

407

408 **4.4 MPB case**



409

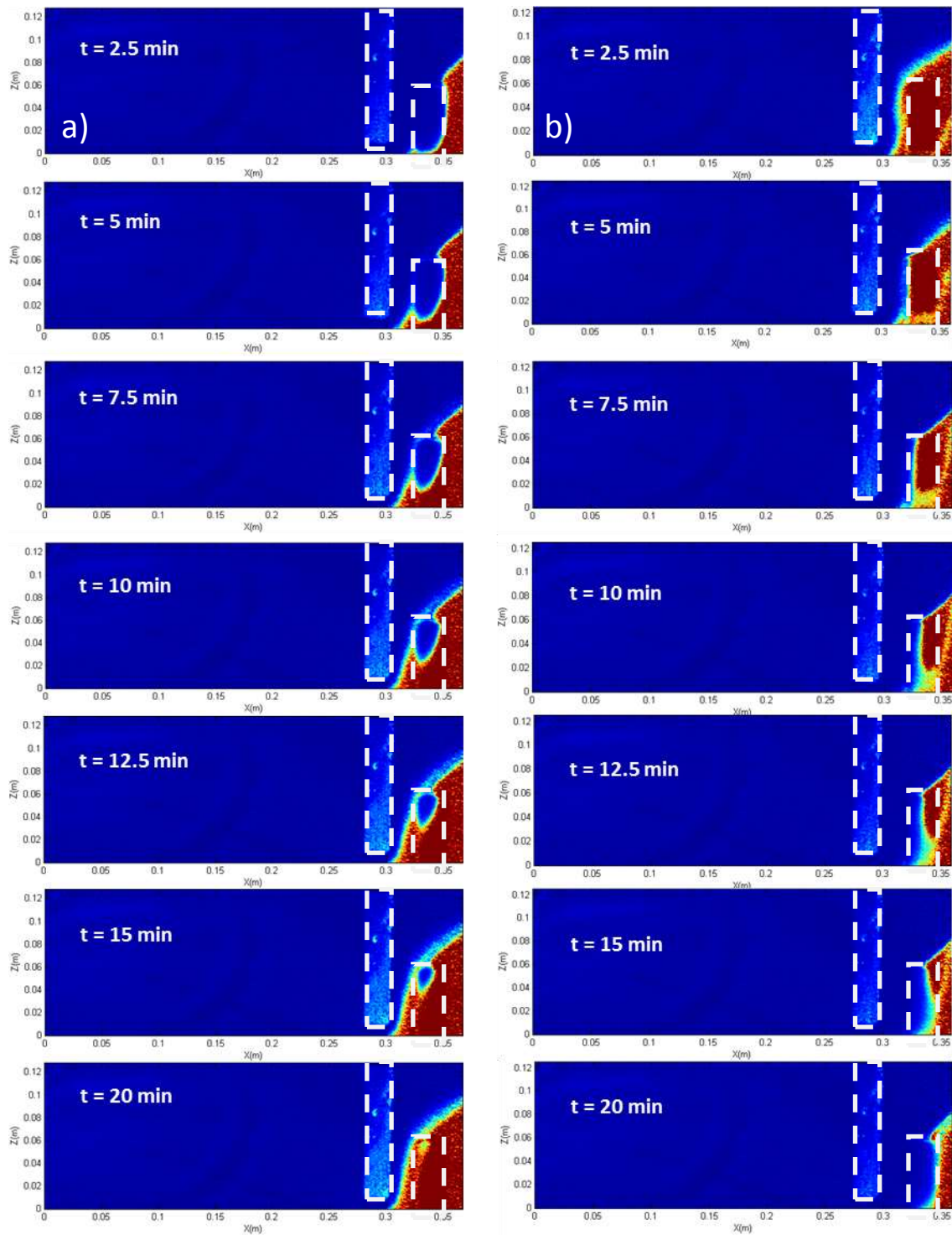
410 **Figure 14 Steady-state experimental saltwater wedge in the MPB case; a) t = 0 min (initial**
411 **condition); b) at t = 50 min; c) at t = 100 min**

412 Fig 14 presents the experimental steady state saltwater wedges for the MPB case. The design
413 parameters of the cutoff wall and the dam cases used here are the same as in the cutoff wall
414 case and subsurface dam case, respectively. Upon imposing the first boundary conditions
415 ($dh=6\text{mm}$), the saline water intruded the system before it was abruptly stopped at the position
416 of the subsurface dam (Fig 14a). The initial intrusion length was 2.6 cm, compared to $TL=8.8$
417 cm recorded in the base case. It is interesting to note that unlike the subsurface dam case, the
418 saline water did not penetrate through the dam here.

419 After applying a head difference of $dh=4\text{mm}$, the saltwater completely penetrated through the
420 dam. The steady state TL was 6.9 cm, corresponding to a reduction R of 61% (Fig 14b). This
421 result indicates that when the freshwater flow was not sufficiently high to prevent the complete

422 saturation of the dam by the saline water, the MBP exhibited similar performance as the single
423 cutoff wall. Laboratory observations revealed the existence of a saltwater lifting mechanism,
424 whereby the residual saline flux was gradually lifted upward and transported over the dam
425 toward the outlet (Fig 15a). This lifting also occurred over the course of the receding phase
426 after increasing the head difference to $dh=6\text{mm}$ (Fig 15b). To the best of our knowledge, this
427 lifting mechanism has not been observed by previous studies. The images clearly show the
428 freshwater flowing through the semi-permeable material of the dam and transporting the dense
429 saline water along the interface.

430 The performance of cutoff walls located nearby the coastline (less than half of the aquifer
431 thickness) depends on the velocity ratio of the freshwater inflow velocity over the velocity of
432 the intruding saltwater driven by density differences (Kaleris and Ziogas, 2013). The combined
433 effects of the cutoff wall and the semi-permeable dam induces an increase of the velocity ratio
434 within the spacing between the barriers, which imposes more resistance to density contrast
435 effects and allows the light freshwater to lift the denser liquid and discharge it outside the
436 domain thereby ensuring an effective obstruction of the saltwater wedge on the seaward side
437 of the dam. The recorded TL was 2.6 cm when the system reached final steady state, which
438 corresponds to a reduction of 70% of the intrusion length (Fig 14c). In other words, the MPB
439 achieved up to 62% and 42% more intrusion length reduction compared to the toe length
440 recorded in the subsurface dam and the cutoff wall cases, respectively.



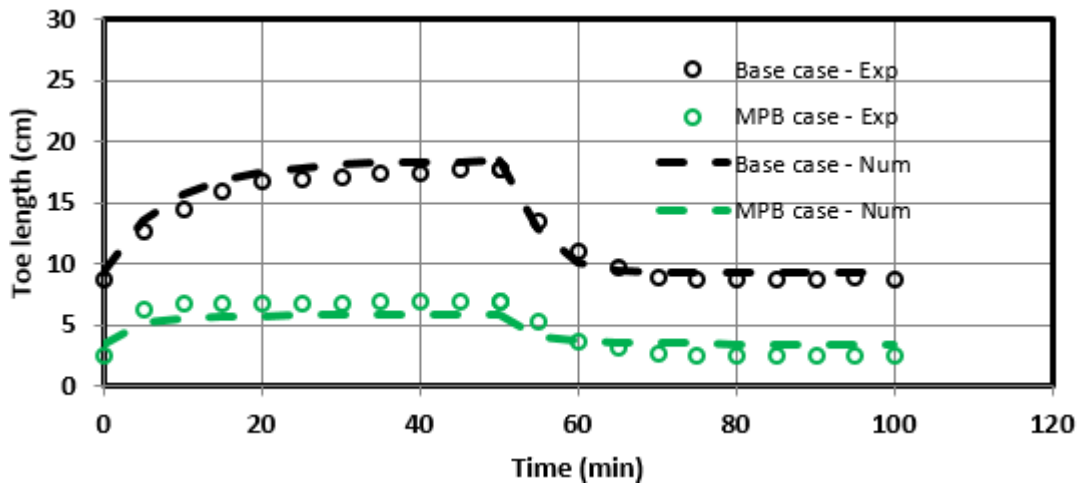
441

442 **Figure 15 Experimental images of the saltwater lifting mechanism a) intruding condition ($dh=4mm$)**
 443 **b) receding condition ($dh=6mm$)**

444

445

446



447
448 **Figure 16 Transient experimental and numerical toe length results of the MPB case**

449

450 The transient dynamics of the saltwater wedge are shown in Fig 16. The transient toe movement
 451 was well reproduced by the numerical model for both hydraulic gradients. The experimental
 452 and numerical data show that the system reached steady state within 15min for both hydraulic
 453 gradients. Additional simulations were conducted to investigate the influence of various key
 454 parameters on the saltwater intrusion length in presence of the MPB. The simulations were run
 455 solely for $dh=6\text{mm}$ where the MPB exhibited the highest efficiency. Simulations were also run
 456 for single cutoff wall for the purpose of comparison. The TL was measured to characterize the
 457 effectiveness of the two barriers relative to each other. The MPB was found considerably more
 458 effective than the subsurface dam, even when the latter was impervious, and hence for this
 459 reason, the case of single semi-permeable dam was not included in the sensitivity analysis.

460

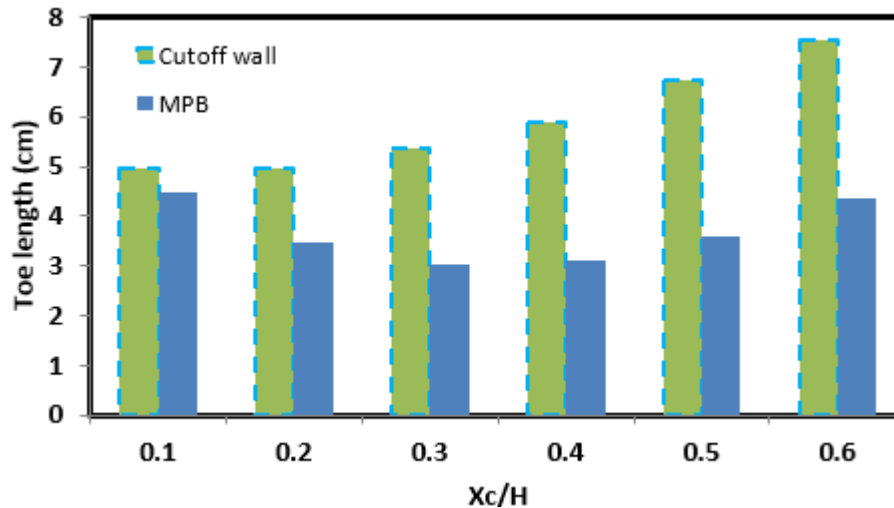


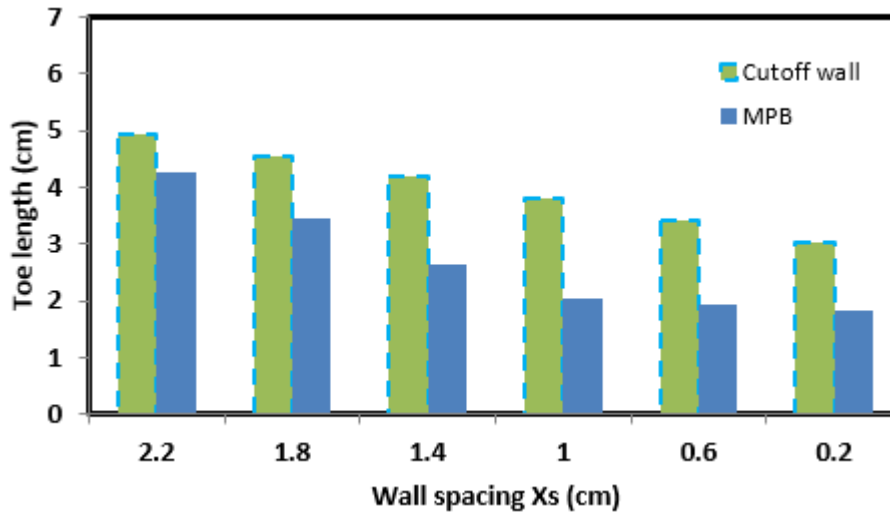
Figure 17 Effect of the ratio X_c/H on the intrusion length in presence of the MPB

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462

463

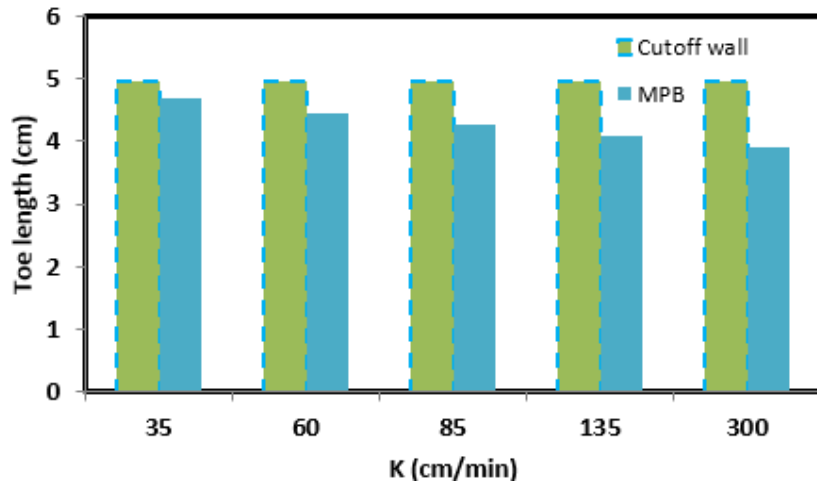
464 The effect of the wall opening size (distance between the wall and aquifer bed) was first
 465 examined, where six X_c/H ratios over the range 0.1-0.6 were tested. Fig 17 shows the TL results
 466 in presence of a MPB and a single cutoff wall. The MPB induced 10% ($X_c/H=0.1$) and 42%
 467 ($X_c/H=0.6$) more reduction in the intrusion length than the cutoff wall. The smallest intrusion
 468 length was observed for $X_c/H=0.3$ in the MPB case. The results indicate that the effect of MPB
 469 on the intrusion length is greater than that of the single cutoff as the wall opening size is
 470 increased. The MPB remains very effective up to opening size as large as $X_c/H=0.6$, which
 471 may imply considerable construction cost saving. In addition, the 42% extra reduction
 472 introduced by the MPB system for $X_c/H=0.6$ could not be achieved when using single cutoff
 473 wall even for wall penetration depth covering 90% of the aquifer thickness ($X_c/H=0.1$). In such
 474 scenario, the MPB was not only substantially more effective in controlling the intrusion, but
 475 could also induce considerable construction cost savings, depending on the site specific
 476 hydrogeological conditions. This may be of particular importance for deep aquifers where the
 477 difference in the penetration depth between the MPB and the cutoff wall may induce significant
 478 saving, even considering the need to construct semi-permeable dam in the MPB case.



479
480 **Figure 18 Effect of the spacing X_s on the intrusion length in presence of the MPB**

481

482 The effect of the spacing X_s between the cutoff and the dam was also investigated. The
 483 subsurface dam was maintained at the same position, while the cutoff was moved seaward,
 484 such that six values of X_s ranging between 0.2-2.2 cm were investigated (Fig 18). The reduction
 485 of the TL achieved by the MPB increased by decreasing the spacing X_s , with a more pronounced
 486 reduction than a single cutoff. The smallest intrusion length was recorded at $X_s=0.2$ cm in the
 487 MPB case, albeit this may be hardly feasible in practical situation. Note that for the range 0.2-
 488 1.0 cm, only little effect on the toe length was observed in the case of the MPB, while the
 489 performance of the single cutoff wall reached a maximum value for a wall position
 490 corresponding to $X_s=0.2$ cm, i.e. when the wall was installed at 4.6 cm from the coastline
 491 boundary. The TL was 1.82 cm and 3.02 cm for the MPB and single cutoff, respectively. In
 492 other words, the MPB achieved 40% more saltwater wedge reduction than the single cutoff for
 493 the smallest spacing considered. Given that moving the cutoff in the seaward direction would
 494 allow greater fresh groundwater storage, this finding implies that a more optimal use of the
 495 available freshwater could be associated with a more effective control of the saltwater intrusion
 496 process using an MPB system compared to a single cutoff wall system, for equivalent seaward
 497 displacement of the impermeable wall.

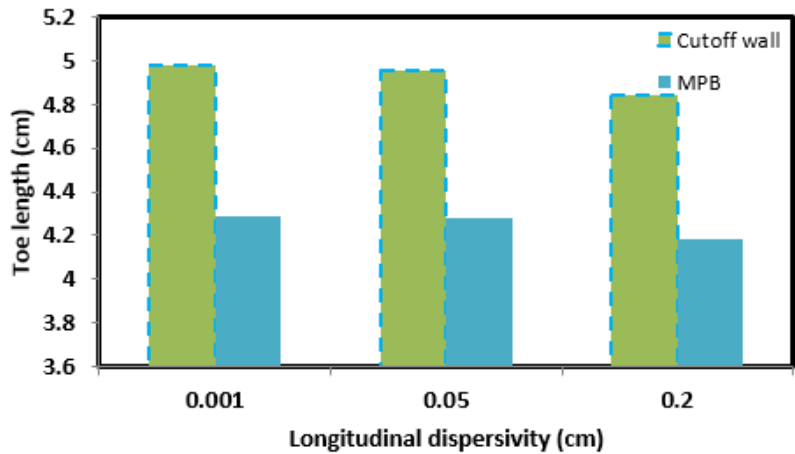


498

499 **Figure 19 Effect of the aquifer hydraulic conductivity on the intrusion length in presence of the**
 500 **MPB**

501

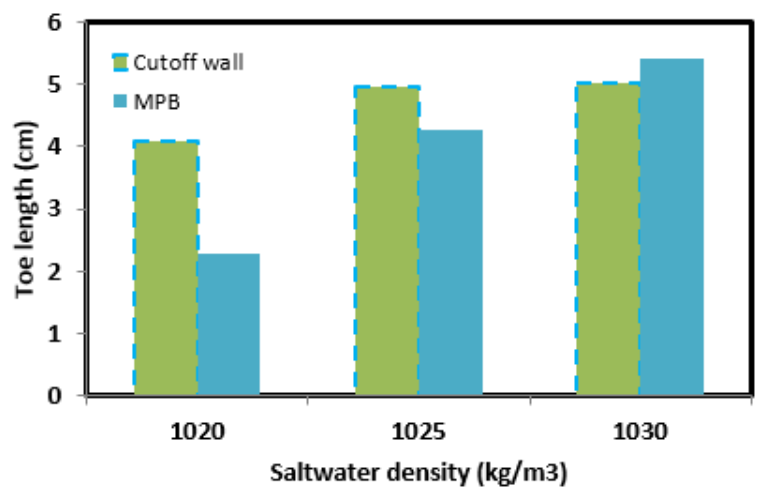
502 The effect of the hydraulic conductivity of the porous medium on the barrier performance was
 503 examined over the range 35-300 cm/min (Fig 19). While the *TL* remains nearly the same in
 504 presence of single cutoff wall for the various *K* values, it continuously decreases with
 505 increasing *K* when using the MPB barrier system. The effect of hydraulic conductivity in the
 506 MPB case may be attributed to the permeability contrast between the dam and the background
 507 aquifer permeability, which keeps varying for different aquifer permeability. As the latter
 508 increases, this contrast ratio becomes bigger. The MPB induced between 5% and 21% more
 509 reduction than the cutoff wall as *K* varied from 35 to 300 cm/min respectively. This result
 510 indicates that the relative effectiveness of MPB compared to a single cutoff is expected to
 511 increase with increasing aquifer hydraulic conductivity.



512

513 **Figure 20 Effect of the longitudinal dispersivity of the aquifer on the intrusion length in presence**
 514 **of the MPB**

515 The effect of the dispersivity coefficients on the performance of MPB was also investigated
 516 (Fig 20). Three values of longitudinal dispersivity were tested: 0.001, 0.05 and 0.2 cm. The
 517 transversal to longitudinal dispersivity ratio remained constant. The net *TL* reduction was
 518 estimated at 2.5% and 2.8%, for the MPB and the cutoff wall, respectively. For the lowest and
 519 highest dispersivity values considered, the MPB induced about 14% additional reduction in the
 520 *TL* for the two extreme dispersivity values considered. The results show that the effectiveness
 521 of the MPB increases for systems with higher dispersivity. The impact of MPB on the saltwater
 522 intrusion length compared to that of a single cutoff wall is therefore expected to be greater in
 523 highly dispersive coastal groundwater systems.



524

525 **Figure 21 Effect of the saltwater density on the intrusion length in presence of the MPB**

526 Results of the influence of the density contrast on *TL* are presented in Fig 21, where three
527 saltwater density contrast between seawater and freshwater of 1.020, 1.025 and 1.030 were
528 examined. The increase in density contrast induced an increase of the intrusion length by 57%
529 for the MPB case, and 18% for the single cutoff case. For the lowest density, the MPB achieved
530 44% more reduction than the single cutoff wall. By contrast, for the highest density difference
531 considered, the single cutoff achieved about 7.8% more reduction of the *TL* than the MPB. The
532 results show that the effectiveness of the MPB increases substantially for lower saltwater
533 density. Obviously, the decrement of the saltwater density eases the lifting of saline flux by the
534 MPB. This result implies that the MPB may display good efficiency in real scale aquifer setting,
535 particularly in zones where wide transition zone generally occurs, where saltwater
536 concentration is subsequently reduced as a result of micro/macro scale heterogeneity. The
537 results suggest that more reduction of the intrusion length may be achieved with the MPB than
538 a single cutoff in coastal groundwater systems with saltwater solutions inferior or equal to 1025
539 kg/m³. The performance of the MPB may however be lower for higher saltwater density values.

540 **5. Summary and Conclusions**

541 This study provides a thorough analysis of the effect of subsurface physical barriers on
542 saltwater intrusion dynamics under transient conditions. A new barrier system was suggested
543 as saltwater intrusion control method: the mixed physical barrier MPB, which combines an
544 impermeable cutoff wall and semi-permeable subsurface dam located on its seaward side.
545 Using laboratory experiments and numerical simulations, the effect of the semi-permeable
546 subsurface dam, cutoff wall and MPB on saltwater intrusion dynamics was investigated for
547 different hydraulic gradients. The sensitivity of the performance of these different barriers to
548 some key design and hydrogeological parameters was then explored. The main findings of the
549 study are:

- 550 • Subsurface dams constructed from semi-permeable material do not provide suitable control
551 of the saltwater intrusion process. A reduction in the toe length may be exhibited provided
552 that the groundwater flux is sufficiently high to assist dam in retaining the intruding
553 saltwater wedge. They primarily affect the rate of the saltwater transport process but this
554 effect is rapidly dissipated after complete saturation of the dam by the saline water. In the
555 cases investigated here, the semi-permeable dam eventually induced a negative effect on
556 wedge length when the hydraulic gradient was lower, causing the toe length to extend
557 beyond the toe location observed prior the dam installation.
- 558 • The worthiness of installing cutoff walls for saltwater intrusion control purposes increases
559 as the hydraulic gradient becomes smaller or shallower. In the cases considered here, the
560 cutoff wall was able to reduce the toe length by up to 63%.
- 561 • The MPB induced a visible saltwater lifting process, whereby freshwater flowing below the
562 wall opening with increased velocity transported dispersive flux of saltwater above the
563 subsurface dam and discharged it towards the outlet. This lifting mechanism has significant
564 effect on the intrusion length, especially when the hydraulic gradient was relatively steep,
565 where it yielded up to 70% reduction of the initial intrusion length, corresponding to 42%
566 more reduction than the single cutoff wall and 62% more than the semi permeable
567 subsurface dam alone.
- 568 • While the effectiveness of single cutoff walls is limited to wall opening sizes not exceeding
569 40% of the aquifer thickness, the MPB exhibited good reduction for wall opening size
570 extending up to 60% of the aquifer thickness, where it could exhibit up to 42% more
571 reduction than a single cutoff wall. This reduction could not be achieved using single cutoff
572 wall even for wall penetration depth covering 90% of the aquifer thickness. This finding
573 therefore implies that there may be a potential for construction cost savings by installing
574 impermeable wall with shorter penetration depth when using MPB (especially in deep

575 coastal aquifer systems), and at the same time best ensuring the repulsion of intruding saline
576 water.

577 • For equivalent seaward displacement of the impermeable wall, the MPB displayed better
578 obstruction of the intruding saline water, achieving up to 40% more intrusion length
579 reduction than the single cutoff wall. This finding implies that displacing the impermeable
580 wall of the MPB seaward would not only ensure a more reliable prevention against saltwater
581 intrusion, but also allow a more optimal use of the available freshwater volume, which is
582 essential from a prospective of water resources management.

583 • The effectiveness of the MPB was found to increase with increasing hydraulic conductivity,
584 dispersivity and decreasing saltwater density ($<1025 \text{ kg/m}^3$) of the coastal groundwater
585 system.

586 In field applications, the installation of the MPB is expected to be more suitable in high
587 hydraulic conductivity aquifers (e.g. sand, gravel), where the groundwater flow velocity is
588 high. In such conditions, the effect of the MPB in increasing the freshwater inflow velocity
589 over the velocity of the intruding saltwater within the spacing between the wall and the semi-
590 permeable dam will be more feasible. In addition, real aquifers generally exhibit higher
591 dispersion often associated with micro/macro scale heterogeneity, which results in
592 considerable widening of the freshwater-saltwater transition zone with different salt
593 concentrations. Consequently, the toe of a marine saltwater intrusion may meet the inland
594 freshwater with only slightly elevated concentrations (brines). This low density contrast
595 between the intruding saline water and fresh groundwater may therefore further enhance the
596 ability of the MPB to lift up saline flux and repulse it seaward.

597 Additional experiments and modelling would however be recommended for future work to
598 further explore the field practicability of this system. For instance, the effect of large-scale
599 model, 3D effects and the bottom boundary morphology are clearly worthy of further analyses.

600 Our ongoing work focus on this and also on exploring the effectiveness of the MPB in
601 heterogeneous aquifers and this shall be the subjects of future publications.

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