

1 **How does layering heterogeneity affect the ability of subsurface dams to clean up coastal**
2 **aquifers contaminated with seawater intrusion?**

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6
7 **Abstract**

8 The main purpose of this work was to examine how aquifer layering impacts the ability of
9 subsurface dams to retain seawater intrusion (SWI) and to clean up contaminated coastal
10 aquifers using both experimental and numerical techniques. Four different layering
11 configurations were investigated, including a homogeneous case (case H), and three different
12 layered cases where a low permeability layer was set at the top of the aquifer (case LH), at the
13 middle part of the aquifer as interlayer (case HLH), and at the lower part of the aquifer (case
14 HL). The subsurface dam was able to retain the saltwater wedge associated with a drop of the
15 hydraulic gradient from 0.0158 down to 0.0095 in all the cases, thereby achieving up to 78%
16 reduction in the saltwater toe length. In cases LH and HLH, the start of the saltwater spillage
17 was delayed compared to the homogeneous case, and the time taken for the freshwater zone to
18 be fully contaminated (post-spillage) was twice and three times longer, respectively. By
19 contrast, the existence of a low K layer at the bottom of the aquifer (case HL) considerably
20 weakened the ability of dams to retain the intrusion, allowing for quicker saltwater spillage
21 past the wall. The natural cleanup of SWI-contaminated coastal aquifers was, for the first
22 time, evidenced in heterogeneous settings. Depending on the stratification pattern, the
23 presence of stratified layers however prolonged the cleanup time to various degrees,
24 compared to the homogeneous scenario, particularly in case HL, where the cleanup time was
25 nearly 50% longer.

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27 experiments; SEAWAT; Aquifer Remediation; Subsurface heterogeneity

28

29 **1. Introduction**

30 With the increasing water demand, the management of coastal aquifers has been a primordial
31 source of distress for coastal populations. Coastal aquifers represent natural underground
32 storage of fresh groundwater located along the shores. While these constitute vital sources of
33 water supply for people living along the shores, they remain very sensitive to degradation due
34 to their proximity with oceanic seawater, specifically to seawater intrusion, which refers to the
35 subsurface movement of seawater into the fresh groundwater. Factors such as groundwater
36 pumping, intermittent sea level fluctuations (e.g. tides) as well as global warming may alter
37 the natural groundwater hydraulic gradient and amplify the intrusion process. The primary
38 adverse effects of SWI are the reduction of the available freshwater volume as well as the
39 abandonment of contaminated production wells. Mixing the fresh groundwater with only 3-
40 4% of saltwater is enough to render it unsuitable for drinking or irrigation purposes and rising
41 this to 6% will render the groundwater unfit for all purposes except for cooling (Morris et al.,
42 2003).

43 The preservation of groundwater quality in coastal areas has promoted the deployment of
44 various practical engineering applications affecting the hydrodynamic of the aquifer, through
45 physical alteration of the aquifer and/or groundwater recharge (Werner et al., 2013). Amongst
46 these are the underground barriers, which are essentially impermeable walls constructed along
47 the seashores, by way of grouting low permeability material to obstruct the inland motion of
48 the saline plume and protect groundwater resources. The use of physical barriers as a SWI
49 control method has been the focus of several studies (Archwichai et al., 2005; Sugio et al.,
50 1987; Anwar, 1983; Kaleris and Ziogas, 2013; Luyun et al., 2009; Strack et al., 2016;

51 Abdoulhalik and Ahmed, 2017; Abdoulhalik et al., 2017). The two main types of physical
52 barriers include the subsurface dam and the cutoff wall. The first type is set in the lower part
53 of the aquifer while an opening is left in the upper part for the seaward freshwater discharge,
54 thereby physically obstructing the inland penetration of saline water. The second type of
55 barrier covers the upper part of the aquifer, while an opening is left at the bottom through
56 which freshwater flows at higher velocity.

57 Abdoulhalik et al. (2017) recently proposed a new barrier system called mixed physical
58 barrier (MPB), which consists in the simultaneous application of a cutoff wall and semi-
59 permeable dam. Their results show that the MPB caused a visible saltwater lifting process
60 whereby freshwater flowing below the wall opening with increased velocity transported
61 dispersive flux of salt above the subsurface dam and discharged it towards the outlet. This
62 lifting mechanism yielded significant reduction of the intrusion length. Strack et al. (2016)
63 recently suggested an excavation-free method of barrier installation, which consists in
64 reducing the hydraulic conductivity of the upper part of the aquifer by injecting precipitate at
65 the surface downstream from production wells to mitigate SWI. The appraisal of the
66 practicality of this method in field application needs nevertheless further investigations.

67 The viability of physical barriers has been discussed in previous studies (e.g. Hasan Basri,
68 2001; Sugio et al., 1987). Hasan Basri (2001) suggested two methods for optimal design of
69 subsurface dams to increase the cost-effectiveness of the implementation of this
70 countermeasure. This type of barrier has met a great success in Japan, where advanced
71 construction procedures have been deployed allowing noticeable saving in construction cost
72 normally involved with the implementation of this method (Luyun, 2010). Hanson and
73 Nilsson (1986) reported from field study that areas with 1-5% slope are the most feasible for
74 subsurface dam installation, especially in high hydraulic conductivity environment.

75 The effect of subsurface dams on saltwater intrusion has been investigated in Luyun et al.
76 (2009) who provided an experimental study on the transient flushing rate of intruded saline
77 water over underground dams of various heights. They concluded that a smaller wall height
78 yielded faster flushing of saline water, as well as a smaller vertical extension of intruding
79 saline plume along the shore. While the result presented by Luyun et al. (2009) are valuable
80 for improving the understanding of flow dynamics imposed by subsurface dams, the previous
81 investigations have so far only been limited to homogeneous soil formations, which is rarely
82 found in real world problems. While heterogeneity is generally known to disturb the flow over
83 many length scales (Abarca, 2006), prevalent heterogeneous formations such as aquifer
84 stratification have been found to significantly modifies the flow path and rate near the coastal
85 boundary (Lu et al., 2013, Abdoulhalik and Ahmed, 2017). The presence of such
86 heterogeneous layering is likely to strongly affect the performance of subsurface dams in
87 preventing SWI.

88 To address this point, this paper aims to examine the use of subsurface dams as SWI intrusion
89 control in heterogeneous aquifers. The effectiveness of subsurface dams was characterized by
90 the ability 1) to restrict saltwater spillage and 2) to clean up the freshwater zone from residual
91 saline water. This study provides for the first time an analysis of the spillage of saline water
92 over the subsurface dam, which has never been captured in previous studies. More generally,
93 this study is amongst the first attempts to provide insight on transience SWI in typical
94 heterogeneous coastal aquifer settings in physical model.

95 The investigation was completed using a combination of laboratory experiments and
96 numerical modelling simulations. The experiments were conducted in head-controlled
97 groundwater system, where the freshwater level was varied to simulate groundwater
98 fluctuations. Such aquifer systems deserve particular attention given their higher vulnerability
99 to seawater intrusion compared to flux-controlled systems particularly when resulting from

100 tidal fluctuations (Ataie-Ashtiani et al., 1999) and/or sea level rise (Ketabchi et al., 2016), and
101 also because head-controlled aquifers represent more than 50% of the total world coastal
102 aquifers (Michael et al., 2013). The numerical simulations were completed using the computer
103 model SEAWAT for the validation of the experimental data.

104 **2. Materials and methods**

105 **2.1. Experimental method**

106 A laboratory flow tank of dimension 0.38 m x 0.15 m x 0.01 m was used to carry out the
107 experiments (Fig 1). The tank was composed of three main parts, namely a central chamber to
108 simulate the porous media and two side reservoirs at either side to impose head boundary
109 conditions. The central chamber and the side reservoirs were separated by two fine mesh
110 acrylic screens. Clear glass beads from Whitehouse Scientific® were siphoned into the central
111 chamber under saturated conditions to limit the risks of air entrapment to simulate the porous
112 medium. The packing of the beads was completed in even-sized layers and each layer was
113 carefully tamped to provide uniform compaction.

114 The left and right side reservoirs were used to supply freshwater and saltwater to the system,
115 respectively. The saltwater solution was prepared prior to the experiments by dissolving
116 commercial salt into freshwater at a concentration of 36.16 g/L. The saltwater solution was
117 dyed with red food colour at a concentration of 0.15 g/L. The density of the saltwater solution
118 was measured at 1025 kg/m³ using a hydrometer (H-B Durac plain-form polycarbonate) and
119 manually using mass/volume ratio.

120 Saltwater concentration was correlated with the intensity of the light transmitting through the
121 main chamber using a calibration procedure, as described in details in Robinson et al. (2015,
122 2016). The light intensity-concentration conversion allowed the determination of key
123 intrusion parameters under transient conditions. The images of the saltwater intrusion
124 experiments were captured with a high speed camera with a resolution of 1280 x 1024 pixels

125 and an 8-bit grayscale pixel depth. A MATLAB code was then used to obtain the light
126 intensity-concentration parameters and then analyse all the experimental images to calculate
127 the toe length of the saltwater wedge and provide maps of the solute concentration throughout
128 the system.

129 In total, two sets of four experiments were completed (Fig 2), which included one set of base
130 cases (without barrier) and another set incorporating a subsurface dam. The four base cases
131 included a homogeneous case with relatively high permeability (K), designated hereafter as
132 case H, and three different layered cases where a low K layer was set at three different
133 locations: case Low K-High K (LH) presented a scenario where a low K layer was set in the
134 top part of the aquifer; case High K-Low K-High K (HLH) referred to the case where a low K
135 layer was located in the middle part of the aquifer; and case High K-Low K (HL) presented a
136 scenario where a low K layer was set along the aquifer bottom. In all the cases, the thickness
137 of the low K layer was about one third of the total saturated thickness of the homogeneous
138 case $h = 136$ mm. The nominal diameter of the glass beads used to simulate the porous media
139 and the low K layer was $1325 \mu\text{m}$ and $780 \mu\text{m}$, respectively. The average hydraulic
140 conductivity of each type of beads was measured within the experimental flow tank using
141 Darcy's law. The average hydraulic conductivity was estimated at 36 cm/min and 108 cm/min
142 for the beads of size $780 \mu\text{m}$ and $1325 \mu\text{m}$, respectively.

143 The second set of experiments included a subsurface dam installed prior to siphoning of the
144 beads into the tank. The subsurface dam was simulated using 12 mm wide PVC material
145 covering the thickness of the tank. The dam was located at 50 mm from the seaside boundary,
146 and has a height of 66 mm from the bottom boundary of the tank (about half of the saturated
147 aquifer). The effect of the subsurface dam was examined within each of the four different
148 aquifer settings, similar to the base cases.

149 In total, 48 experimental cases were carried out in this investigation. These includes 20
150 different experiments (4 physical experiments x 5 different hydraulic gradients) for the base
151 cases where the saltwater wedge was analysed in advancing and receding conditions; and 28
152 different experiments (4 physical experiments x 7 different hydraulic gradients) for the
153 subsurface dam cases, where the ability of subsurface dams to retain SWI and clean up
154 aquifers from previously intruded saline water was assessed in the various aquifer settings.

155 **2.2. Experimental procedure**

156 The various hydraulic gradients were simulated by varying the freshwater level such that
157 various head differences were successively imposed to the system. In all the investigated
158 cases, the initial condition was set by forcing a head of 135.7 mm at the freshwater boundary
159 to impose a first head difference $dh = 6$ mm to the system, corresponding to a hydraulic
160 gradient of 0.0158. The dense saltwater solution was allowed to intrude into a fully freshwater
161 aquifer, until the system reached the first steady state condition.

162 In the base cases, three head differences were applied thereafter, including $dh = 5.2$ mm, $dh =$
163 4.4 mm, $dh = 3.6$ mm, corresponding to hydraulic gradients of 0.0137, 0.0116 and 0.0095,
164 respectively. The final head difference was eventually reset to the initial value $dh = 6$ mm to
165 allow the analysis of the seaward motion of the saltwater.

166 In the subsurface dam cases, two additional head differences were imposed to the system,
167 specifically $dh = 2.8$ mm and $dh = 2$ mm, corresponding to a hydraulic gradient of 0.0074 and
168 0.0053, respectively, before returning the head to $dh = 6$ mm. The application of these
169 additional head difference was primarily to ensure the spillage of the saline water over the
170 wall, which is primordial in this investigation. The highest and lowest head differences
171 applied to the system $d = 6$ mm and $dh = 2$ mm corresponded to hydraulic gradient values of
172 0.0158 and 0.0053, respectively. These gradient values are typical values used in similar

173 laboratory studies (Abdoulhalik et al., 2017; Goswami and Clement, 2007; Chang and
174 Clement, 2012) and within the range of values measured in some real coastal aquifers
175 (Ferguson and Gleesson, 2012; Attanayake and Michael, 2007).

176 The investigation of the effect of the subsurface dam on saltwater intrusion dynamics was
177 subdivided into two main phases, namely the advancing-wedge and the receding-wedge
178 phases. The advancing-wedge phase includes the period prior to spillage where saltwater
179 builds up in the seaward side of the wall, and the period post-spillage where saline water
180 overflows the crest of the subsurface dam and penetrates into the freshwater zone. The
181 receding-wedge phase relates to the removal of the residual saline water from the freshwater
182 zone, after restoration of the initial freshwater head boundary condition.

183 The effectiveness of subsurface dams was characterized by two different criteria, depending
184 on the phase analysed. The first criterion, used in the advancing-wedge phase, was the ability
185 to restrict the SWI mechanism, which was identified differently depending on the location of
186 the saltwater wedge toe on either side of the wall. When located on the seaward side of the
187 wall (prior to spillage), the percentage reduction of the saltwater wedge length R was used,
188 where $R = (X_0 - X_d)/X_0$, with X_0 and X_d are the intrusion length before and after the dam
189 installation. When the toe was located on the landward side of the wall, the ability to restrict
190 SWI was identified by T_{spil} and T_{crit} , corresponding respectively to the time taken for the
191 saline water to start spilling over the wall and the time taken to reach the critical point X_{crit} ,
192 which was arbitrarily located at 90% of the total aquifer length from the seaside, at which the
193 freshwater was considered completely contaminated. In the current system, the critical point
194 X_{crit} was located at 34 cm from the coastline. For the sake of convenience, the time of spillage
195 T_{spil} was defined as the time at which the overflowing of the saline water reaches the aquifer
196 bottom in the landward side of the dam.

197 The second criterion used to characterise the performance of subsurface dams was the ability
198 to completely flush out residual saline water in the seaward side of the wall during the
199 receding-wedge phase. It was characterized by the time required for the freshwater zone to be
200 completely cleaned up T_{flush} .

201 **2.3. Numerical method and procedure**

202 The SEAWAT code (Guo et al., 2002) was adopted to validate the experimental results. The
203 numerical model consisted in a rectangular domain of dimensions 38 x 14 cm with uniform
204 size mesh of 0.2 cm representing the porous media chamber. The longitudinal dispersivity and
205 the transverse dispersivity values were set to 0.1 cm and 0.05 cm, respectively. The
206 dispersivity and element dimensions provided numerical stability by satisfying the Peclet
207 number criterion (Voss and Provost, 2010). A freshwater ($C = 0$ g/L) hydrostatic boundary
208 condition was forced on the left side boundary and a hydrostatic saltwater ($C = 36.16$ g/L)
209 boundary condition was applied on the right side boundary. The time step of the simulations
210 was 0.5 min and 1 min for the base case and subsurface dam case simulations, respectively. A
211 summary of the parameters involved in the numerical simulations is presented in table 1.

212 The SEAWAT code was used to simulate the base cases to assess the validity of the
213 numerical model. At the initial condition, the model domain corresponded to an entirely fresh
214 aquifer. The first stress period was used to set the first steady state condition, whereby the
215 freshwater and saltwater boundary were set at 135.7 mm and 129.7 mm, respectively,
216 allowing penetration of saline water into a fully fresh model domain. In the next three stress
217 periods, the freshwater head was dropped such that to impose head differences $dh = 5.2$ mm
218 and 4.4 mm, 3.6 mm to the system. The last stress period was dedicated for the retreat of the
219 saltwater water wedge, following the rise of the head difference to its initial value ($dh = 6$
220 mm).

221 The SEAWAT models were then used to perform numerical simulations incorporating the
222 subsurface dam. The later was simulated by rendering the cells occupied by the wall as
223 inactive. As noted above, two extra stress periods were added ($dh = 2.8$ mm and $dh = 2$ mm)
224 in the subsurface dam simulation to reproduce the spillage. The models were then used again
225 to perform numerical simulations of the receding phase of the saline water in presence of the
226 subsurface dam. The initial condition corresponded to the final wedge for $dh = 2$ mm. A
227 single stress period was thereafter used to initiate the saline water flushing process, following
228 the rise of the inland freshwater head boundary to 135.7 mm to reset the initial $dh = 6$ mm.

229 **3. Results and discussion**

230 **3.1. Base cases**

231
232 The assessment of the effectiveness of the subsurface dam and the understanding of the flow
233 dynamics imposed by each layering pattern required first the analysis of saltwater intrusion
234 dynamics in each aquifer setting, with no barrier. Fig 3 presents the concentration colour map
235 of the base cases at the initial condition, i.e. after the application of the initial head difference
236 $dh = 6$ mm. This first head change disrupted the equilibrium of the system and allowed the
237 penetration of the saline water into the porous medium, forming an idealized wedge-like
238 shape of the plume in homogeneous conditions, while slightly distorted in the heterogeneous
239 cases HL and HLH, where the freshwater-saltwater interface crosses the boundary between
240 two layers of contrasted permeability (Abdoulhalik and Ahmed, 2017). Such distortion of the
241 wedge does not however occur in case LH, as the wedge penetrates “freely” into the high
242 permeability zone, which accounts for two thirds of the aquifer height.

243 The further decrement of the head difference down to $dh = 3.6$ mm induced a reduction in the
244 freshwater flux transmitted to the system and thus allowing deeper inland encroachment of the
245 saltwater wedge. The toe length data of all the investigated cases are presented in table 2. The
246 subsequent increase of the freshwater flow following resetting of the initial head difference to

247 $dh = 6$ mm forced the retreat of the saltwater toward the coastline boundary (Fig 4). The toe
248 reached the same position as in the initial condition in all cases, which indicates that no
249 hysteresis occurred in the system.

250 The data show that the shortest saltwater intrusion toe length was exhibited in case LH for all
251 the inland heads applied. In such configuration, the existence of the low K on the top of the
252 aquifer drives part of the freshwater flow into the bottom layer that has greater hydraulic
253 conductivity, i.e. directly facing the saltwater wedge, thereby obstructing its inland
254 penetration. In other words, the freshwater flow is increased in the lower part of the aquifer,
255 which leads to a greater repulsion of the saltwater wedge back towards the coast. This result is
256 in agreement with the steady state analysis presented by Strack et al. (2016), where similar
257 configuration was examined. The transient data provided in Fig 4 shows that the receding toe
258 motion in this setting is noticeably faster compared to the homogeneous scenario, which
259 indicate higher freshwater flow velocity promoting faster repulsion of the saline wedge.

260 The toe length was also shorter in case HLH relative to the homogeneous case, albeit the
261 difference is less obvious here. The low K layer in the middle portion of the aquifer is
262 expected to force the freshwater to flow on the top and bottom parts of the aquifer. While the
263 freshwater flowing in the top high K layer exits the system without substantial contribution in
264 the saltwater wedge repulsion, the flow in the bottom layer of high K has greater impact to
265 push the wedge in the seaward direction resulting in shorter wedge compared to the
266 homogeneous scenario. This observation is analogous to that reported in Abdoulhalik and
267 Ahmed (2017) and Lu et al. (2013) where saltwater intrusion mechanism in such typical
268 heterogeneous aquifer setting was also analysed.

269 The longer toe length values recorded in case HL compared to those observed in case LH are
270 consistent with Strack et al. (2015) where the saltwater intrusion length in their dual-layered

271 aquifer with underlying low K layer was up to twice longer than the opposite scenario. The
272 transient data shows that the toe motion exhibited in this setting is considerably slower
273 compared to the other cases. While the saltwater intrusion process is mainly controlled by the
274 freshwater flow transmitted through the system (Chang and Clement, 2012), the freshwater
275 flow transiting in the lower part of the aquifer is considerably slowed through the underlying
276 low K layer, which resulted in inhibiting the effective seaward repulsion of the saline water.
277 The subsequent increase of the flow velocity in the upper part of the aquifer is little involved
278 in the repulsion effort, but rather directly exits at the outlet.

279 The comparison between the experimental and numerical toe length results of the base cases
280 are shown in Fig 5. The transient experimental toe length data were very well predicted by the
281 SEAWAT model in all the cases. The largest toe length was however observed in case HL,
282 while compared to the other numerical cases. This may be because the experimental case HL
283 has not reached the complete steady-state condition, as the penetration of the wedge was very
284 slow through the underlying low K layer. The numerical results nonetheless show that the
285 minimum intrusion length was occurs in case LH, in agreement with the experimental
286 observations. The resulting models were then used to simulate the subsequent subsurface dam
287 experiments for each respective aquifer setting, as shown below.

288 **3.2. Subsurface dam cases**

289 **Advancing-wedge phase**

290 Fig 6 shows the concentration colour maps of the subsurface dam experiments at the initial
291 conditions, i.e after applying $dh = 6$ mm. In all the investigated cases, the subsurface dam was
292 able to retain the intrusion of saline water for all the head differences applied to the base
293 cases, i.e. up to $dh = 3.6$ mm, which means that the subsurface dam could withstand the
294 saltwater intrusion process associated with a decrement of the gradient from 0.0158 down to
295 0.0095. This was expected because the height of the saltwater wedge in the base cases at the

296 location of the wall is slightly smaller than the height of the subsurface dam (Luyun et al.,
297 2009; Abdoulhalik et al., 2017). The values of the percentage reduction of intrusion length R
298 achieved by the subsurface dam are presented in table 3. The lowest values of reduction are
299 recorded in case LH for all the head differences tested. This is because the difference $X_0 - X_d$
300 is the smallest in case LH, given that it exhibited the smallest toe length values prior to wall
301 installation, while X_d is limited by the location of the subsurface dam in all the cases.

302 In order to observe the spillage of saline water over the wall, the head difference was
303 thereafter gradually decreased by maintaining a step head decrement of 0.8 mm. The initial
304 condition of this experiment ($t = 0$ min) corresponded to the steady state saltwater wedge
305 under $dh = 3.6$ mm. The spillage process was first observed following the application of $dh =$
306 2.8 mm in case HL (Fig 7), while an additional inland head drop ($dh = 2$ mm) was needed in
307 cases H, LH and HLH (Fig 8). In other words, the spillage of saline water occurred following
308 the application of a hydraulic gradient 0.0074 in case HL, and 0.0053 in the other cases.

309 In case HL, the spillage occurred 12 min following the application of $dh = 2.8$ mm, and it
310 took nearly 100 min for the saltwater length to extend up to 21.6 cm from the sea boundary
311 (or 15.4 cm from the left edge of the wall) where it became quasi steady. A significant
312 widening of the transition zone occurred during the spillage in all cases, due to the excessive
313 dispersion and diffusion occurring along the freshwater-saltwater interface. The further
314 decrement of the head difference to $dh = 2$ mm prompted the saline water to extend up to the
315 critical point X_{crit} within 29 min. This observation shows that the ability of the subsurface
316 dam to retain the saltwater intrusion process was significantly weakened in presence of the
317 low permeability at the bottom part of the aquifer.

318 After decreasing the head difference from $dh = 2.8$ mm to $dh = 2$ mm, Fig 8 shows that, at first
319 glance, the inland progression of the saltwater wedge was inhibited in presence of a low K

320 layer in the middle (case HLH) and top part of the aquifer (LH). The spillage process also
321 exhibited different pattern depending on the layer arrangement. In case LH, the saline water
322 almost dripped into the landward side of the wall with an interface exhibiting a slightly curved
323 shape compared to the homogeneous case. In cases LH and HLH, the transition zone was
324 noticeably wider than the homogeneous case with the case HLH exhibiting greatest transition
325 zone and slowest spillage. Nevertheless, the spillage caused substantial widening of the
326 transition zone in all cases even in case H, especially near the location of the dam, caused by
327 the excessive dispersion along the interface. It is very interesting to note in case HLH the
328 substantial reduction of the salt concentration of the residual saline water in the landward side
329 of the wall, probably caused by much stronger dispersion in the lower portion of the aquifer,
330 where the flow is increased due to the middle low K layer.

331 The rate of inland extension of the saline water was quantified in each case in order to assess
332 the difference in time taken to reach the critical point X_{crit} , following the head decrement
333 from $dh = 2.8$ mm to $dh = 2$ mm. The parameter $\Delta X_{adv}(t)$ is introduced to characterise the
334 distance to be travelled by the toe before reaching X_{crit} , such that $\Delta X_{adv}(t) = \text{abs}[X(t) - X_{crit}]/$
335 X_{crit} ; where $X(t)$ is the toe length at time t . We considered that the critical point T_{crit} was
336 reached when $\Delta X_{adv}(t)$ becomes smaller than 1%. The curves of $\Delta X_{adv}(t)$ are shown in Fig 9
337 and the recorded T_{spil} and T_{crit} values are presented in table 4. Note that in case HL the saline
338 water has already intruded deeper into the freshwater zone prior to applying $dh = 2$ mm; it
339 was therefore not deemed necessary to include this case in this analysis.

340 The data show that the inland extension of the saline water was considerably lower in cases
341 LH and HLH compared to the homogeneous scenario (Fig 9). This means that the rate of
342 saline water spillage was much slower in presence of the low permeability layer in the central
343 and top part of the aquifer. This slower intruding rate is clearly manifested by the milder slope
344 observed in case LH and HLH, while a much steeper slope is exhibited in case H, indicating

345 faster intrusion. This is further confirmed by the delayed starting times of spillage T_{spil}
346 observed in the heterogeneous cases compared to the homogeneous setting, as well as the
347 recorded values of T_{crit} , which are nearly twice in case LH and three times greater in HLH,
348 compared to the homogeneous scenario.

349 Comparison between the numerical data and the experimental results for the advancing-wedge
350 phase is shown in Fig 10. The simulation results yielded very good agreement with the
351 experimental data in all cases. The numerical model confirms the ability of the dam to retain
352 saline water for the all the various inland head previously applied to the bases cases, yielding
353 a reduction of 77%, 76%, 77% and 78% in case H, LH, HLH and HL respectively. The model
354 predicted the spillage of saltwater following the application of $dh = 2.8$ mm in case HL, while
355 no spilling occurred in the other cases until $dh = 2$ mm was applied to the system, in
356 agreement with the experimental observations. The curves show that both the starting time of
357 the spillage and the intruding rate of the saline water are consistent with the experimental data
358 in all cases. The results demonstrate that the ability of subsurface dams to control saline water
359 intrusion mechanism is strongly affected by the existence of stratified layers and the
360 stratification pattern.

361 An analysis of the flow velocity vectors was completed to gain an insight on the impact of
362 each layering pattern on the flow dynamics before the spillage of saline water over the
363 subsurface dam (Fig 11). The model-predicted inflow rate was also recorded in each aquifer
364 setting, as shown in table 5. As expected, the inflow rate was maximal in the homogeneous
365 case and the flow velocity vectors exhibited relatively similar magnitude throughout the
366 system. Obviously, the magnitude of the vectors was very low at the bottom right corner, i.e
367 within the location of the saltwater wedge, and very high at the top right corner of the model
368 domain, i.e. where the freshwater exits the system. The magnitude of the flow velocity vectors
369 was also substantially high at the crest of the subsurface dam, indicating that the freshwater

370 discharge velocity increases over the wall, thereby exerting a downward pressure on the saline
371 plume on the seaward side of the wall, which is in agreement with Luyun et al. (2009).

372 In the layered cases, the results show that there are basically three main processes that
373 influence the saltwater intrusion mechanism which depend essentially on the location of the
374 low permeability zone in the system. The first process, occurring in case LH, is the
375 downwards channelling of the freshwater flow between the crest of the wall and the interlayer
376 boundary. Hence, the freshwater flow increases in the reduced cross section, which result in
377 more “pushing” effects exerted on the saltwater plume, thereby leading to a more effective
378 resistance to the buoyancy forces which drive the intrusion of saline water. This is clearly
379 shown in Fig 11, where the flow velocity vectors of highest magnitude were all located
380 between the crest and the layer boundary, resulting in a visibly smaller saline plume and a
381 rather curvier interface, in agreement with the experimental observations (Fig 6). In other
382 words, the ability of the subsurface dam to resist SWI mechanism increased compared to the
383 homogeneous case, despite the recorded inflow rate was decreased by 32% in this setting
384 relative to the homogeneous scenario. It is also interesting to note that the inflow rate was
385 smaller than in case HL, which suggests that the flow magnitude at the crest of the wall has
386 greater influence on the ability of subsurface dams to control SWI than overall freshwater
387 inflow rate.

388 The second process, taking place in case HLH, is the weakening of the density contrast effects
389 induced by intense mixing occurring as the seaward saline plume is forced to rise through low
390 permeability material. The considerably lower solute concentration of the intruded saline
391 water observed in case HLH at $t = 50$ min tends to support this explanation (Fig 8). Hence,
392 this process directly reduces the buoyancy forces and therefore helps the subsurface dam to
393 withstand the SWI mechanism, despite the magnitude of the flow velocity at the crest as well
394 as the inflow rate were both smaller than the homogeneous case.

395 The third process, occurring in case HL, is the subsequent slowdown of the freshwater flow in
396 the lower part of the system leading to the lowering of the freshwater flow at the crest of the
397 wall. This is clearly observable in Fig 11, where the red zone at the crest of the wall is much
398 smaller than the homogeneous case. In other words, the flow at the crest exerts lesser
399 resistance to the buoyancy forces driving the intrusion compared to the homogeneous case.
400 This means that in such condition, the building up of the saline plume on the seaward side of
401 the wall is facilitated. This process therefore causes the weakening of the ability of the
402 subsurface dam to restrict the saline water intrusion mechanism, and induce easier saltwater
403 spillage compared to a homogeneous scenario, following even lesser drop of the inland head
404 boundary.

405 **Receding-wedge phase**

406 The receding-wedge phase was initiated by instantaneously raising the freshwater level such
407 that to increase the head difference from $dh = 2$ mm to the initial value $dh = 6$ mm. This
408 subsequently caused a sharp increase of the freshwater flow throughout the system that
409 abruptly repulsed the saline water towards the seaside (Fig 12). The receding process was
410 associated with a significant widening of the transition-zone due to the sharp increase of the
411 freshwater flow that transported saline flux along the freshwater-saltwater interface,
412 especially in case HLH, where the lifted saline water passed through the lower permeability
413 media. The removal of the saline water was not completed within 50 min in none of the
414 investigated cases. Rather, the residual saltwater became relatively steady towards the end of
415 the test period, forming a smaller residual wedge on the landward side of the wall. At $t = 50$
416 min, the lengths of the residual wedge measured from landward edge of the wall were 5.4 cm,
417 5.2 cm, 5.1 cm and 7 cm in case H, LH, HLH and HL, respectively.

418 The migration rate of the receding wedge was analysed in all the cases and the results are
419 presented in Fig 13. The parameter $\Delta X_{\text{rec}}(t)$ was used to characterise the distance to be
420 travelled by the toe until its position when the receding motion saltwater plume became
421 steady forming a residual wedge on the landward side of the wall, i.e. at $t = 50$ min, such that
422 $\Delta X_{\text{rec}}(t) = \text{abs}[X(t) - X_f] / X(t_0)$; where $X(t_0)$ and X_f are the toe lengths at $t = 0$ min and $t =$
423 50 min, respectively. The small discrepancies at the initial condition ($t = 0$ min) are simply
424 due to the minor differences of $X(t_0)$ upon the application of the inland head change. The data
425 show that the migrating saline water was much slower in case HL, while relatively similar in
426 the other cases. This was expected because the bottom low K layer slows the transit of the
427 freshwater flow in the lower part of the system, thereby preventing the effective upward
428 lifting of saline water.

429 The complete cleanup of the freshwater zone required extending the test retreat time beyond
430 50 min. The freshwater zone was considered cleaned up when no saline water could be
431 observable, even of low concentration. The time required for the saline water to be completely
432 flushed from the freshwater zone T_{flush} was recorded in each aquifer setting (table 6). The
433 presence of stratified layers generally prolonged the time needed for the residual saline water
434 to be flushed out. Unexpectedly, the time for complete saltwater removal in case LH was
435 longer than the homogeneous scenario (15% longer).

436 This rather counter intuitive finding may be the result of two opposed influential factors
437 associated with the presence of an overlying low K layer. The first is the downwards
438 channelling of the freshwater flow by the upper low K layer, which increases the flow
439 velocity in the lower part of the system and thus promotes the easier lifting of saline water.
440 The second factor is the reduction of the total freshwater inflow, which leads to a reduction of
441 the forces required to lift the denser saline water upward back over the wall. As a result, the
442 time needed for complete flushing of the saltwater is longer. Our results therefore suggest that

443 the second factor has more impact on the ability of the subsurface dam to clean up the
444 freshwater area from SWI contamination. This is clearly shown in table 7, which shows the
445 influence of the top low K layer thickness W_{top} on the cleanup time. The data show that T_{flush}
446 initially decreased with increasing values of W_{top} (for $\leq 20\%$), mainly under the influence of
447 the first process described above. For values of $W_{top} \geq 20\%$, the increasing values of W_{top} ,
448 which obviously caused further reduction of the total freshwater inflow, led to increasing
449 values of T_{flush} , thus mainly under the influence of the second process.

450 In case HL, the presence of the underlying low K layer induced a substantial delay in the
451 flushing time of the saline water, as expected. It took nearly 50% more time for the residual
452 saline water to be removed than the homogeneous setting. As explained above, this is because
453 the underlying low K layer in this setting slows the freshwater flow that faces the residual
454 saltwater wedge thus inhibits the effective upward lifting of saline flux. It is obvious that if
455 the thickness of the low K layer was increased, the flushing time would be considerably
456 increased, as this would not only cause a decrease in the total freshwater inflow, but it would
457 also induce a greater zone where the flow velocity would be considerably lower. In case HLH,
458 the freshwater flow at the crest is reduced by the middle layer low K layer, which partly
459 compromises the landward-seaward transfer of saline flux above the wall. This can be seen in
460 Fig 12, where the transition zone above the crest of the wall is noticeably wider and the
461 wedge is more refracted relative to the homogeneous case. The impact of the low K layer is
462 nonetheless much lessened than in case HL, since in case HLH the freshwater is allowed to
463 flow freely along the aquifer bottom, where it is needed to initiate the lifting process.

464 The results show that the receding rate of saline water in the numerical model yielded very
465 good agreement with the experimental data in all the cases (Fig 14). The time required for
466 complete removal of saline water from the landward side of the wall was also reported in
467 table 6. The data show that it took relatively less time for the freshwater zone to be

468 completely cleaned up in the numerical model for all the cases. The numerical results
469 nonetheless confirm the negative impact the stratified layers has in prolonging the time
470 needed to clean up the freshwater zone, in agreement with the experimental observations.
471 These findings imply that the in cases of equivalent water table rise, the time required for the
472 residual saline water to be completely removed from a coastal aquifer system would be
473 substantially longer in presence of low permeability layers into the system, compared to an
474 idealized homogeneous aquifer system. In other words, the ability of subsurface dams to clean
475 up coastal aquifer from intruded saline water may be largely overestimated when neglecting
476 aquifer heterogeneity effect through the assumption of idealized homogeneous condition.

477 While Oswald et al. (2002) and Luyun et al. (2009) demonstrated that full removal of saline
478 water by the inland freshwater flow is a plausible phenomenon in homogeneous system, the
479 present findings provide for the first time strong evidence of the plausibility of such a natural
480 cleanup process of contaminated coastal ground waters in strongly heterogeneous aquifer
481 settings, with a rate of removal severely affected by the permeability and arrangement of the
482 layers.

483 **4. Summary and Conclusions**

484 In this study, laboratory experiments and numerical simulations were used to assess the
485 impact of layered heterogeneity on the ability of subsurface dams to control saltwater
486 intrusion and to clean-up salinized coastal aquifers. Three layering configurations were
487 examined, where a low K layer was located in the top part of the system (case LH), in the
488 middle part of the aquifer as interlayer (case HLH) and at the bottom part of the system (case
489 HL). An idealized homogeneous aquifer (case H) was also examined for reference purposes.
490 The performance of subsurface dams was tested for their ability (1) to restrict the saline water
491 intrusion mechanism during the advancing-wedge phase, and (2) to clean up the freshwater

492 zone from residual saline water in the receding-wedge phase. The main findings of this
493 investigation are:

494 • The existence of a low permeability zone in the upper part of an aquifer system generally
495 enhanced the ability of subsurface dams to restrict SWI mechanism and lower the rate of
496 saltwater spillage when it occurs, compared to the homogeneous setting. The overlying low
497 K layer forces the freshwater to flow in the reduced spacing between the crest of the wall
498 and the bottom boundary of this low K layer, which pushes the saltwater wedge downwards
499 and impedes its building up. The results showed that the time taken for the aquifer to be
500 contaminated was nearly twice longer than in the homogeneous case.

501 • Conversely, the existence of low permeability zone in the lower part of the aquifer
502 substantially weakens the ability of subsurface dams to retain SWI. The underlying low K
503 layer caused magnitude of the flow velocity over the crest of the wall, which allowed an
504 easier building up of saltwater wedge on the seaward side of the wall and caused the saline
505 water to spill over the wall at even larger head difference compared to the homogeneous
506 scenario.

507 • The natural cleanup of SWI-contaminated coastal aquifers was evidenced for the first time
508 in heterogeneous (multi-layered) geological formations. The presence of stratified layers
509 nonetheless prolonged the cleanup time compared to the homogeneous case to various
510 degrees, depending on the stratification pattern.

511 • In presence of a low K layer at the upper part of the system (case LH), the time for complete
512 saltwater removal was longer than the homogeneous scenario (about 15%). This rather
513 counter intuitive finding was because of the overall reduction of the total freshwater inflow
514 into the aquifer associated with the presence of the low K zone, which induced a lessening
515 of the forces required to lift the residual saline upward back towards the coastline.

516 • In case where a low permeability zone underlies the aquifer system (case HL), the time of
517 completion of the cleanup process was at least about 50% longer than in the homogenous
518 scenario. In such setting, the underlying low K zone significantly slows the freshwater flow
519 that faces the wedge and thus inhibits the effective upward lifting of saline flux on the
520 seaward side of the wall.

521 The findings presented here are expected to have significant implications from water
522 resources management prospective. Our results highlight the limitation of considering the
523 common assumption of homogeneous condition when attempting to assess the performance of
524 subsurface dams, which lead to large erroneous estimation of their ability to retain saltwater
525 intrusion mechanism and clean-up previously contaminated coastal aquifers.

526 Our results also suggest that the residual saline water trapped in the landward side of the wall
527 may be naturally removed from the freshwater zone without the need of mechanical removal
528 techniques, despite the existence of such typical heterogeneous structures. The rate of removal
529 would however be strongly dependent on the total groundwater inflow and the layering
530 pattern, particularly the position of the low permeability layers in the aquifer. Other factors
531 such as the dispersion within the aquifer and the density contrast may also considerably
532 influence the cleanup time.

533 Although real world stratified coastal aquifers may exhibit much more complex layering
534 patterns, the findings of the study provide a first insight on the impact of the expected
535 disruption of flow dynamics imposed by typical layered structures on the performance of
536 subsurface dams in controlling SWI.

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