# Measurement of differential cross sections for the production of top quark pairs and of additional jets in lepton + jets events from pp collisions at $\sqrt{s} = 13$ TeV

A. M. Sirunyan *et al.*<sup>\*</sup> (CMS Collaboration)

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Differential and double-differential cross sections for the production of top quark pairs in proton-proton collisions at  $\sqrt{s} = 13$  TeV are measured as a function of kinematic variables of the top quarks and the top quark-antiquark ( $t\bar{t}$ ) system. In addition, kinematic variables and multiplicities of jets associated with the  $t\bar{t}$  production are measured. This analysis is based on data collected by the CMS experiment at the LHC in 2016 corresponding to an integrated luminosity of 35.8 fb<sup>-1</sup>. The measurements are performed in the lepton + jets decay channels with a single muon or electron and jets in the final state. The differential cross sections are presented at the particle level, within a phase space close to the experimental acceptance, and at the parton level in the full phase space. The results are compared to several standard model predictions that use different methods and approximations. The kinematic variables of the top quarks and the  $t\bar{t}$  system are reasonably described in general, though none predict all the measured distributions. In particular, the transverse momentum distribution of the top quarks is more steeply falling than predicted. The kinematic distributions and multiplicities of jets are adequately modeled by certain combinations of next-to-leading-order calculations and parton shower models.

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#### I. INTRODUCTION

Measurements of differential production cross sections of top quark pairs  $(t\bar{t})$  provide important information for testing the standard model and searching for phenomena beyond the standard model. Precise theoretical predictions of these measurements are challenging since higher-order effects of quantum chromodynamics (QCD) and electroweak (EW) corrections [1] are important. Moreover, the generation of  $t\bar{t}$  events requires a realistic modeling of the parton shower (PS). The measured kinematic properties and multiplicities of jets allow for a detailed comparison of different PS models to the data and provide insight into their tuning.

In this paper, differential and double-differential production cross sections as a function of kinematic variables of the top quarks and the  $t\bar{t}$  system are reported. In addition, measurements of multiplicities and kinematic properties of jets in  $t\bar{t}$  events are presented. The measurements are based on proton-proton (*pp*) collision data at a center-of-mass energy of 13 TeV corresponding to an integrated luminosity of 35.8 fb<sup>-1</sup> [2]. The data were recorded by the CMS experiment at the CERN LHC in 2016. Only  $t\bar{t}$  decays into the  $\ell' + \text{jets}$  ( $\ell' = e, \mu$ ) final state are considered, where, after the decay of each top quark into a bottom quark and a *W* boson, one of the *W* bosons decays hadronically and the other one leptonically. Hence, the experimental signature consists of two jets coming from the hadronization of *b* quarks (*b* jets), two jets from a hadronically decaying *W* boson, a transverse momentum imbalance associated with the neutrino from the leptonically decaying *W* boson, and a single isolated muon or electron.

This measurement continues a series of differential  $t\bar{t}$  production cross section measurements in pp collisions at the LHC. Previous measurements of differential cross sections at  $\sqrt{s} = 7$  TeV [3,4] and 8 TeV [5–11] have been performed in various  $t\bar{t}$  decay channels. First measurements at 13 TeV are available [12–14]. Previous studies of multiplicities and kinematic properties of jets in  $t\bar{t}$  events can be found in Refs. [15–17]. With about 15 times more data and an improved understanding of systematic uncertainties, we provide an update and extension to the previous CMS analysis in the  $\ell$  + jets channel at 13 TeV [18].

We measure differential cross sections defined in two ways: at the particle level and the parton level. For the particle-level measurement a proxy of the top quark is defined based on experimentally accessible quantities, such as properties of jets, which are made up of quasistable

<sup>&</sup>lt;sup>\*</sup>Full author list given at the end of the article.

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particles with a mean lifetime greater than 30 ps. These quantities are described by theoretical predictions that require modeling of the PS and hadronization, in addition to the matrix-element calculations. The kinematic requirements on these objects are chosen to closely reproduce the experimental acceptance. Muons and electrons stemming from  $\tau$  lepton decays are not treated separately and can contribute to the particle-level signal. A detailed definition of particle-level objects is given in Sec. III. The particle-level approach has the advantage that it reduces theoretical uncertainties in the experimental results by avoiding theory-based extrapolations from the experimentally accessible portion of the phase space to the full range, and from jets to partons.

For the parton-level measurement top quarks in the  $\ell$  + jets decay channel are defined as signal directly before their decays into a bottom quark and a *W* boson. The  $\tau$  + jets decay channel is not considered here as signal even in cases where the  $\tau$  lepton decays into a muon or electron. No restriction on the phase space is applied for parton-level top quarks. The corrections and extrapolations used in this measurement are based on a next-to-leading-order (NLO) calculation of  $t\bar{t}$  production, combined with a simulation of the PS.

For both particle- and parton-level measurements the  $t\bar{t}$  system is reconstructed at the detector level with a likelihood-based approach using the top quark and W boson mass constraints to identify the corresponding top quark decay products. The differential cross sections are measured at the particle and parton levels as a function of the transverse momentum  $p_{\rm T}$  and the absolute rapidity |y| of the top quarks, separately for the hadronically (labeled  $t_{\rm h}$ ) and leptonically (labeled  $t_{\ell}$ ) decaying W bosons, and the  $p_{\rm T}$ , |y|, and invariant mass M of the  $t\bar{t}$  system. In addition, the differential cross sections at the parton level are determined as a function of the lower- and higher- $p_{\rm T}$  values of the top quarks in an event. Double-differential cross sections for the following combinations of variables are determined at both levels:  $|y(t_h)|$  vs.  $p_T(t_h)$ ,  $M(t\bar{t})$  vs.  $|y(t\bar{t})|$ , and  $p_T(t_h)$  vs.  $M(t\bar{t})$ . At particle level, the differential cross sections as a function of  $p_{\rm T}(t_{\rm h})$ ,  $p_{\rm T}(t\bar{t})$ , and  $M(t\bar{t})$  are measured in bins of jet multiplicity. Using the four jets identified as the  $t\bar{t}$ decay products and the four highest- $p_{\rm T}$  additional jets, the cross sections are determined as a function of the jet  $p_{\rm T}$ and absolute pseudorapidity  $|\eta|$ , the minimal separation  $\Delta R_{i}$  of jets from another jet in the  $t\bar{t}$  system, and the separation  $\Delta R_t$  of jets from the closest top quark. Here  $\Delta R = \sqrt{(\Delta \phi)^2 + (\Delta \eta)^2}$ , where  $\Delta \phi$  and  $\Delta \eta$  are the differences in azimuthal angle (in radians) and pseudorapidity between the directions of the two objects. Finally, we determine the gap fraction, defined as the fraction of events that do not contain jets above a given  $p_{\rm T}$  threshold, and the jet multiplicities for various thresholds of the jet  $p_{\rm T}$ .

This paper is organized as follows: In Sec. II, we provide a description of the signal and background simulations, followed by the definition of the particle-level top quarks in Sec. III. After a short overview of the CMS detector and the particle reconstruction in Sec. IV, we describe the object and event selections in Sec. V. Section VI contains a detailed description of the reconstruction of the  $t\bar{t}$  system. Details on the background estimation and the unfolding are presented in Secs. VII and VIII. After a discussion of systematic uncertainties in Sec. IX, the differential cross sections as a function of observables of the top quark and the  $t\bar{t}$  system are presented in Sec. X. Finally, observables involving jets are discussed in Sec. XII. The results are summarized in Sec. XII.

### **II. SIGNAL AND BACKGROUND MODELING**

The Monte Carlo generator POWHEG [19–22] (v2,hvq) is used to calculate the production of  $t\bar{t}$  events at NLO accuracy in QCD. The renormalization  $\mu_r$  and factorization  $\mu_{\rm f}$  scales are set to the transverse mass  $m_{\rm T} = \sqrt{m_t^2 + p_{\rm T}^2}$  of the top quark, where a top quark mass  $m_t = 172.5$  GeV is used in all simulations. The result is combined with the PS simulations of PYTHIA8 [23,24] (v8.219) using the underlying event tune CUETP8M2T4 [25,26], and of HERWIG++ [27] (v2.7.1) using the tune EE5C [28]. In addition, MADGRAPH 5\_AMC@NLO [29] (v2.2.2) (MG5\_AMC@NLO) is used to produce a simulation of  $t\bar{t}$  events with additional partons. All processes with up to two additional partons are calculated at NLO and combined with the PYTHIA8 PS simulation using the FxFx [30] algorithm. The scales are selected as  $\mu_{\rm r} = \mu_{\rm f} = \frac{1}{2} (m_{\rm T}(t) + m_{\rm T}(\bar{t}))$ . The default parametrization of the parton distribution functions (PDFs) used in all simulations is NNPDF30\_nlo\_as\_0118 [31]. The simulations are normalized to an inclusive  $t\bar{t}$  production cross section of  $832_{-46}^{+40}$  pb [32]. This value is calculated with next-to-NLO (NNLO) accuracy, including the resummation of next-to-next-to-leading-logarithmic soft-gluon terms. Its uncertainty is evaluated by varying the choice of  $\mu_r$  and  $\mu_f$  and by propagating uncertainties in the PDFs.

Distributions that correspond to variations in the PDFs or the scales  $\mu_r$  and  $\mu_f$  are obtained by applying different event weights. These distributions are used for the corresponding uncertainty estimates. For additional uncertainty estimations we use POWHEG+PYTHIA8 simulations with top quark masses of 171.5 and 173.5 GeV, with initial and final PS scales varied up and down by a factor of two, with variations of the underlying event tune, and a simulation with an alternative color-reconnection model.

The main backgrounds are simulated using the same techniques. The MG5\_aMC@NLO generator is used for the simulation of W boson production in association with jets, *t*-channel single top quark production, and Drell–Yan (DY) production in association with jets. The generator POWHEG [33] is used for the simulation of single top quark associated production with a W boson (tW), and PYTHIA8 is used for multijet production. In all cases, the PS and the

hadronization are described by PYTHIA8. The *W* boson and DY backgrounds are normalized to their NNLO cross sections calculated with FEWZ [34] (v3.1). The *t*-channel single top quark production is normalized to the NLO calculation obtained from HATHOR [35] (v2.1). The production of *tW* is normalized to the NLO calculation [36], and the multijet simulation is normalized to the LO calculation obtained with PYTHIA8 [24].

The detector response is simulated using GEANT4 [37]. The simulations include multiple pp interactions per bunch crossing (pileup). The simulated events are weighted, depending on their number of pileup interactions, to reproduce the measured pileup distribution. Finally, the same reconstruction algorithms that are applied to the data are used for the simulated events.

#### **III. PARTICLE-LEVEL TOP QUARK DEFINITION**

The definitions of particle-level objects constructed from quasi-stable simulated particles, obtained from the predictions of  $t\bar{t}$  event generators before any detector simulation, are summarized below. These particle-level objects are further used to define the particle-level top quarks. Detailed studies on particle-level definitions can be found in Ref. [38].

- (i) All simulated muons and electrons are corrected for effects of bremsstrahlung by adding the photon momenta to the momentum of the closest lepton if their separation is  $\Delta R < 0.1$ . All photons are considered for the momentum correction. A corrected lepton is selected if it fulfills the isolation requirement that the  $p_{\rm T}$  sum of all quasi-stable particles, excluding corrected leptons and neutrinos, within  $\Delta R = 0.4$  is less than 35% of the corrected lepton  $p_{\rm T}$ . In addition, we require the lepton to have  $p_{\rm T} > 15$  GeV and  $|\eta| < 2.4$ .
- (ii) Simulated photons with  $p_{\rm T} > 15$  GeV and  $|\eta| < 2.4$  that are not used in the momentum correction of a lepton are considered if their isolation, defined analogously to the lepton isolation, is below 25%.
- (iii) All neutrinos are selected including those stemming from decays of hadrons.
- (iv) Jets are clustered by the anti- $k_{\rm T}$  jet algorithm [39,40] with a distance parameter of 0.4. All quasistable particles with the exception of neutrinos are clustered. Jets with  $p_{\rm T} > 25$  GeV and  $|\eta| < 2.4$  are selected if there is no isolated lepton or photon, as defined above, within  $\Delta R = 0.4$ .
- (v) b jets at the particle level are defined as those jets that contain a b hadron. As a result of the short lifetime of b hadrons, these are not quasistable particles and only their decay products should be considered for the jet clustering. However, to allow their association with a jet, the b hadrons are also included with their momenta scaled down to a negligible value. This preserves the information of

their directions, but removes their impact on the jet clustering.

Based on the invariant masses of these objects, we construct a pair of particle-level top quarks in the  $\ell$  + jets final state. Events with exactly one muon or electron with  $p_{\rm T} > 30$  GeV and  $|\eta| < 2.4$  are selected. Simulated events with an additional muon or electron with  $p_{\rm T} > 15$  GeV and  $|\eta| < 2.4$  are rejected. We take the sum of the four-momenta of all neutrinos as the neutrino candidate momentum  $p_{\nu}$  from the leptonically decaying top quark and find the permutation of jets that minimizes the quantity

$$\begin{split} & [M(p_{\nu} + p_{\ell'} + p_{b_{\ell'}}) - m_t]^2 + [M(p_{j_{W1}} + p_{j_{W2}}) - m_W]^2 \\ & + [M(p_{j_{W1}} + p_{j_{W2}} + p_{b_h}) - m_t]^2, \end{split} \tag{1}$$

where  $p_{j_{W1,2}}$  are the four-momenta of two light-flavor jet candidates, considered as the decay products of the hadronically decaying *W* boson;  $p_{b_{\ell,h}}$  are the four-momenta of two *b* jet candidates;  $p_{\ell}$  is the four-momentum of the lepton; and  $m_W = 80.4$  GeV [41] is the mass of the *W* boson. All jets with  $p_T > 25$  GeV and  $|\eta| < 2.4$  are considered. At least four jets are required, of which at least two must be *b* jets. The remaining jets with  $p_T >$ 30 GeV and  $|\eta| < 2.4$  are defined as additional jets.

Events with a hadronically and a leptonically decaying particle-level top quark are not required to be  $\ell$  + jets events at the parton level, e.g.,  $t\bar{t}$  dilepton events with additional jets can be identified as  $\ell$  + jets event at the particle level if one lepton fails to pass the selection. As an example, the comparison between the  $p_{\rm T}(t_{\rm h})$  distributions at the particle and parton levels are shown in Fig. 1 and demonstrates the direct relation between particle-level and parton-level top quarks.

To obtain an unambiguous nomenclature for the jets, we define  $j_{W1}$  to be the jet in the W boson decay with the higher  $p_{T}$ . The additional jets  $j_i$  are sorted by their transverse momenta where  $j_1$  has the highest  $p_{T}$ .

### **IV. THE CMS DETECTOR**

The central feature of the CMS detector is a superconducting solenoid of 6 m internal diameter, providing a magnetic field of 3.8 T. Within the solenoid volume are a silicon pixel and strip tracker, a lead tungstate crystal electromagnetic calorimeter (ECAL), and a brass and scintillator hadron calorimeter (HCAL), each composed of a barrel and two endcap sections. Forward calorimeters extend the  $\eta$  coverage provided by the barrel and endcap detectors. Muons are measured in gas-ionization detectors embedded in the steel flux-return yoke outside the solenoid. A more detailed description of the CMS detector, together with a definition of the coordinate system and relevant kinematic variables, can be found in Ref. [42].

The particle-flow (PF) event algorithm [43] reconstructs and identifies each individual particle with an optimized



FIG. 1. Comparison between the  $p_{\rm T}(t_{\rm h})$  distributions at the particle and parton level, extracted from the POWHEG+PYTHIA8 simulation. Left: fraction of parton-level top quarks in the same  $p_{\rm T}$  bin at the particle level (purity), fraction of particle-level top quarks in the same  $p_{\rm T}$  bin at the parton level (stability), ratio of the number of particle- to parton-level top quarks (bin efficiency), and fraction of events with a particle-level top quark pair that are not considered as signal events at the parton level (non-parton-level signal). Right:  $p_{\rm T}$  -bin migrations between particle and parton level. The  $p_{\rm T}$  range of the bins can be taken from the left panel. Each column is normalized such that the sum of its entries corresponds to the fraction of particle-level events in this bin at the parton level in the full phase space.

combination of information from the various elements of the CMS detector. The energy of muons is obtained from the curvature of the corresponding track. The energy of electrons is determined from a combination of the electron momentum at the primary interaction vertex as determined by the tracker, the energy of the corresponding ECAL cluster, and the energy sum of all bremsstrahlung photons spatially compatible with originating from the electron track. The energy of photons is directly obtained from the ECAL measurement, corrected for zero-suppression effects. The energy of charged hadrons is determined from a combination of their momentum measured in the tracker and the matching ECAL and HCAL energy deposits, corrected for zero-suppression effects and for the response function of the calorimeters to hadronic showers. Finally, the energy of neutral hadrons is obtained from the corresponding corrected ECAL and HCAL energy.

### V. PHYSICS OBJECT RECONSTRUCTION AND EVENT SELECTION

The measurements presented in this paper depend on the reconstruction and identification of muons, electrons, jets, and missing transverse momentum associated with a neutrino. Muons and electrons are selected if they are compatible with originating from the primary vertex, which, among the reconstructed primary vertices, is the one with the largest value of summed physics-object  $p_T^2$ . The physics objects are jets, clustered using the jet finding algorithm [39,40] with the tracks assigned to the primary vertex as inputs, and the associated missing transverse momentum, taken as the negative vector sum of the  $\vec{p}_T$  of those jets.

Since leptons from  $t\bar{t}$  decays are typically isolated, a requirement on the lepton isolation is used to reject leptons produced in decays of hadrons. The lepton isolation variables are defined as the sum of the  $p_{\rm T}$  of neutral hadrons, charged hadrons, and photon PF candidates within a cone of  $\Delta R = 0.4$  for muons and  $\Delta R = 0.3$  for electrons. It is required to be less than 15% (6%) of the muon (electron)  $p_{\rm T}$ . Event-by-event corrections are applied to maintain a pileup-independent isolation efficiency. The muon and electron reconstruction and selection efficiencies are measured in the data using tag-and-probe techniques [44–46]. Depending on the  $p_{\rm T}$  and  $\eta$ , their product is 75–85% for muons and 50–80% for electrons.

Jets are clustered from PF objects using the anti- $k_{\rm T}$  jet algorithm with a distance parameter of 0.4 implemented in the FASTJET package [40]. Charged particles originating from a pileup interaction vertex are excluded. The total energy of the jets is corrected for energy depositions from pileup. In addition,  $p_{\rm T}$ - and  $\eta$ -dependent corrections are applied to correct for the detector response effects [47]. If an isolated lepton with  $p_{\rm T} > 15$  GeV within  $\Delta R = 0.4$ around a jet exists, the jet is assumed to represent the isolated lepton and is removed from further consideration.

For the identification of b jets, the combined secondary vertex algorithm [48] is used. It provides a discriminant between b and non-b jets based on the combined information of secondary vertices and the impact parameter of tracks at the primary vertex. A jet is identified as a b jet if the associated value of the discriminant exceeds a threshold criterion with an efficiency of about 63% and a combined charm and light-flavor jet rejection probability of 97%.

The missing transverse momentum  $\vec{p}_{T}^{\text{miss}}$  is calculated as the negative of the vectorial sum of transverse momenta of all PF candidates in the event. Jet energy corrections are also propagated to improve the measurement of  $\vec{p}_{T}^{\text{miss}}$ . Events considered for this analysis are selected by single-lepton triggers. These require  $p_{\rm T} > 24$  GeV for muons and  $p_{\rm T} > 27$  GeV for electrons, as well as various quality and isolation criteria.

To reduce the background contributions and optimize the  $t\bar{t}$  reconstruction, additional requirements are imposed on the recorded events. Events with exactly one muon or electron with  $p_{\rm T} > 30$  GeV and  $|\eta| < 2.4$  are selected. No additional muons or electrons with  $p_{\rm T} > 15$  GeV and  $|\eta| < 2.4$  are allowed. In addition to the lepton, at least four jets with  $p_{\rm T} > 30$  GeV and  $|\eta| < 2.4$  are required. At least two of these jets must be identified as *b* jets.

We compare several kinematic distributions in the data to the simulation separately for the muon and electron channels to verify that there are no unexpected differences. The ratios of the measured to the expected event yields in the two channels agree within the uncertainty in the lepton reconstruction and selection efficiencies. In the remaining steps of the analysis, the two channels are combined by adding their distributions.

### VI. RECONSTRUCTION OF THE TOP QUARK-ANTIQUARK SYSTEM

The reconstruction of the  $t\bar{t}$  system follows closely the methods used in Ref. [18]. The goal is the correct identification of detector-level objects as parton- or particle-level top quark decay products. In the simulation, a jet or lepton at the particle level can be spatially matched to the corresponding detector-level object. If no one-to-one assignment to a corresponding detector-level object is possible for any of the objects in the particle-level  $t\bar{t}$ system, the event is considered as "nonreconstructable" in the particle-level measurement. For the parton-level measurement a quark from the  $t\bar{t}$  decay is assigned to the detector-level jet with the highest  $p_{\rm T}$  within  $\Delta R = 0.4$ around the parton. If no one-to-one correspondence at detector level is found for any of these quarks or the leptons, the event is "nonreconstructable" in the partonlevel measurement. In particular, this includes events with merged topologies where at least two quarks are matched to the same jet. Based on these relations between detector level and parton or particle level, the efficiencies of the  $t\bar{t}$ reconstruction are studied. A detailed discussion on the relationship between quantities at the parton or particle level and detector level is presented in Sec. VIII.

For the reconstruction all possible permutations of assigning detector-level jets to the corresponding  $t\bar{t}$  decay products are tested and a likelihood that a certain permutation is correct is evaluated. Permutations are considered only if the two jets with the highest *b* identification probabilities are the two *b* jet candidates. In each event, the permutation with the highest likelihood is selected. The likelihoods are evaluated separately for the particle- and the parton-level measurements.

For each tested permutation the neutrino four-momentum  $p_{\nu}$  is reconstructed using the algorithm of Ref. [49]. The idea is to find all possible solutions for the three components of the neutrino momentum vector using the two mass constraints  $(p_{\nu} + p_{\ell})^2 = m_W^2$  and  $(p_{\nu} + p_{\ell} + p_{b_{\ell}})^2 = m_t^2$ . Each equation describes an ellipsoid in the threedimensional momentum space of the neutrino. The intersection of these two ellipsoids is usually an ellipse. We select  $p_{\nu}$  as the point on the ellipse for which the distance  $D_{\nu,\min}$  between the ellipse projection onto the transverse plane and  $\vec{p}_{T}^{\text{miss}}$  is minimal. This algorithm leads to a unique solution for the longitudinal neutrino momentum and an improved resolution of its transverse component. For the cases where the invariant mass of the lepton and  $b_{\ell}$  candidate is above  $m_t$  no solution can be found and the corresponding permutation is discarded. The minimum distance  $D_{\nu,\min}$  is also used to identify the correct  $b_{\ell}$ , as described below.

The value of  $D_{\nu,\min}$  from the neutrino reconstruction and the mass constraints on the hadronically decaying top quark are combined in a likelihood function  $\lambda$ , given by

$$-\log[\lambda] = -\log[P_{\rm m}(m_2, m_3)] - \log[P_{\nu}(D_{\nu, \rm min})], \quad (2)$$

where  $P_{\rm m}$  is the two-dimensional probability density of the invariant masses of W bosons and top quarks that are correctly reconstructed, based on the matching criteria described above. The value of  $\lambda$  is maximized to select the permutation of jets. The probability density  $P_{\rm m}$  is calculated as a function of the invariant mass of the two jets,  $m_2$ , tested as the W boson decay products, and the invariant mass of the three jets,  $m_3$ , tested as the decay products of the hadronically decaying top quark. The distributions for the correct jet assignments, taken from the POWHEG+PYTHIA8 simulation and normalized to unit area, are shown in Fig. 2 (upper) for the particle- and parton-level measurements. This part of the likelihood function is sensitive to the correct reconstruction of the hadronically decaying top quark. Permutations with probabilities less than 0.1% of the maximum value of the probability density  $P_{\rm m}$  are rejected. This selection criterion discards less than 1% of the correctly reconstructed events. Especially in the parton-level measurement, it removes events that are incompatible with the hypothesis of a hadronically decaying top quark and reduces the background contribution. This is caused by the stringent mass constraints for a parton-level top quark, where, in contrast to the particle-level top quark, close compatibility with the top quark and W boson masses are required.

The probability density  $P_{\nu}$  describes the distribution of  $D_{\nu,\min}$  for a correctly selected  $b_{\ell}$ . In Fig. 2 (lower), the normalized distributions of  $D_{\nu,\min}$  for  $b_{\ell}$  and for other jets are shown. On average, the distance  $D_{\nu,\min}$  for a correctly selected  $b_{\ell}$  is smaller and has a smaller tail compared to the distance obtained for other jets. Permutations with values of



FIG. 2. Upper: normalized two-dimensional mass distribution of the correctly reconstructed hadronically decaying W bosons M(W) and the correctly reconstructed top quarks  $M(t_h)$  for the (left) parton- and the (right) particle-level measurements. Lower: normalized distributions of the distance  $D_{\nu,\min}$  for correctly and incorrectly selected b jets from the leptonically decaying top quarks. The distributions are taken from the POWHEG+PYTHIA8  $t\bar{t}$  simulation.

 $D_{\nu,\min} > 150$  GeV are rejected since they are very unlikely to originate from a correct  $b_{\ell}$  association. This part of the likelihood function is sensitive to the correct reconstruction of the leptonically decaying top quark. Since the likelihood function  $\lambda$  combines the probabilities from the reconstruction of the leptonically and hadronically decaying top quarks, it provides information on the reconstruction of the whole  $t\bar{t}$  system. The



FIG. 3. Reconstruction efficiency of the  $t\bar{t}$  system as a function of the number of additional jets for the (left) parton- and (right) particle-level measurements. The efficiencies are calculated based on the simulations with POWHEG+PYTHIA8 (P8) with scale variations up and down of the final-state PS, POWHEG+HERWIG++ (H++), and MG5\_aMC@NLO+PYTHIA8. The vertical bars represent the statistical uncertainties in each simulation.



FIG. 4. Distribution of the negative log-likelihood for the selected best permutation in the (left) parton- and the (right) particle-level measurements in data and simulations. Events generated with POWHEG+PYTHIA8 are used to describe the  $t\bar{t}$  production. The contribution of multijet, DY, and W boson plus jets background events is extracted from the data (cf. Sec. VII). Combined experimental (cf. Sec. IX) and statistical uncertainties (hatched area) are shown for the total predicted yields. The data points are shown with statistical uncertainties. The ratios of data to the sum of the predicted yields are provided at the bottom of each panel.

performance of the reconstruction as a function of jet multiplicity is shown for several  $t\bar{t}$  simulations in Fig. 3, where we use the input distributions  $P_{\rm m}$  and  $P_{\nu}$  from the POWHEG+PYTHIA8 simulation. The reconstruction efficiency of the algorithm is defined as the probability that the most-likely permutation, as identified through the maximization of the likelihood  $\lambda$ , is the correct one, given that all  $t\bar{t}$  decay products are reconstructed and selected. The performance deteriorates with the increase in the number of jets, since the number of permutations increases drastically and the probability of selecting a wrong permutation increases. The differences observed between the various simulations are taken into account in the estimation of the systematic uncertainties. We observe a lower reconstruction efficiency for the particle-level measurement. This is caused by the less powerful mass constraints for a particle-level top quark. This can be seen in the mass distributions of Fig. 2 and the likelihood distributions in Fig. 4, where the simulations are normalized to the measured integrated luminosity of the data sample, and the  $t\bar{t}$  simulation is divided into the following categories: correctly reconstructed  $t\bar{t}$  systems ( $t\bar{t}$  right reco); events where all decay products are available, but the algorithm failed to identify the correct permutation ( $t\bar{t}$  wrong reco); the nonreconstructable events ( $t\bar{t}$  nonreconstructable); and events that are according to the parton- or particle-level definitions not  $t\bar{t}$  signal events ( $t\bar{t}$  nonsignal). Only the last category is treated as  $t\bar{t}$  background, while the other categories are considered as signal. The lower reconstruction efficiency of the particle-level top quark is compensated by the higher number of reconstructable events.

In Fig. 5, the  $p_{\rm T}$  of the jets from the  $t\bar{t}$  system, as identified by the reconstruction algorithm, and of the additional jets are presented and compared to the simulation. In Fig. 6, the distributions of  $p_{\rm T}$  and |y| of the

reconstructed top quarks, and in Fig. 7, the distributions of  $p_{\rm T}(t\bar{t})$ ,  $|y(t\bar{t})|$ , and  $M(t\bar{t})$  for the parton- and particle-level measurements are shown. The simulations are normalized according to the measured integrated luminosity of the data. In general, good agreement is observed between the data and the simulation, although all measured  $p_{\rm T}$  spectra are softer than predicted by the simulation.

### **VII. BACKGROUND SUBTRACTION**

After the event selection and  $t\bar{t}$  reconstruction, we observe about 450 000 and 570 000 events at the parton and particle levels, respectively, where total background contributions of 4.5 and 6.0% from single top quark, DY, *W* boson, and multijet events are predicted. These backgrounds have to be estimated and subtracted from the selected data. In addition, a residual contamination from nonsignal  $t\bar{t}$  events is expected and estimated from the simulation, as detailed below.

The predictions of the single top quark background are taken from simulations. Its overall contribution corresponds to about 2.7 and 3.3% of the selected data in the parton- and particle-level measurements, respectively.

Single top quark production cross sections are calculated with a precision of a few percent [35,36]. However, these calculations do not consider the production of additional jets as required by the  $t\bar{t}$  selection. Therefore, we use an overall uncertainty of 50%, which represents a conservative estimate of the PS modeling, scale, and PDF uncertainties. Even with such a conservative estimate, its impact on the precision of the final results is negligible.

After the full  $t\bar{t}$  selection, the numbers of events in the simulations of multijet, DY, and W boson production are not sufficient to obtain smooth background distributions. Therefore, we extract a common distribution for these



FIG. 5. Comparisons between data and simulation at the particle level of the reconstructed distributions of the  $p_T$  of jets as identified by the  $t\bar{t}$  reconstruction algorithm. The simulation of POWHEG+PYTHIA8 is used to describe the  $t\bar{t}$  production. The contribution of multijet, DY, and W boson plus jets background events is extracted from the data (cf. Sec. VII). Combined experimental (cf. Sec. IX) and statistical uncertainties (hatched area) are shown for the total predicted yields. The data points are shown with statistical uncertainties. The ratios of data to the predicted yields are given at the bottom of each panel.



FIG. 6. Comparisons of the reconstructed  $p_T$  (upper) and |y| (lower) in data and simulations for the  $t_\ell$  (left) at the parton level and the  $t_h$  (right) at the particle level. The simulation of POWHEG+PYTHIA8 is used to describe the  $t\bar{t}$  production. The contribution of multijet, DY, and W boson plus jets background events is extracted from the data (cf. Sec. VII). Combined experimental (cf. Sec. IX) and statistical uncertainties (hatched area) are shown for the total predicted yields. The data points are shown with statistical uncertainties. The ratios of data to the predicted yields are given at the bottom of each panel.

backgrounds from a control region in the data. Its selection differs from the signal selection by the requirement of having no b-tagged jet in the event. In this control region, the contribution of  $t\bar{t}$  events is estimated to be about 15%, while the remaining fraction consists of multijet, DY, and W boson events. The background distributions are obtained after applying exactly the same  $t\bar{t}$  reconstruction algorithm as in the signal region. The two b jet candidates still have the highest value of the *b* identification discriminant to maintain a similar number of allowed permutations of jets in the control and signal regions. To estimate the shape dependency on the selection of the control region, we vary the selection threshold of the b identification discriminant. This changes the  $t\bar{t}$  signal contribution and the flavor composition. However, we find the observed shape variations to be small. In addition, we verify in the simulation that the shapes of the distributions obtained from the control region are compatible with the background distributions in the signal region. For the background subtraction the distributions extracted from the control region are normalized individually in each bin of jet multiplicity to the yield of multijet, DY, and W boson events predicted by the simulation in the signal region. In the control region, the expected and measured event yields agree within their statistical uncertainties. Taking into account the statistical uncertainty in the normalization factor and the shape differences between the signal and control regions in the simulation, we derive an overall uncertainty of 20% in this background estimation.

Special care has to be taken with the contribution of nonsignal  $t\bar{t}$  events. For the parton-level measurement these are dilepton, all-jets, and  $\tau$  + jets events. For the particle-level measurement all  $t\bar{t}$  events for which no pair of particle-level top quarks exists are considered as nonsignal  $t\bar{t}$  events. The corresponding contributions are about 11.5% for both the parton- and the particle-level measurements. The behavior of these backgrounds depends on the  $t\bar{t}$  cross section, and a subtraction according to the expected value can result in a bias of the measurement, especially if large differences between the simulation and the data are observed. However, the shapes of the distributions from data and simulation are consistent within their uncertainties, and we subtract the predicted relative fractions from the remaining event yields.



FIG. 7. Comparisons of the reconstructed distributions of  $p_T(t\bar{t})$  (upper),  $|y(t\bar{t})|$  (middle), and  $M(t\bar{t})$  (lower) for the (left) parton- and the (right) particle-level measurements in data and simulation. The simulation of POWHEG+PYTHIA8 is used to describe the  $t\bar{t}$  production. The contribution of multijet, DY, and W boson plus jets background events is extracted from the data (cf. Sec. VII). Combined experimental (cf. Sec. IX) and statistical uncertainties (hatched area) are shown for the total predicted yields. The data points are shown with statistical uncertainties. The ratios of data to the predicted yields are given at the bottom of each panel.

# VIII. CORRECTIONS TO PARTICLE AND PARTON LEVELS

After the subtraction of the backgrounds, an unfolding procedure is used to correct the reconstructed distributions for detector-specific effects, e.g., efficiency and resolutions, and to extrapolate either to the parton or particle level. We do not subtract the fractions of wrongly reconstructed or nonreconstructable events, since in many of these events a rather soft jet is misidentified, which has little impact on the resolution of the measured quantities. The iterative D'Agostini method [50] is used to unfold the data. The migration matrices, which relate the quantities at the parton or particle level and at detector level, and the acceptances are needed as the input. However, not only the detector simulation, but also the theoretical description of  $t\bar{t}$  events affects the migration matrix. This dependence is reduced in the particle-level measurement, where no extrapolation to parton-level top quarks is needed. For the central results the migration matrices and the acceptances are taken from the POWHEG+PYTHIA8 simulation, and other simulations are used to estimate the uncertainties. The binning of the distributions is optimized based on the resolution in the simulation. The minimal bin widths are selected such that, according to the resolution, at least 50% of the events are reconstructed in the correct bin. As an example, the migration matrices for the parton- and particle-level measurements of  $p_{\rm T}(t_{\rm h})$  are shown in the right-hand plots of Fig. 8. For the measured parton-level distributions of any quantity we define the purity as the fraction of parton-level top quarks in the same bin at the detector level, the stability as the fraction of detector-level top quarks in the same bin at the parton level, and the bin efficiency as the ratio of the number of detector- to parton-level top quarks in the same bin. Similar parameters are defined for the particle-level distributions. The purity, stability, and bin efficiency are shown for the  $p_{\rm T}(t_{\rm h})$  measurements in the left-hand plots of Fig. 8. These illustrate the improved agreement between the reconstructed and the unfolded quantities, as well as the reduced extrapolation in the particle-level measurement.

To control the level of regularization, the iterative D'Agostini method takes the number of iterations as an input parameter. The initial distributions for the D'Agostini unfolding are taken from the POWHEG +PYTHIA8 simulation. The number of iterations is chosen such that the compatibility between a model and the unfolded data at either the parton or particle level is the same as the compatibility between the folded model and the data at detector level. The compatibilities are determined by  $\chi^2$  tests at each level that are based on all the available simulations and on several modified spectra obtained by reweighting the POWHEG+PYTHIA8 distributions of  $p_{\rm T}(t)$ , |y(t)|,  $p_{\rm T}(t\bar{t})$ , or  $p_{\rm T}(j_1)$  before the detector simulation. The modified spectra are chosen such that the effect of the reweighting corresponds roughly to the observed differences between the data and the unmodified simulation at detector level.

We have found that the number of iterations needed to fulfill the above criterion is such that a second  $\chi^2$  test between the detector-level spectrum with its statistical



FIG. 8. Migration studies of the (upper) parton- and (lower) particle-level measurements of  $p_{\rm T}(t_{\rm h})$ , extracted from the POWHEG +PYTHIA8 simulation. Left: purity, stability, and bin efficiency. Right: bin migrations between detector and parton (particle) level. The  $p_{\rm T}$  range of the bins can be taken from the left panels. Each column is normalized such that the sum of its entries corresponds to the percentage of reconstructed events in this bin at the parton (particle) level.



FIG. 9. Migration studies of the particle-level measurement of the jet  $p_T$  spectra, extracted from the POWHEG+PYTHIA8 simulation. Left: purity, stability, and bin efficiency. Right: bin migrations between detector and particle level. On the axes the  $p_T$  bins for each jet are shown. Each column is normalized in the way that the sum of its entries corresponds to the percentage of reconstructed events in this bin at the particle level.

uncertainty and the refolded spectrum with zero uncertainty exceeds a probability of 99.9%. The refolded spectrum is obtained by inverting the unfolding step. This consists of a multiplication with the response matrix and does not need any regularization. The algorithm needs between 4 and 56 iterations depending on the distribution. The numbers of iterations are higher for measurements with lower purities and stabilities of the migration matrices. This is the case for the measurements of  $p_{\rm T}(t_{\ell})$  and  $|y(t_{\ell})|$ , whose resolutions are significant worse than those of  $p_{\rm T}(t_{\rm h})$  and  $|y(t_{\rm h})|$  due to the missing neutrino information.

For the two-dimensional measurements with *n* bins in one quantity and  $m_i$ , i = 1...n bins in the other the D'Agostini unfolding can be generalized using a vector of  $B = \sum_{i=1}^{n} m_i$  entries of the form:  $b_{1,1}, b_{2,1}...b_{n,1}, ...$  $b_{1,m_1}, b_{2,m_2}...b_{n,m_n}$ , with a corresponding  $B \times B$  migration matrix. The number of iterations is optimized in the same way.

In the measurements of jet kinematic properties, we do not unfold the measured spectra of each jet separately, but do correct for the effect of misidentified jets. The response matrix showing the migration among the identified jets is given in Fig. 9 for the measurements of the jet  $p_{\rm T}$  spectra.

# **IX. SYSTEMATIC UNCERTAINTIES**

Several sources of experimental and theoretical systematic uncertainty are considered. Uncertainties in the jet and  $\vec{p}_{T}^{miss}$  calibrations, pileup modeling, *b* identification and lepton selection efficiencies, and integrated luminosity fall into the first category.

The total uncertainty in the jet energy calibration is the combination of 19 different sources of uncertainty and the jet-flavor-specific uncertainties [47], where the uncertainty for b jets is evaluated separately. For each uncertainty source the energies of jets in the simulation are shifted up

and down. At the same time,  $\vec{p}_{T}^{\text{miss}}$  is recalculated accordingly to the rescaled jet energies. The recomputed backgrounds, response matrices, and acceptances are used to unfold the data. The observed differences between these and the original results are taken as an uncertainty in the unfolded event yields. The same technique is used to calculate the impact of the uncertainties in the jet energy resolution, the uncertainty in  $\vec{p}_{T}^{\text{miss}}$  not related to the jet energy calibration, the *b* identification, the pileup modeling, and the lepton reconstruction and selection.

The *b* identification efficiency in the simulation is corrected using scale factors determined from data [51]. These have an uncertainty of about 1–3% depending on the  $p_{\rm T}$  of the *b* jet.

The effect on the measurement due to the uncertainty in the modeling of pileup in simulation is estimated by varying the average number of pileup events per bunch crossing by 4.6% [52] and reweighting the simulated events accordingly.

The trigger, reconstruction, and identification efficiencies of leptons are evaluated with tag-and-probe techniques using Z boson dilepton decays [45,46]. The uncertainties in the scale factors, which are used to correct the simulation to match the data, take into account the different lepton selection efficiencies in events with high jet multiplicities as in  $t\bar{t}$  events. The uncertainty in the lepton reconstruction and selection efficiencies depends on  $p_T$  and  $\eta$  and is below 2% in the relevant phase-space region.

The relative uncertainty in the integrated luminosity measurement is 2.5% [2].

Uncertainties in the choice of  $\mu_r$  and  $\mu_f$ , the combination of the matrix-element calculation with the PS, the modeling of the PS and hadronization, the top quark mass, and the PDFs fall into the second category of uncertainties. The effects of these theoretical uncertainties are estimated either by using the event weights introduced in Sec. II, or by using a  $t\bar{t}$  signal simulation with varied settings. Again, the uncertainties are assessed using the recomputed backgrounds, response matrices, and acceptances to unfold the data.

The scales  $\mu_r$  and  $\mu_f$  are varied up and down by a factor of two individually and simultaneously in the same directions. Afterwards, the envelope of the observed variations is quoted as the uncertainty.

The uncertainty in the combination of the matrixelement calculation with the PS is estimated from an  $\approx 40\%$  variation of the  $h_{damp}$  parameter in POWHEG, normally set to  $h_{damp} = 1.58m_t$ . This variation has been found to be compatible with the modeling of jet multiplicities in previous measurements at  $\sqrt{s} = 8$  TeV [16].

To estimate the uncertainty in the PS, several effects have been studied and are assessed individually. The scale of the initial- (ISR) and final-state (FSR) radiation is varied up and down by a factor of 2 and  $\sqrt{2}$ , respectively. These variations are motivated by the uncertainties in the PS tuning [25]. The effect of multiple parton interactions and the parametrization of color reconnection have been studied in Ref. [26] and are varied accordingly. In addition, we use a simulation with activated color reconnection of resonant decays. This enables the color reconnection of top quark decay products with other partons, which is not allowed in the default tune. The uncertainty in the b fragmentation function is taken from measurements at LEP experiments [53–55] and SLD [56], and the parametrization in PYTHIA8 is changed accordingly. Finally, the semileptonic branching fractions [41] of *b* hadrons are varied within their measured uncertainties.

The effect due to the uncertainty in the top quark mass is estimated using simulations with altered top quark masses. We quote as the uncertainty the cross section differences observed for a top quark mass variation of 1 GeV around the central value of 172.5 GeV used in the default simulation.

For the PDF uncertainty only the variation in the acceptance is taken into account, while variations due to migrations between bins can be neglected. It is calculated according to the uncertainties in the NNPDF30\_nlo\_ as\_0118 [31] parametrization. In addition, the uncertainties obtained using the PDF sets derived with the strong coupling strength set at  $\alpha_s = 0.117$  and 0.119 are considered.



FIG. 10. Relative uncertainties due to the individual sources in the absolute (upper) and normalized (lower) measurement of  $p_T(t_h)$  at the parton level (left) and particle level (right). Sources whose impact never exceeds 1% are summarized in the category "Others." The combination of the individual sources of jet energy uncertainty is labeled "Jet energy." The combined uncertainty is the sum in quadrature of the statistical and all the systematic uncertainties.

As an example, the sources of systematic uncertainty in the measurements of  $p_{\rm T}(t_{\rm h})$ , as well as the statistical and total uncertainty, are shown in Fig. 10. Among the experimental uncertainties, the dominant sources are the jet energy scale; lepton triggering, reconstruction, and identification; and the *b* identification. In the parton-level measurement, the FSR scale is typically an important contribution to the systematic uncertainty.

As an additional consistency test, we subtract the  $t\bar{t}$  background and unfold the data using the reweighted simulations that include all the differences in the measured distributions at detector level described in Sec. VIII. The differences between these unfolded distributions and the

PHYS. REV. D 97, 112003 (2018)

# X. DIFFERENTIAL CROSS SECTIONS AS FUNCTIONS OF OBSERVABLES OF THE TOP QUARK AND THE $\vec{t}$ SYSTEM

compared to the uncertainties evaluated by the variations

described above.

The cross section  $\sigma$  in each bin is calculated as the ratio of the unfolded signal yield and the integrated luminosity. These are further divided by the bin width or the product of the two bin widths to obtain the single- or doubledifferential cross section results, respectively. To allow for a



FIG. 11. Absolute (left) and normalized (right) differential cross sections at the parton level as a function of  $p_T(t_h)$  (upper) and  $p_T(t_{\ell})$  (lower). The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++), the multiparton simulation MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx, and the NNLO QCD + NLO EW calculations. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 12. Absolute (left) and normalized (right) differential cross sections at the parton level as a function of  $|y(t_h)|$  (upper) and  $|y(t_\ell)|$  (lower). The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++), the multiparton simulation MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx, and the NNLO QCD + NLO EW calculations. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.

precise comparison of the measured shapes with theoretical predictions, irrespective of the integrated cross section and its uncertainty, we also present normalized differential cross sections. For this purpose the absolute differential cross sections are divided by the normalizing cross sections  $\sigma_{norm}$ , which are obtained for each measurement from the integration of the cross section over the measured one- or two-dimensional range. The uncertainties in the normalized distributions are evaluated using error propagation and include the correlations between uncertainties in the individual measurements and  $\sigma_{norm}$ . For the statistical uncertainty the covariances are taken directly from the unfolding procedure. For each of the studied systematic uncertainties we assume a full correlation among all bins,

while the various sources are assumed to be uncorrelated. The same assumptions about correlations of uncertainty sources are made for the calculation of the normalized theoretical predictions.

The measured differential cross sections are compared to the predictions of POWHEG, combined with the PS simulations of PYTHIA8 and HERWIG++, and the  $t\bar{t}$  multiparton simulation of MG5\_aMC@NLO+PYTHIA8 FxFx. In addition, several parton-level results are compared to calculations of  $t\bar{t}$  production with NNLO QCD + NLO EW [1] accuracy, where a top quark mass of 173.3 GeV [57] is used. For the calculations of the theoretical cross sections as functions of  $M(t\bar{t})$  and rapidities the scales are set to  $\mu_{\rm r} = \mu_{\rm f} = (1/4)(m_{\rm T}(t) + m_{\rm T}(\bar{t}))$  and the scales for the  $p_{\rm T}$ 



FIG. 13. Absolute (left) and normalized (right) differential cross sections at the particle level as a function of  $p_T(t_h)$  (upper) and  $p_T(t_\ell)$  (lower). The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.

calculations are selected as  $(1/2)m_{\rm T}(t)$  or  $(1/2)m_{\rm T}(\bar{t})$ depending on the variable under consideration. The PDF parametrizations LUXqed\_plus\_PDF4LHC15\_nnlo\_100 [58] are used for these calculations. The uncertainties consider variations of the scales  $\mu_{\rm r}$  and  $\mu_{\rm f}$ . The particlelevel results are compared to a prediction obtained with the Monte Carlo generator SHERPA [59] (v2.2.3) in combination with OPENLOOPS [60]. The processes of  $t\bar{t}$  production with up to one additional parton are calculated at NLO QCD accuracy, and those with up to four additional partons are calculated at LO. These processes are merged and matched with the Catani–Seymour PS [61] based on the SHERPA default tune. For the scales we select

$$\mu_{\rm r} = \mu_{\rm f} = \frac{1}{2} \left( m_{\rm T}(t) + m_{\rm T}(\bar{t}) + \sum_{\rm partons} p_{\rm T} \right), \qquad (3)$$

where the summation over partons includes the  $p_T$  of all partons obtained from the fixed-order calculation. The NNPDF30\_nlo\_as\_0118 [31] PDF parametrizations are used. Uncertainties in the predictions of SHERPA are evaluated by halving and doubling the scales of renormalization, factorization, resummation, and the initial- and final-state PS. In addition, the PDF uncertainties are taken into account. For the predictions of POWHEG+PYTHIA8 we evaluate all the theoretical uncertainties described in Sec. IX. Although the



FIG. 14. Absolute (left) and normalized (right) differential cross sections at the particle level as a function of  $|y(t_h)|$  (upper) and  $|y(t_\ell)|$  (lower). The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.

SHERPA and the POWHEG+PYTHIA8 simulations are normalized to the NNLO  $t\bar{t}$  production cross section, we use their intrinsic scale uncertainties.

The comparisons between the measurements and the theoretical predictions as a function of the top quark  $p_T$  and |y| are shown in Figs. 11–12 and 13–14 for the parton and particle level, respectively. At parton level, the kinematic properties of  $t_h$  and  $t_\ell$  are identical, and we measure the differential cross section as a function of the top quark  $p_T$  using the higher- and lower- $p_T$  values in the  $t\bar{t}$  pair, as shown in Fig. 15. The measured  $p_T$  spectra of  $t_h$  and  $t_\ell$  are consistently softer than predicted by all the simulations using the PYTHIA8 PS generator at both the parton and

particle levels. Also the NNLO QCD + NLO EW calculation predicts a slightly harder  $p_T$  spectrum than observed in the data. The POWHEG+HERWIG++ simulation describes the data well at the parton level. However, at the particle level, the  $p_T(t_h)$  distribution is noticeably softer than in the data. In Figs. 16 and 17, the cross sections as a function of kinematic variables of the  $t\bar{t}$  system are compared to the same theoretical predictions. In general, the predictions are in agreement with the measured distributions. The NNLO QCD + NLO EW calculation predicts a higher-average  $M(t\bar{t})$  spectrum than observed in the data. For POWHEG +HERWIG++ a similar behavior as for the  $p_T(t_h)$  distributions is observed—while the parton-level distribution is



FIG. 15. Absolute (left) and normalized (right) differential cross sections at the parton level as a function of the transverse momentum of the top quark with the higher and lower  $p_{\rm T}$ . The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++), and the multiparton simulation MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.

well described, a softer spectrum is observed at the particle level.

The measurement of double-differential cross sections allows for the study of correlations between kinematic properties of the top quarks and provides insights into extreme regions of the phase space. The most fundamental doubledifferential distribution is that of the top quark properties  $|y(t_h)|$  vs.  $p_T(t_h)$ . The absolute double-differential cross sections are shown in Figs. 18 and 20, and the normalized in Figs. 19 and 21 at the parton and particle levels, respectively. The observation of a softer  $p_T(t)$  spectrum is persistent in all rapidity regions. In Figs. 22–25, the corresponding measurements as a function of  $M(t\bar{t})$  vs.  $|y(t\bar{t})|$  are shown. This distribution is sensitive to the PDFs [11]. As  $M(t\bar{t})$  increases, the simulations overestimate the cross sections at high  $|y(t\bar{t})|$ . Finally, we measure  $p_{\rm T}(t_{\rm h})$  vs.  $M(t\bar{t})$ , as shown in Figs. 26–29. For these distributions the simulations of POWHEG+PYTHIA8, MG5\_AMC@NLO+PYTHIA8 FxFx, and SHERPA predict similar shapes, which differ substantially from the data.

The precision of the differential cross section measurements is limited by the systematic uncertainty, dominated by jet energy scale uncertainties on the experimental side and PS modeling and scale uncertainties on the theoretical side. As expected, the theoretical uncertainties are reduced in the particle-level measurements since they are less dependent on theory-based extrapolations.



FIG. 16. Absolute (left) and normalized (right) differential cross sections at the parton level as a function of  $p_{\rm T}(t\bar{t})$  (upper),  $|y(t\bar{t})|$  (middle), and  $M(t\bar{t})$  (lower). The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++), the multiparton simulation MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx, and the NNLO QCD + NLO EW calculations. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 17. Absolute (left) and normalized (right) differential cross sections at the particle level as a function of  $p_T(t\bar{t})$  (upper),  $|y(t\bar{t})|$  (middle), and  $M(t\bar{t})$  (lower). The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 18. Double-differential cross section at the parton level as a function of  $|y(t_h)|$  vs.  $p_T(t_h)$ . The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++), and the multiparton simulation MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.

We evaluate the level of agreement between the measured differential cross sections and the various theoretical predictions using  $\chi^2$  tests. In these tests, we take into account the full covariance matrices of the measured differential cross sections. For the POWHEG+PYTHIA8 and the SHERPA predictions we consider the theoretical uncertainties and their correlation among the bins. In addition, we perform the  $\chi^2$  tests without any uncertainties in the theoretical models. We do this since the generation of simulated events does not include any of these theoretical uncertainties; the simulated distributions of the various kinematic quantities correspond exactly to the central predictions. Therefore, it is worthwhile to compare how well the central predictions agree with the data, independent of the theoretical uncertainties. From the  $\chi^2$  values and the numbers of degrees of freedom, which correspond to the numbers of bins in the distributions, the *p*-values are calculated. The results are shown in Table I for the parton-level and in Table III for the particle-level absolute measurements. The corresponding  $\chi^2$  tests for the normalized distributions, for which the numbers of degrees of freedom are reduced by 1, are given in Tables II and IV for the parton- and particle-level measurements, respectively.

The  $\chi^2$  tests show that the measurements are largely compatible with the POWHEG+PYTHIA8 and SHERPA predictions if the uncertainties in the simulations are taken into account. Some tension is observed between the data and the



FIG. 19. Normalized double-differential cross section at the parton level as a function of  $|y(t_h)|$  vs.  $p_T(t_h)$ . The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++), and the multiparton simulation MG5\_aMC@NLO (MG5) +PYTHIA8 FxFx. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.

predictions of  $p_{\rm T}(t)$  and related distributions like  $p_{\rm T}(t_{\rm h})$  vs.  $M(t\bar{t})$ . Comparisons of the *p*-values at the parton and particle level obtained for the central predictions, ignoring their theoretical uncertainties, show a similar performance. For all tested models we obtain *p*-values below 1% for at least two distributions. These are typically distributions related to  $p_{\rm T}(t)$  and  $p_{\rm T}(t\bar{t})$ .

### XI. MEASUREMENTS OF MULTIPLICITIES AND KINEMATIC PROPERTIES OF JETS

In the following, we discuss the measurements involving the multiplicities and kinematic properties of jets in  $t\bar{t}$ events. These are performed at the particle level only. In the POWHEG simulations, all jets beyond one additional jet are described by the PS simulation and, hence, their description is subject to PS tuning. In the SHERPA simulation, the production of up to one additional jet is calculated at NLO accuracy, and up to four jets at LO. However, these LO calculations are very sensitive to the choice of the scales. Since in the MG5\_AMC@NLO+PYTHIA8 FxFx simulation up to two additional jets are calculated at NLO, it is expected to be more accurate at high jet multiplicities.

The absolute and normalized differential cross sections as a function of  $p_{\rm T}(t_{\rm h})$ ,  $M(t\bar{t})$ , and  $p_{\rm T}(t\bar{t})$  for different numbers of additional jets are shown in Figs. 30–35. These distributions are helpful to estimate the  $t\bar{t}$  background contribution in searches for physics beyond the standard



FIG. 20. Double-differential cross section at the particle level as a function of  $|y(t_h)|$  vs.  $p_T(t_h)$ . The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.

model that are looking for signatures with high jet multiplicities. The observation that the  $p_{\rm T}(t)$  distribution is softer in data than in the simulations is mainly true for events with zero or one additional jet.

We also measure the properties of the individual jets in  $t\bar{t}$  events. The absolute and normalized differential cross sections as a function of the  $p_{\rm T}$  of jets in the  $t\bar{t}$  system and of the four leading additional jets are shown in Figs. 36 and 37, respectively. The trend of a softer  $p_{\rm T}$  spectrum of

the top quark is also visible for all jets of the  $t\bar{t}$  system. From these  $p_T$  distributions we calculate the jet multiplicities with minimum  $p_T$  thresholds of 30, 50, 75, and 100 GeV shown in Fig. 38, and gap fractions [16,17]. The gap fraction  $f_n(p_T)$  is the fraction of unfolded events that contain less than *n* additional jets above the given  $p_T$ threshold. It is shown for n = 1 and 2 in Fig. 39. In the calculations of jet multiplicities and gap fractions, we take into account the small fraction of jets above the displayed



FIG. 21. Normalized double-differential cross section at the particle level as a function of  $|y(t_h)|$  vs.  $p_T(t_h)$ . The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.

 $p_{\rm T}$  ranges. The uncertainties are obtained by error propagation using the full covariance matrices. The jet multiplicities and gap fractions are reasonably described by most of the simulations. However, the central predictions of SHERPA and POWHEG+HERWIG++ show noticeable deviations in the gap fraction.

In Figs. 40–45, the absolute and normalized distributions of  $|\eta|$ ,  $\Delta R_{j_t}$ , and  $\Delta R_t$  are shown for the jets in the  $t\bar{t}$ system and the additional jets. The differential cross section as a function of  $|\eta|$  is well described by most of the simulations, while POWHEG+HERWIG++ overestimates the radiation of additional jets close to the jets in the  $t\bar{t}$ system. In the predictions, such collinear radiation is mainly described by the PS model. Since the parton-level prediction is not affected by the simulation of the finalstate PS, this overestimation of radiation may explain the discrepancies between the parton- and particle-level predictions of POWHEG+HERWIG++ in the  $p_{\rm T}(t_{\rm h})$  and  $M(t\bar{t})$  distributions.

Table V presents the results of the  $\chi^2$  tests comparing the absolute measurements involving multiplicities and kinematic properties of jets to the simulations. The corresponding results for the normalized measurements are shown in Table VI. Most of the kinematic distributions and multiplicities of the additional jets are reasonably well modeled by POWHEG+PYTHIA8. Inconsistencies with the data are observed for  $p_T$  and  $\eta$  of jets, and  $p_T(t\bar{t})$  for different jet multiplicities. The POWHEG descriptions of



FIG. 22. Double-differential cross section at the parton level as a function of  $M(t\bar{t})$  vs.  $|y(t\bar{t})|$ . The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++), and the multiparton simulation MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.

additional jets rely on phenomenological models of the PS and are substantially different for PYTHIA8 and HERWIG++. With the selected settings SHERPA fails to describe most of the kinematic distributions and multiplicities of the jets. Comparisons of the measurements to the central predictions, ignoring their theoretical uncertainties, show that the *p*-values are typically below 1% for all models. Here the multiparton simulation MG5\_aMC@NLO+PYTHIA8 FxFx performs best.

All cross section values, together with their statistical and systematic uncertainties, are listed in Appendices A and B for the parton- and particle-level measurements, respectively. In addition, the corresponding normalized cross sections are provided in Appendices C and D.



FIG. 23. Normalized double-differential cross section at the parton level as a function of  $M(t\bar{t})$  vs.  $|y(t\bar{t})|$ . The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++), and the multiparton simulation MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 24. Double-differential cross section at the particle level as a function of  $M(t\bar{t})$  vs.  $|y(t\bar{t})|$ . The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 25. Normalized double-differential cross section at the particle level as a function of  $M(t\bar{t})$  vs.  $|y(t\bar{t})|$ . The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5) +PYTHIA8 FxFx and SHERPA. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 26. Double-differential cross section at the parton level as a function of  $p_T(t_h)$  vs.  $M(t\bar{t})$ . The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++), and the multiparton simulation MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 27. Normalized double-differential cross section at the parton level as a function of  $p_T(t_h)$  vs.  $M(t\bar{t})$ . The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++), and the multiparton simulation MG5\_aMC@NLO (MG5) +PYTHIA8 FxFx. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 28. Double-differential cross section at the particle level as a function of  $p_T(t_h)$  vs.  $M(t\bar{t})$ . The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 29. Normalized double-differential cross section at the particle level as a function of  $p_T(t_h)$  vs.  $M(t\bar{t})$ . The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.

TABLE I. Comparison between the measured absolute differential cross sections at the parton level and the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++), the multiparton simulation MG5\_aMC@NLO FxFx, and the NNLO QCD + NLO EW calculations. The compatibility with the POWHEG+PYTHIA8 prediction is also calculated including its theoretical uncertainties (with unc.), while those are not taken into account for the other comparisons. The results of the  $\chi^2$  tests are listed, together with the numbers of degrees of freedom (dof) and the corresponding *p*-values.

Distribution	$\chi^2/dof$	<i>p</i> -value	$\chi^2/dof$	<i>p</i> -value	$\chi^2/dof$	<i>p</i> -value
	POWHEG+P8 with unc.		POWHEG+P8		NNLO QCD + NLO EW	
$p_{\rm T}(t_{\rm high})$	16.4/12	0.173	27.4/12	< 0.01		
$p_{\rm T}(t_{\rm low})$	22.4/12	0.033	42.7/12	< 0.01		
$p_{\rm T}(t_{\rm h})$	16.4/12	0.175	24.0/12	0.020	5.13/12	0.953
$ y(t_{\rm h}) $	1.28/11	1.000	1.41/11	1.000	2.27/11	0.997
$p_{\mathrm{T}}(t_{\ell})$	22.2/12	0.035	38.3/12	< 0.01	9.56/12	0.654
$ y(t_{\ell}) $	2.04/11	0.998	2.42/11	0.996	8.14/11	0.700
$M(t\bar{t})$	7.67/10	0.661	11.6/10	0.314	24.7/10	< 0.01
$p_{\mathrm{T}}(t\bar{t})$	5.38/8	0.717	46.5/8	< 0.01		
$ y(t\bar{t}) $	3.98/10	0.948	5.66/10	0.843	9.26/10	0.507
$ y(t_h) $ vs. $p_T(t_h)$	23.6/44	0.995	41.6/44	0.577		
$M(t\bar{t})$ vs. $ y(t\bar{t}) $	20.6/35	0.975	35.0/35	0.469		
$p_{\rm T}(t_{\rm h})$ vs. $M(t\bar{t})$	38.9/32	0.188	59.3/32	< 0.01		
	POWHEG+H++		mg5_amc@nlo+P8 FxFx			
$p_{\rm T}(t_{\rm high})$	6.60/12	0.883	16.3/12	0.180		
$p_{\rm T}(t_{\rm low})$	28.5/12	< 0.01	15.3/12	0.225		
$p_{\rm T}(t_{\rm h})$	5.09/12	0.955	11.0/12	0.530		
$ y(t_{\rm h}) $	2.39/11	0.997	2.21/11	0.998		
$p_{\mathrm{T}}(t_{\ell})$	6.55/12	0.886	17.4/12	0.136		
$ \mathbf{y}(t_{\ell}) $	2.54/11	0.995	3.99/11	0.970		
$M(t\bar{t})$	4.16/10	0.940	12.1/10	0.275		
$p_{\rm T}(t\bar{t})$	55.0/8	< 0.01	26.8/8	< 0.01		
$ y(t\overline{t}) $	11.9/10	0.292	8.92/10	0.540		
$ y(t_{\rm h}) $ vs. $p_{\rm T}(t_{\rm h})$	57.9/44	0.077	40.2/44	0.634		
$M(t\bar{t})$ vs. $ y(t\bar{t}) $	40.8/35	0.229	58.7/35	< 0.01		
$p_{\rm T}(t_{\rm h})$ vs. $M(t\bar{t})$	93.0/32	< 0.01	166/32	< 0.01		

TABLE II. Comparison between the measured normalized differential cross sections at the parton level and the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++), the multiparton simulation MG5\_aMC@NLO FxFx, and the NNLO QCD + NLO EW calculations. The compatibility with the POWHEG+PYTHIA8 prediction is also calculated including its theoretical uncertainties (with unc.), while those are not taken into account for the other comparisons. The results of the  $\chi^2$  tests are listed, together with the numbers of degrees of freedom (dof) and the corresponding *p*-values.

Distribution	$\chi^2/dof$	<i>p</i> -value	$\chi^2/dof$	<i>p</i> -value	$\chi^2/dof$	<i>p</i> -value
	POWHEG+P8 with unc.		POWHEG+P8		NNLO QCD + NLO EW	
$p_{\rm T}(t_{\rm high})$	18.4/11	0.073	24.4/11	0.011		
$p_{\rm T}(t_{\rm low})$	16.6/11	0.120	40.0/11	< 0.01		
$p_{\rm T}(t_{\rm h})$	16.1/11	0.138	22.9/11	0.018	4.99/11	0.932
$ y(t_{\rm h}) $	1.25/10	1.000	1.33/10	0.999	2.23/10	0.994
$p_{\mathrm{T}}(t_{\ell})$	23.6/11	0.014	33.0/11	< 0.01	8.67/11	0.652
$ y(t_{\ell}) $	2.03/10	0.996	2.29/10	0.994	8.18/10	0.611
$M(t\bar{t})$	7.78/9	0.556	11.3/9	0.259	24.4/9	< 0.01
$p_{\rm T}(t\bar{t})$	5.52/7	0.597	40.9/7	< 0.01		
$ y(t\overline{t}) $	3.89/9	0.919	5.36/9	0.802	9.29/9	0.411

(Table continued)

Distribution	$\chi^2/dof$	<i>p</i> -value	$\chi^2/dof$	<i>p</i> -value	$\chi^2/dof$	<i>p</i> -value
$ y(t_{\rm h}) $ vs. $p_{\rm T}(t_{\rm h})$	22.7/43	0.995	38.8/43	0.654		
$M(t\bar{t})$ vs. $ y(t\bar{t}) $	20.2/34	0.970	33.2/34	0.507		
$p_{\rm T}(t_{\rm h})$ vs. $M(t\bar{t})$	34.4/31	0.309	57.4/31	< 0.01		
	POWHE	G+H++	MG5_aMC@N	ilo+P8 FxFx		
$p_{\rm T}(t_{\rm high})$	4.10/11	0.967	13.2/11	0.283		
$p_{\rm T}(t_{\rm low})$	17.4/11	0.096	11.9/11	0.370		
$p_{\rm T}(t_{\rm h})$	3.61/11	0.980	9.95/11	0.535		
$ y(t_{\rm h}) $	1.63/10	0.998	1.11/10	1.000		
$p_{\mathrm{T}}(t_{\ell})$	8.36/11	0.680	16.4/11	0.128		
$ y(t_{\ell}) $	1.57/10	0.999	2.48/10	0.991		
$M(t\bar{t})$	3.57/9	0.937	7.61/9	0.574		
$p_{\rm T}(t\bar{t})$	43.4/7	< 0.01	20.5/7	< 0.01		
$ y(t\overline{t}) $	5.94/9	0.746	4.65/9	0.864		
$ y(t_{\rm h}) $ vs. $p_{\rm T}(t_{\rm h})$	32.6/43	0.877	27.8/43	0.965		
$M(t\bar{t})$ vs. $ y(t\bar{t}) $	27.2/34	0.788	40.2/34	0.214		
$p_{\rm T}(t_{\rm h})$ vs. $M(t\bar{t})$	67.9/31	< 0.01	77.9/31	< 0.01		

TABLE II. (Continued)

TABLE III. Comparison between the measured absolute differential cross sections at the particle level and the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations of MG5\_aMC@NLO FxFx and SHERPA. The compatibilities with the POWHEG+PYTHIA8 and the SHERPA predictions are also calculated including their theoretical uncertainties (with unc.), while those are not taken into account for the other comparisons. The results of the  $\chi^2$  tests are listed, together with the numbers of degrees of freedom (dof) and the corresponding *p*-values.

Distribution	$\chi^2/dof$	<i>p</i> -value	$\chi^2/dof$	<i>p</i> -value	$\chi^2/dof$	<i>p</i> -value
	POWHEG+P8 with unc.		SHERPA with unc.		POWHEG+P8	
$p_{\mathrm{T}}(t_{\mathrm{h}})$	15.9/12	0.197	7.21/12	0.844	29.5/12	< 0.01
$ y(t_{\rm h}) $	1.96/11	0.999	1.48/11	1.000	2.23/11	0.997
$p_{\mathrm{T}}(t_{\ell})$	27.0/12	< 0.01	22.3/12	0.034	80.2/12	< 0.01
$ y(t_{\ell}) $	4.55/11	0.951	5.07/11	0.928	4.99/11	0.932
$M(t\bar{t})$	5.83/10	0.829	2.40/10	0.992	9.07/10	0.525
$p_{\rm T}(t\bar{t})$	4.96/8	0.761	28.9/8	< 0.01	41.2/8	< 0.01
$ y(t\bar{t}) $	5.93/10	0.821	6.63/10	0.760	8.61/10	0.570
$ y(t_h) $ vs. $p_T(t_h)$	35.7/44	0.810	29.6/44	0.953	64.1/44	0.025
$M(t\bar{t})$ vs. $ y(t\bar{t}) $	25.9/35	0.867	24.2/35	0.914	56.2/35	0.013
$p_{\rm T}(t_{\rm h})$ vs. $M(t\bar{t})$	47.4/32	0.039	57.2/32	< 0.01	73.2/32	< 0.01
	SHERPA		POWHEG+H++		mg5_amc@nlo+P8 FxFx	
$p_{\rm T}(t_{\rm h})$	13.5/12	0.335	32.1/12	< 0.01	17.4/12	0.137
$ y(t_{\rm h}) $	2.32/11	0.997	4.89/11	0.936	3.16/11	0.988
$p_{\mathrm{T}}(t_{\ell})$	39.4/12	< 0.01	21.8/12	0.040	47.7/12	< 0.01
$ y(t_{\ell}) $	5.54/11	0.902	4.04/11	0.969	7.22/11	0.781
$M(t\bar{t})$	2.86/10	0.985	52.8/10	< 0.01	5.45/10	0.859
$p_{\rm T}(t\bar{t})$	68.7/8	< 0.01	46.8/8	< 0.01	21.3/8	< 0.01
$ y(t\bar{t}) $	12.1/10	0.276	18.6/10	0.046	8.13/10	0.616
$ y(t_h) $ vs. $p_T(t_h)$	48.3/44	0.305	116/44	< 0.01	44.9/44	0.434
$M(t\bar{t})$ vs. $ y(t\bar{t}) $	41.5/35	0.208	219/35	< 0.01	55.7/35	0.014
$p_{\rm T}(t_{\rm h})$ vs. $M(t\bar{t})$	66.5/32	< 0.01	152/32	< 0.01	48.9/32	0.028

TABLE IV. Comparison between the measured normalized differential cross sections at the particle level and the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations of MG5\_aMC@NLO FxFx and SHERPA. The compatibilities with the POWHEG+PYTHIA8 and the SHERPA predictions are also calculated including their theoretical uncertainties (with unc.), while those are not taken into account for the other comparisons. The results of the  $\chi^2$  tests are listed, together with the numbers of degrees of freedom (dof) and the corresponding *p*-values.

Distribution	$\chi^2/dof$	<i>p</i> -value	$\chi^2/dof$	<i>p</i> -value	$\chi^2/dof$	<i>p</i> -value
	POWHEG+P8 with unc.		SHERPA with unc.		POWHEG+P8	
$p_{\mathrm{T}}(t_{\mathrm{h}})$	14.9/11	0.186	6.99/11	0.800	29.4/11	< 0.01
$ y(t_{\rm h}) $	1.77/10	0.998	1.25/10	1.000	1.90/10	0.997
$p_{\mathrm{T}}(t_{\ell})$	25.3/11	< 0.01	28.0/11	< 0.01	74.0/11	< 0.01
$ y(t_{\ell}) $	4.50/10	0.922	4.88/10	0.899	5.00/10	0.891
$M(t\bar{t})$	5.69/9	0.770	2.17/9	0.989	9.33/9	0.407
$p_{\mathrm{T}}(t\bar{t})$	5.36/7	0.616	12.5/7	0.086	34.8/7	< 0.01
$ y(t\bar{t}) $	5.79/9	0.761	6.68/9	0.671	8.48/9	0.486
$ y(t_{\rm h}) $ vs. $p_{\rm T}(t_{\rm h})$	27.6/43	0.967	32.7/43	0.872	53.8/43	0.126
$M(t\bar{t})$ vs. $ y(t\bar{t}) $	26.5/34	0.817	22.7/34	0.931	54.0/34	0.016
$p_{\rm T}(t_{\rm h})$ vs. $M(t\bar{t})$	42.5/31	0.082	39.2/31	0.149	64.8/31	< 0.01
	SHERPA		POWHEG+H++		mg5_amc@nlo+P8 FxFx	
$p_{\mathrm{T}}(t_{\mathrm{h}})$	13.9/11	0.238	34.1/11	< 0.01	15.2/11	0.173
$ y(t_{\rm h}) $	1.60/10	0.999	3.81/10	0.955	2.73/10	0.987
$p_{\mathrm{T}}(t_{\ell})$	37.3/11	< 0.01	25.0/11	< 0.01	40.5/11	< 0.01
$ y(t_{\ell}) $	5.28/10	0.872	3.92/10	0.951	5.54/10	0.853
$M(t\bar{t})$	2.99/9	0.965	51.7/9	< 0.01	4.98/9	0.836
$p_{\rm T}(t\bar{t})$	59.4/7	< 0.01	43.8/7	< 0.01	17.9/7	0.013
$ y(t\bar{t}) $	11.3/9	0.253	18.2/9	0.033	8.37/9	0.498
$ y(t_h) $ vs. $p_T(t_h)$	47.7/43	0.287	108/43	< 0.01	40.9/43	0.561
$M(t\bar{t})$ vs. $ y(t\bar{t}) $	37.6/34	0.308	234/34	< 0.01	55.5/34	0.011
$p_{\rm T}(t_{\rm h})$ vs. $M(t\bar{t})$	63.2/31	< 0.01	126/31	< 0.01	43.0/31	0.074



FIG. 30. Differential cross sections at the particle level as a function of  $p_T(t_h)$  in bins of the number of additional jets. The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.


FIG. 31. Differential cross sections at the particle level normalized to the sum of the cross sections  $\sigma_{norm}$  in the measured ranges as a function of  $p_T(t_h)$  in bins of the number of additional jets. The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 32. Differential cross sections at the particle level as a function of  $M(t\bar{t})$  in bins of the number of additional jets. The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 33. Differential cross sections at the particle level normalized to the sum of the cross sections  $\sigma_{norm}$  in the measured ranges as a function of  $M(t\bar{t})$  in bins of the number of additional jets. The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 34. Differential cross sections at the particle level as a function of  $p_T(t\bar{t})$  in bins of the number of additional jets. The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 35. Differential cross sections at the particle level normalized to the sum of the cross sections  $\sigma_{norm}$  in the measured ranges as a function of  $p_T(t\bar{t})$  in bins of the number of additional jets. The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 36. Differential cross section at the particle level as a function of jet  $p_T$ . The upper two rows show the  $p_T$  distributions for the jets in the  $t\bar{t}$  system, the lower two rows the distribution for additional jets. The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 37. Normalized differential cross section at the particle level as a function of jet  $p_T$ . The upper two rows show the  $p_T$  distributions for the jets in the  $t\bar{t}$  system, the lower two rows the distribution for additional jets. The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 38. Upper: absolute (left) and normalized (right) cross sections of jet multiplicities. Middle, lower: absolute cross sections of jet multiplicities for various thresholds of the jet  $p_T$ . The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 39. Distributions of the gap fractions  $f_1(p_T)$  and  $f_2(p_T)$ . The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The measurements are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 40. Differential cross section at the particle level as a function of jet  $|\eta|$ . The upper two rows show the  $|\eta|$  distributions for the jets in the  $t\bar{t}$  system, the lower two rows the distributions for additional jets. The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 41. Normalized differential cross section at the particle level as a function of jet  $|\eta|$ . The upper two rows show the  $|\eta|$  distributions for the jets in the  $t\bar{t}$  system, the lower two rows the distributions for additional jets. The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 42. Differential cross section at the particle level as a function of jet  $\Delta R_{j_t}$ . The upper two rows show the  $\Delta R_{j_t}$  distributions for the jets in the  $t\bar{t}$  system, the lower two rows the distribution for additional jets. The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 43. Normalized differential cross section at the particle level as a function of jet  $\Delta R_{j_t}$ . The upper two rows show the  $\Delta R_{j_t}$  distributions for the jets in the  $t\bar{t}$  system, the lower two rows the distribution for additional jets. The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 44. Differential cross section at the particle level as a function of  $\Delta R_t$ . The upper two rows show the  $\Delta R_t$  distributions for the jets in the  $t\bar{t}$  system, the lower two rows the distribution for additional jets. The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the predictions to the measured cross sections are shown at the bottom of each panel.



FIG. 45. Normalized differential cross section at the particle level as a function of  $\Delta R_t$ . The upper two rows show the  $\Delta R_t$  distributions for the jets in the  $t\bar{t}$  system, the lower two rows the distribution for additional jets. The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx and SHERPA. The ratios of the predictions to the measured cross sections are shown at the bottom of each panel.

TABLE V. Comparison between the absolute measurements involving multiplicities and kinematic properties of jets and the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations of MG5\_aMC@NLO FxFx and SHERPA. The compatibilities with the POWHEG+PYTHIA8 and the SHERPA predictions are also calculated including their theoretical uncertainties (with unc.), while those are not taken into account for the other comparisons. The results of the  $\chi^2$  tests are listed, together with the numbers of degrees of freedom (dof) and the corresponding *p*-values. The rows labeled as "Additional jets" refer to the measurement of the cross section as a function of jet multiplicities for up to five additional jets with  $p_T > 30$  GeV (Fig. 38 upper row).

Distribution	$\chi^2/dof$	<i>p</i> -value	$\chi^2/dof$	<i>p</i> -value	$\chi^2/dof$	<i>p</i> -value
	POWHEG+P	8 with unc.	SHERPA V	with unc.	POWHI	EG+P8
Additional jets	1.52/6	0.958	27.3/6	< 0.01	10.1/6	0.121
Additional jets vs. $p_{\rm T}(t_{\rm h})$	35.1/44	0.830	64.6/44	0.023	71.6/44	< 0.01
Additional jets vs. $M(t\bar{t})$	27.5/36	0.845	68.9/36	< 0.01	38.8/36	0.345
Additional jets vs. $p_{\rm T}(t\bar{t})$	64.6/29	< 0.01	181/29	< 0.01	175/29	< 0.01
$p_{\rm T}({\rm jet})$	70.2/47	0.016	374/47	< 0.01	133/47	< 0.01
$ \eta(\text{jet}) $	120/70	< 0.01	174/70	< 0.01	171/70	< 0.01
$\Delta R_{i}$	60.9/66	0.655	215/66	< 0.01	168/66	< 0.01
$\Delta R_t$	64.0/62	0.405	229/62	< 0.01	121/62	< 0.01
	SHE	RPA	POWHE	G+H++	MG5_aMC@N	ilo+P8 FxFx
Additional jets	63.0/6	< 0.01	34.1/6	< 0.01	11.1/6	0.086
Additional jets vs. $p_{\rm T}(t_{\rm h})$	88.5/44	< 0.01	230/44	< 0.01	53.4/44	0.156
Additional jets vs. $M(t\bar{t})$	112/36	< 0.01	300/36	< 0.01	55.1/36	0.022
Additional jets vs. $p_{\rm T}(t\bar{t})$	285/29	< 0.01	223/29	< 0.01	122/29	< 0.01
$p_{\rm T}({\rm jet})$	768/47	< 0.01	624/47	< 0.01	111/47	< 0.01
$ \eta(\text{jet}) $	214/70	< 0.01	259/70	< 0.01	133/70	< 0.01
$\Delta R_{i}$	334/66	< 0.01	959/66	< 0.01	67.0/66	0.441
$\Delta R_t$	316/62	< 0.01	483/62	< 0.01	78.9/62	0.073

TABLE VI. Comparison between the normalized measurements involving multiplicities and kinematic properties of jets and the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++) and the multiparton simulations of MG5\_aMC@NLO FxFx and SHERPA. The compatibilities with the POWHEG+PYTHIA8 and the SHERPA predictions are also calculated including their theoretical uncertainties (with unc.), while those are not taken into account for the other comparisons. The results of the  $\chi^2$  tests are listed, together with the numbers of degrees of freedom (dof) and the corresponding *p*-values. The rows labeled as "Additional jets" refer to the measurement of the cross section as a function of jet multiplicities for up to five additional jets with  $p_T > 30$  GeV (Fig. 38 upper row).

Distribution	$\chi^2/dof$	<i>p</i> -value	$\chi^2/dof$	<i>p</i> -value	$\chi^2/dof$	<i>p</i> -value
	powheg+P	8 with unc.	SHERPA V	with unc.	POWHI	EG+P8
Additional jets	2.20/5	0.820	26.4/5	< 0.01	12.5/5	0.029
Additional jets vs. $p_{\rm T}(t_{\rm h})$	28.6/43	0.955	35.8/43	0.773	69.7/43	< 0.01
Additional jets vs. $M(t\bar{t})$	24.5/35	0.908	46.1/35	0.100	38.9/35	0.298
Additional jets vs. $p_{\rm T}(t\bar{t})$	73.3/28	< 0.01	122/28	< 0.01	164/28	< 0.01
$p_{\rm T}({\rm jet})$	75.3/46	< 0.01	184/46	< 0.01	134/46	< 0.01
$ \eta(\text{jet}) $	141/69	< 0.01	162/69	< 0.01	160/69	< 0.01
$\Delta R_{i_l}$	69.9/65	0.317	157/65	< 0.01	173/65	< 0.01
$\Delta R_t$	82.2/61	0.036	163/61	< 0.01	126/61	< 0.01
	SHE	RPA	POWHE	G+H++	MG5_aMC@N	lo+P8 FxFx
Additional jets	62.4/5	< 0.01	35.4/5	< 0.01	9.31/5	0.097
Additional jets vs. $p_{\rm T}(t_{\rm h})$	79.8/43	< 0.01	194/43	< 0.01	51.4/43	0.178
Additional jets vs. $M(t\bar{t})$	86.3/35	< 0.01	287/35	< 0.01	48.2/35	0.068
Additional jets vs. $p_{\rm T}(t\bar{t})$	282/28	< 0.01	232/28	< 0.01	112/28	< 0.01
$p_{\rm T}({\rm jet})$	692/46	< 0.01	623/46	< 0.01	112/46	< 0.01
$ \eta(\text{jet}) $	213/69	< 0.01	255/69	< 0.01	121/69	< 0.01
$\Delta R_{i_l}$	301/65	< 0.01	976/65	< 0.01	65.2/65	0.469
$\Delta R_t$	325/61	< 0.01	506/61	< 0.01	74.7/61	0.112

## **XII. SUMMARY**

Measurements of the absolute and normalized differential and double-differential cross sections for  $t\bar{t}$  production in proton-proton collisions at  $\sqrt{s} = 13$  TeV have been presented. The data correspond to an integrated luminosity of 35.8 fb<sup>-1</sup> recorded by the CMS experiment. The  $t\bar{t}$ production cross section is measured in the  $\ell$  + jets channels at the parton and particle levels as a function of the transverse momentum  $p_{\rm T}$  and absolute rapidity |y| of the top quarks and  $p_{\rm T}$ , |y|, and invariant mass of the  $t\bar{t}$ system. In addition, at the particle level detailed studies of multiplicities and kinematic properties of the jets in  $t\bar{t}$ events are performed. The dominant sources of uncertainty are the jet energy scale uncertainties on the experimental side and parton shower modeling on the theoretical side.

The results are compared to several standard model predictions that use different methods and approximations for their calculations. The simulations of POWHEG +PYTHIA8 and SHERPA, for which theoretical uncertainties are considered, describe most of the studied kinematic distributions of the top quark and the  $t\bar{t}$  system reasonably well. The largest deviation is the measurement of a softer  $p_{\rm T}$  spectrum of the top quarks compared to all the predictions. This has also been observed in other measurements [5-10,13,14,18]. Most of the kinematic distributions and multiplicities of additional jets are modeled reasonably well by POWHEG+PYTHIA8, however, this description of additional jets relies on the phenomenological model of the parton shower with tuned parameters. With the selected settings SHERPA fails to describe most of these distributions. Comparisons of the measurements to the central values of all tested models, ignoring their theoretical uncertainties, result in low *p*-values for many distributions related to the  $p_{\rm T}$  of the top quarks or the  $t\bar{t}$  system, and for the kinematic distributions and multiplicities of additional jets.

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# APPENDIX A: TABLES OF PARTON-LEVEL CROSS SECTIONS

The measured differential cross sections at the parton level as a function of all the measured variables are listed in Tables VII–XVI. The results are shown together with their statistical and systematic uncertainties.

TABLE VII. Differential cross section at the parton level as a function of  $p_{\rm T}(t_{\rm high})$ . The values are shown together with their statistical and systematic uncertainties.

$p_{\rm T}(t_{\rm high})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\mathrm{high}})}$ [fb GeV <sup>-1</sup> ]	$p_{\rm T}(t_{\rm high})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\mathrm{high}})}$ [fb GeV <sup>-1</sup> ]
0-40	$333 \pm 8 \pm 31$	240-280	$258\pm3\pm16$
40-80	$1244 \pm 11 \pm 96$	280-330	$135.0 \pm 1.9 \pm 9.2$
80-120	$1460 \pm 10 \pm 110$	330-380	$67.3 \pm 1.3 \pm 5.2$
120-160	$1213 \pm 9 \pm 94$	380-430	$34.4 \pm 1.0 \pm 3.9$
160-200	$777\pm7\pm53$	430-500	$15.7 \pm 0.6 \pm 1.5$
200–240	$468\pm5\pm31$	500-800	$3.16 \pm 0.11 \pm 0.34$

TABLE VIII. Differential cross section at the parton level as a function of  $p_{\rm T}(t_{\rm low})$ . The values are shown together with their statistical and systematic uncertainties.

$p_{\rm T}(t_{\rm low})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\mathrm{low}})}$ [fb GeV <sup>-1</sup> ]	$p_{\rm T}(t_{\rm low})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\mathrm{low}})}$ [fb GeV <sup>-1</sup> ]
0-40	$1054\pm8\pm77$	240-280	$115.4 \pm 1.5 \pm 7.0$
40-80	$1770\pm9\pm130$	280-330	$54.3 \pm 0.9 \pm 3.7$
80-120	$1420\pm8\pm110$	330–380	$24.3 \pm 0.6 \pm 1.8$
120-160	$871 \pm 5 \pm 61$	380-430	$11.2 \pm 0.4 \pm 1.1$
160-200	$463 \pm 4 \pm 28$	430-500	$5.34 \pm 0.28 \pm 0.52$
200-240	$232\pm2\pm16$	500-800	$0.92 \pm 0.08 \pm 0.20$

TABLE IX. Differential cross section at the parton level as a function of  $p_{T}(t_{h})$ . The values are shown together with their statistical and systematic uncertainties.

$p_{\rm T}(t_{\rm h})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\mathrm{h}})}$ [fb GeV <sup>-1</sup> ]	$p_{\rm T}(t_{\rm h})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\mathrm{h}})}$ [fb GeV <sup>-1</sup> ]
0-40	$687\pm7\pm50$	240–280	$188 \pm 2 \pm 11$
40-80	$1490\pm8\pm100$	280-330	$95.6 \pm 1.3 \pm 6.0$
80-120	$1460 \pm 8 \pm 110$	330-380	$47.2 \pm 0.9 \pm 3.4$
120-160	$1022 \pm 6 \pm 79$	380-430	$22.9 \pm 0.6 \pm 1.8$
160-200	$621 \pm 4 \pm 42$	430-500	$10.03 \pm 0.40 \pm 0.95$
200–240	$347\pm3\pm23$	500-800	$2.15 \pm 0.11 \pm 0.33$

$ y(t_{\rm h}) $	$\frac{\mathrm{d}\sigma}{\mathrm{d} y(t_{\mathrm{h}}) }$ [pb]	$ y(t_{\rm h}) $	$\frac{\mathrm{d}\sigma}{\mathrm{d} y(t_{\mathrm{h}}) }  [\mathrm{pb}]$
0.0-0.2	$145.5 \pm 0.8 \pm 9.4$	1.2–1.4	$93.3 \pm 0.8 \pm 6.6$
0.2-0.4	$144.5 \pm 0.9 \pm 9.5$	1.4–1.6	$78.1 \pm 0.8 \pm 6.6$
0.4-0.6	$137.0 \pm 0.9 \pm 8.7$	1.6-1.8	$66.9 \pm 0.8 \pm 5.4$
0.6-0.8	$129.7 \pm 0.8 \pm 8.8$	1.8-2.0	$53.2 \pm 0.8 \pm 4.8$
0.8-1.0	$117.0 \pm 0.8 \pm 8.1$	2.0-2.5	$32.9 \pm 0.6 \pm 2.9$
1.0-1.2	$106.5 \pm 0.8 \pm 7.8$		

TABLE X. Differential cross section at the parton level as a function of  $|y(t_h)|$ . The values are shown together with their statistical and systematic uncertainties.

TABLE XI. Differential cross section at the parton level as a function of  $p_T(t\bar{t})$ . The values are shown together with their statistical and systematic uncertainties.

$p_{\rm T}(t\bar{t})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t\bar{t})}$ [fb GeV <sup>-1</sup> ]	$p_{\rm T}(t\bar{t})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t\bar{t})}$ [fb GeV <sup>-1</sup> ]
0-40	$2950\pm20\pm230$	220-300	$78.4 \pm 1.9 \pm 7.8$
40-80	$1470\pm20\pm110$	300-380	$26.7 \pm 1.1 \pm 2.5$
80-150	$570\pm 6\pm 45$	380-500	$10.15 \pm 0.42 \pm 0.93$
150-220	$194\pm4\pm14$	500-1000	$1.20 \pm 0.05 \pm 0.11$

TABLE XII. Differential cross section at the parton level as a function of  $|y(t\bar{t})|$ . The values are shown together with their statistical and systematic uncertainties.

$ y(t\bar{t}) $	$\frac{\mathrm{d}\sigma}{\mathrm{d} y(t\bar{t}) }$ [pb]	$ y(t\overline{t}) $	$\frac{\mathrm{d}\sigma}{\mathrm{d} y(t\bar{t}) }$ [pb]
0.0–0.2	$173 \pm 1 \pm 12$	1.0-1.2	$105.2 \pm 1.2 \pm 7.9$
0.2-0.4	$168 \pm 1 \pm 11$	1.2–1.4	$90.2 \pm 1.2 \pm 6.4$
0.4-0.6	$157 \pm 1 \pm 11$	1.4–1.6	$71.2 \pm 1.3 \pm 6.3$
0.6-0.8	$145 \pm 1 \pm 10$	1.6-1.8	$50.7 \pm 1.4 \pm 6.2$
0.8–1.0	$128.1 \pm 1.2 \pm 9.0$	1.8–2.4	$26.4 \pm 1.1 \pm 3.0$

TABLE XIII. Differential cross section at the parton level as a function of  $M(t\bar{t})$ . The values are shown together with their statistical and systematic uncertainties.

$M(t\bar{t})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}M(t\bar{t})}$ [fb GeV <sup>-1</sup> ]	$M(t\bar{t})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}M(t\bar{t})}$ [fb GeV <sup>-1</sup> ]
300–360	$247 \pm 8 \pm 57$	680-800	$125 \pm 2 \pm 10$
360-430	$1081\pm9\pm92$	800-1000	$47.7 \pm 0.9 \pm 3.5$
430-500	$791\pm8\pm70$	1000-1200	$16.3 \pm 0.6 \pm 1.3$
500-580	$485\pm 6\pm 32$	1200-1500	$4.85 \pm 0.27 \pm 0.56$
580-680	$261 \pm 4 \pm 20$	1500-2500	$0.62 \pm 0.05 \pm 0.12$

$p_{\rm T}(t_{\rm h})$ [GeV]	$\frac{\mathrm{d}^2\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\mathrm{h}})\mathrm{d} y(t_{\mathrm{h}}) } \ [\mathrm{pb} \ \mathrm{GeV}^{-1}]$	$p_{\rm T}(t_{\rm h})$ [GeV]	$\frac{\mathrm{d}^2\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\mathrm{h}})\mathrm{d} y(t_{\mathrm{h}}) }$ [pb GeV <sup>-1</sup> ]
	0 <  y	$(t_{\rm h})  < 0.5$	
0–40	$0.382 \pm 0.004 \pm 0.026$	240–280	$0.1276 \pm 0.0017 \pm 0.0075$
40-80	$0.850 \pm 0.006 \pm 0.058$	280-330	$0.0669 \pm 0.0011 \pm 0.0041$
80-120	$0.860 \pm 0.006 \pm 0.060$	330–380	$0.0343 \pm 0.0008 \pm 0.0024$
120-160	$0.622 \pm 0.005 \pm 0.043$	380-450	$0.0150 \pm 0.0005 \pm 0.0014$
160-200	$0.394 \pm 0.003 \pm 0.027$	450-800	$(2.59 \pm 0.12 \pm 0.28) \times 10^{-3}$
200-240	$0.225 \pm 0.002 \pm 0.015$		
	0.5 <	$ y(t_{\rm h})  < 1$	
0–40	$0.337 \pm 0.004 \pm 0.027$	240–280	$0.1060 \pm 0.0016 \pm 0.0068$
40-80	$0.759 \pm 0.006 \pm 0.054$	280-330	$0.0562 \pm 0.0010 \pm 0.0035$
80-120	$0.766 \pm 0.005 \pm 0.056$	330–380	$0.0287 \pm 0.0007 \pm 0.0024$
120-160	$0.548 \pm 0.004 \pm 0.044$	380-450	$0.0131 \pm 0.0005 \pm 0.0015$
160-200	$0.334 \pm 0.003 \pm 0.024$	450-800	$(1.77 \pm 0.10 \pm 0.20) \times 10^{-3}$
200-240	$0.191 \pm 0.002 \pm 0.014$		
	1 <  y	$(t_{\rm h})  < 1.5$	
0–40	$0.269 \pm 0.004 \pm 0.022$	240–280	$0.0770 \pm 0.0014 \pm 0.0061$
40-80	$0.603 \pm 0.006 \pm 0.046$	280-330	$0.0382 \pm 0.0009 \pm 0.0029$
80-120	$0.583 \pm 0.005 \pm 0.046$	330–380	$0.0176 \pm 0.0006 \pm 0.0014$
120-160	$0.414 \pm 0.004 \pm 0.035$	380-450	$(7.63 \pm 0.35 \pm 0.79) \times 10^{-3}$
160-200	$0.252 \pm 0.003 \pm 0.018$	450-800	$(1.17 \pm 0.08 \pm 0.21) \times 10^{-3}$
200-240	$0.143 \pm 0.002 \pm 0.011$		
	1.5 <	$ v(t_{\rm h})  < 2.5$	
0–40	$0.150 \pm 0.003 \pm 0.015$	240–280	$0.0299 \pm 0.0008 \pm 0.0032$
40-80	$0.318 \pm 0.004 \pm 0.026$	280-330	$0.0144 \pm 0.0005 \pm 0.0015$
80-120	$0.309 \pm 0.004 \pm 0.028$	330–380	$(5.99 \pm 0.29 \pm 1.00) \times 10^{-3}$
120-160	$0.214 \pm 0.003 \pm 0.022$	380-450	$(2.35 \pm 0.16 \pm 0.42) \times 10^{-3}$
160-200	$0.119 \pm 0.002 \pm 0.011$	450-800	$(2.63 \pm 0.31 \pm 0.51) \times 10^{-4}$
200-240	$0.0596 \pm 0.0012 \pm 0.0054$		••••

TABLE XIV. Double-differential cross section at the parton level as a function of  $|y(t_h)|$  vs.  $p_T(t_h)$ . The values are shown together with their statistical and systematic uncertainties.

TABLE XV. Double-differential cross section at the parton level as a function of  $M(t\bar{t})$  vs.  $|y(t\bar{t})|$ . The values are shown together with their statistical and systematic uncertainties.

$ y(t\overline{t}) $	$\frac{\mathrm{d}^2\sigma}{\mathrm{d}M(t\bar{t})\mathrm{d} y(t\bar{t}) }$ [fb GeV <sup>-1</sup> ]	$ y(t\overline{t}) $	$\frac{\mathrm{d}^2\sigma}{\mathrm{d}M(t\bar{t})\mathrm{d} y(t\bar{t}) } [\mathrm{fb}\mathrm{GeV^{-1}}]$
		$300 < M(t\bar{t}) < 450$	
0.0-0.2	$473 \pm 4 \pm 31$	1.0–1.2	$323\pm4\pm23$
0.2-0.4	$460\pm4\pm30$	1.2–1.4	$282\pm4\pm21$
0.4–0.6	$441\pm4\pm29$	1.4–1.6	$238\pm4\pm19$
0.6-0.8	$420\pm4\pm29$	1.6–2.4	$128\pm3\pm13$
0.8-1.0	$379 \pm 4 \pm 27$		
		$450 < M(t\bar{t}) < 625$	
0.0-0.2	$379\pm3\pm27$	1.0–1.2	$229\pm3\pm20$
0.2-0.4	$368 \pm 3 \pm 26$	1.2–1.4	$194 \pm 3 \pm 17$
0.4-0.6	$344 \pm 3 \pm 26$	1.4–1.6	$151\pm3\pm16$
0.6-0.8	$310\pm3\pm26$	1.6–2.4	$60.3 \pm 1.8 \pm 8.3$
0.8-1.0	$275\pm3\pm22$		
		$625 < M(t\bar{t}) < 850$	
0.0-0.2	$113.6 \pm 1.6 \pm 9.5$	1.0–1.2	$58.8 \pm 1.5 \pm 5.6$
0.2-0.4	$108.2 \pm 1.5 \pm 7.4$	1.2–1.4	$43.7 \pm 1.5 \pm 4.2$
0.4–0.6	$99.9 \pm 1.6 \pm 8.6$	1.4–1.6	$30.0 \pm 1.6 \pm 3.3$

$ y(t\bar{t}) $	$\frac{\mathrm{d}^2\sigma}{\mathrm{d}M(i\bar{t})\mathrm{d} y(i\bar{t}) }$ [fb GeV <sup>-1</sup> ]	$ y(t\overline{t}) $	$\frac{\mathrm{d}^2\sigma}{\mathrm{d}M(t\bar{t})\mathrm{d} y(t\bar{t}) }$ [fb GeV <sup>-1</sup> ]
0.6–0.8	$88.9 \pm 1.6 \pm 7.3$	1.6–2.4	$9.6 \pm 0.7 \pm 1.3$
0.8-1.0	$75.7 \pm 1.6 \pm 5.7$		
	850 < M(	$(t\bar{t}) < 2000$	
0.0-0.2	$9.21 \pm 0.21 \pm 0.77$	0.8–1.0	$5.00 \pm 0.22 \pm 0.54$
0.2–0.4	$9.36 \pm 0.23 \pm 0.85$	1.0-1.2	$4.27 \pm 0.24 \pm 0.45$
0.4-0.6	$8.39 \pm 0.23 \pm 0.74$	1.2–1.4	$2.71 \pm 0.22 \pm 0.58$
0.6–0.8	$6.94 \pm 0.23 \pm 0.59$	1.4–2.4	$0.433 \pm 0.057 \pm 0.091$

TABLE XVI. Double-differential cross section at the parton level as a function of  $p_T(t_h)$  vs.  $M(t\bar{t})$ . The values are shown together with their statistical and systematic uncertainties.

$M(t\bar{t})$ [GeV]	$\frac{\mathrm{d}^2\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\mathrm{h}})\mathrm{d}M(t\bar{t})} [\mathrm{fb}\mathrm{GeV}^{-2}]$	$M(t\bar{t})$ [GeV]	$\frac{\mathrm{d}^2\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\mathrm{h}})\mathrm{d}M(t\bar{t})} [\mathrm{fb}\mathrm{GeV}^{-2}]$
	$0 < \mu$	$p_{\rm T}(t_{\rm h}) < 90$	
300-360	$2.30 \pm 0.04 \pm 0.42$	580–680	$0.652 \pm 0.015 \pm 0.059$
360-430	$8.07 \pm 0.05 \pm 0.61$	680-800	$0.279 \pm 0.009 \pm 0.036$
430-500	$2.98 \pm 0.04 \pm 0.37$	800-1000	$0.096 \pm 0.005 \pm 0.019$
500-580	$1.37 \pm 0.02 \pm 0.13$	1000-2000	$0.0113 \pm 0.0014 \pm 0.0033$
	$90 < \mu$	$p_{\rm T}(t_{\rm h}) < 180$	
300-360	$0.184 \pm 0.007 \pm 0.031$	580–680	$1.144 \pm 0.017 \pm 0.097$
360-430	$3.89 \pm 0.04 \pm 0.29$	680-800	$0.489 \pm 0.011 \pm 0.056$
430-500	$5.23 \pm 0.04 \pm 0.44$	800-1000	$0.172 \pm 0.006 \pm 0.019$
500-580	$2.59 \pm 0.03 \pm 0.21$	1000-2000	$0.0169 \pm 0.0012 \pm 0.0039$
	180 <	$p_{\rm T}(t_{\rm h}) < 270$	
300-430	$0.105 \pm 0.005 \pm 0.029$	680–800	$0.387 \pm 0.008 \pm 0.033$
430-500	$0.573 \pm 0.014 \pm 0.040$	800-1000	$0.134 \pm 0.004 \pm 0.013$
500-580	$1.330 \pm 0.018 \pm 0.096$	1000-1200	$0.0437 \pm 0.0027 \pm 0.0066$
580-680	$0.937 \pm 0.013 \pm 0.075$	1200-2000	$(5.2 \pm 0.6 \pm 1.6) \times 10^{-3}$
	270 <	$p_{\rm T}(t_{\rm h}) < 800$	
300-430	$(3.1 \pm 0.4 \pm 1.1) \times 10^{-3}$	680–800	$0.0464 \pm 0.0010 \pm 0.0033$
430-500	$0.0141 \pm 0.0009 \pm 0.0022$	800-1000	$0.0259 \pm 0.0005 \pm 0.0020$
500-580	$0.0196 \pm 0.0009 \pm 0.0032$	1000-1200	$0.01027 \pm 0.00038 \pm 0.00097$
580-680	$0.0359 \pm 0.0011 \pm 0.0034$	1200-2000	$(2.02 \pm 0.08 \pm 0.21) \times 10^{-3}$

#### APPENDIX B: TABLES OF PARTICLE-LEVEL CROSS SECTIONS

The measured differential cross sections at the particle level as a function of all the measured variables are listed in Tables XVII–XXXIV. The results are shown together with their statistical and systematic uncertainties.

TABLE XVII. Differential cross section at the particle level as a function of  $p_{\rm T}(t_{\rm h})$ . The values are shown together with their statistical and systematic uncertainties.

$p_{\rm T}(t_{\rm h})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\mathrm{h}})}$ [fb GeV <sup>-1</sup> ]	$p_{\rm T}(t_{\rm h})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\mathrm{h}})}$ [fb GeV <sup>-1</sup> ]
0-40	$163.5 \pm 1.3 \pm 8.9$	240–280	$70.0 \pm 0.7 \pm 4.0$
40-80	$376\pm2\pm20$	280-330	$39.1 \pm 0.5 \pm 2.5$
80-120	$391\pm2\pm23$	330-380	$20.4 \pm 0.3 \pm 1.3$
120-160	$295\pm2\pm17$	380-430	$10.37 \pm 0.24 \pm 0.75$
160-200	$192\pm1\pm11$	430-500	$4.64 \pm 0.15 \pm 0.38$
200–240	$116.5 \pm 0.9 \pm 6.7$	500-800	$0.81 \pm 0.03 \pm 0.11$

$ y(t_{\rm h}) $	$\frac{\mathrm{d}\sigma}{\mathrm{d} y(t_{\mathrm{h}}) }$ [pb]	$ y(t_{\rm h}) $	$\frac{\mathrm{d}\sigma}{\mathrm{d} y(t_{\mathrm{h}}) }$ [pb]
0.0-0.2	$52.8 \pm 0.2 \pm 2.8$	1.2–1.4	$27.1 \pm 0.2 \pm 1.6$
0.2-0.4	$51.6 \pm 0.2 \pm 2.7$	1.4–1.6	$19.9 \pm 0.2 \pm 1.4$
0.4-0.6	$48.2 \pm 0.2 \pm 2.6$	1.6–1.8	$13.08 \pm 0.13 \pm 0.90$
0.6-0.8	$44.9 \pm 0.2 \pm 2.4$	1.8-2.0	$6.79 \pm 0.10 \pm 0.50$
0.8-1.0	$39.1 \pm 0.2 \pm 2.2$	2.0-2.5	$1.009 \pm 0.024 \pm 0.084$
1.0-1.2	$33.8 \pm 0.2 \pm 1.9$		

TABLE XVIII. Differential cross section at the particle level as a function of  $|y(t_h)|$ . The values are shown together with their statistical and systematic uncertainties.

TABLE XIX. Differential cross section at the particle level as a function of  $p_{T}(t_{\ell})$ . The values are shown together with their statistical and systematic uncertainties.

$p_{\mathrm{T}}(t_{\ell})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\ell})}$ [fb GeV <sup>-1</sup> ]	$p_{\mathrm{T}}(t_{\ell})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\ell})}$ [fb GeV <sup>-1</sup> ]
0-40	$151.1 \pm 2.4 \pm 9.9$	240–280	$75.5 \pm 1.6 \pm 6.0$
40-80	$357\pm4\pm21$	280-330	$43.2 \pm 1.0 \pm 2.8$
80-120	$368\pm4\pm22$	330–380	$22.1 \pm 0.7 \pm 2.3$
120-160	$316 \pm 3 \pm 18$	380-430	$11.1 \pm 0.6 \pm 1.7$
160-200	$195\pm3\pm12$	430-500	$5.78 \pm 0.29 \pm 0.71$
200–240	$132.1 \pm 2.0 \pm 8.1$	500-800	$0.97 \pm 0.04 \pm 0.10$

TABLE XX. Differential cross section at the particle level as a function of  $|y(t_{\ell})|$ . The values are shown together with their statistical and systematic uncertainties.

$ y(t_\ell) $	$\frac{\mathrm{d}\sigma}{\mathrm{d} y(t_\ell) }$ [pb]	$ y(t_\ell) $	$\frac{\mathrm{d}\sigma}{\mathrm{d} y(t_{\ell}) }$ [pb]
0.0–0.2	$49.9 \pm 0.5 \pm 2.9$	1.2–1.4	$28.0 \pm 0.5 \pm 2.0$
0.2-0.4	$48.7 \pm 0.6 \pm 2.7$	1.4–1.6	$19.2 \pm 0.4 \pm 1.6$
0.4–0.6	$47.6 \pm 0.6 \pm 2.6$	1.6-1.8	$14.6 \pm 0.4 \pm 1.2$
0.6-0.8	$44.2 \pm 0.6 \pm 2.6$	1.8-2.0	$8.75 \pm 0.31 \pm 0.98$
0.8-1.0	$39.0 \pm 0.6 \pm 2.4$	2.0-2.5	$2.34 \pm 0.10 \pm 0.27$
1.0–1.2	$33.9 \pm 0.5 \pm 2.0$		

TABLE XXI. Differential cross section at the particle level as a function of  $p_{\rm T}(t\bar{t})$ . The values are shown together with their statistical and systematic uncertainties.

$p_{\rm T}(t\bar{t})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t\bar{t})}$ [fb GeV <sup>-1</sup> ]	$p_{\rm T}(t\bar{t})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t\bar{t})}$ [fb GeV <sup>-1</sup> ]
0-40	$768 \pm 3 \pm 45$	220-300	$26.4 \pm 0.5 \pm 1.9$
40-80	$436 \pm 4 \pm 25$	300-380	$9.59 \pm 0.33 \pm 0.82$
80-150	$172\pm1\pm11$	380-500	$3.96 \pm 0.14 \pm 0.30$
150-220	$63.1 \pm 0.9 \pm 3.9$	500-1000	$0.447 \pm 0.017 \pm 0.035$

TABLE XXII. Differential cross section at the particle level as a function of  $|y(t\bar{t})|$ . The values are shown together with their statistical and systematic uncertainties.

$ y(t\bar{t}) $	$\frac{\mathrm{d}\sigma}{\mathrm{d} y(t\bar{t}) }$ [pb]	$ y(t\bar{t}) $	$\frac{\mathrm{d}\sigma}{\mathrm{d} y(t\bar{t}) }$ [pb]
0.0-0.2	$67.0 \pm 0.3 \pm 3.6$	1.0-1.2	$27.8 \pm 0.3 \pm 1.7$
0.2-0.4	$63.4 \pm 0.4 \pm 3.4$	1.2–1.4	$19.0 \pm 0.2 \pm 1.2$
0.4-0.6	$57.0 \pm 0.4 \pm 3.2$	1.4–1.6	$10.59 \pm 0.18 \pm 0.76$
0.6-0.8	$49.1 \pm 0.3 \pm 2.8$	1.6–1.8	$4.57 \pm 0.12 \pm 0.51$
0.8–1.0	$39.2 \pm 0.3 \pm 2.2$	1.8–2.4	$0.643 \pm 0.030 \pm 0.082$

$M(t\bar{t})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}M(t\bar{t})}$ [fb GeV <sup>-1</sup> ]	$M(t\bar{t})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}M(t\bar{t})}$ [fb GeV <sup>-1</sup> ]
300-360	$76.2 \pm 1.1 \pm 8.6$	680-800	$55.1 \pm 0.6 \pm 3.3$
360-430	$200\pm1\pm12$	800-1000	$24.6 \pm 0.3 \pm 1.5$
430-500	$191\pm1\pm13$	1000-1200	$8.91 \pm 0.21 \pm 0.65$
500-580	$147.1 \pm 1.0 \pm 8.3$	1200-1500	$3.03 \pm 0.11 \pm 0.27$
580-680	$96.3 \pm 0.8 \pm 5.7$	1500-2500	$0.417 \pm 0.025 \pm 0.049$

TABLE XXIII. Differential cross section at the particle level as a function of  $M(t\bar{t})$ . The values are shown together with their statistical and systematic uncertainties.

TABLE XXIV. Cross sections at the particle level for different numbers of additional jets. The values are shown together with their statistical and systematic uncertainties.

Additional jets	$\sigma$ [pb]	Additional jets	$\sigma$ [pb]
0	$38.0 \pm 0.10 \pm 1.8$	3	$2.33 \pm 0.03 \pm 0.21$
1	$19.7 \pm 0.08 \pm 1.2$	4	$0.629 \pm 0.017 \pm 0.079$
2	$7.13 \pm 0.05 \pm 0.55$	≥5	$0.244 \pm 0.008 \pm 0.033$

 $\frac{\mathrm{d}^2\sigma}{\mathrm{d}p_\mathrm{T}(t_\mathrm{h})\mathrm{d}|y(t_\mathrm{h})|}$  [fb GeV^-1]  $\frac{\mathrm{d}^2\sigma}{\mathrm{d}p_\mathrm{T}(t_\mathrm{h})\mathrm{d}|y(t_\mathrm{h})|}$  [fb GeV<sup>-1</sup>]  $p_{\rm T}(t_{\rm h})$  [GeV]  $p_{\rm T}(t_{\rm h})$  [GeV]  $0 < |y(t_{\rm h})| < 0.5$ 0-40  $121.9 \pm 1.1 \pm 6.8$ 240 - 280 $53.8 \pm 0.7 \pm 3.0$ 40-80  $284\pm2\pm16$ 280-330  $29.6 \pm 0.5 \pm 1.9$ 80-120  $298\pm2\pm17$ 330-380  $15.9 \pm 0.3 \pm 1.0$  $222\pm1\pm13$  $7.14 \pm 0.21 \pm 0.58$ 120-160 380-450 160 - 200 $146.4 \pm 1.1 \pm 8.0$ 450-800  $1.12 \pm 0.04 \pm 0.11$ 200-240  $87.9 \pm 0.9 \pm 5.1$ . . .  $0.5 < |y(t_{\rm h})| < 1$ 0-40  $103.1 \pm 1.0 \pm 7.2$ 240-280  $43.1 \pm 0.6 \pm 2.7$ 40-80  $240 \pm 2 \pm 13$ 280-330  $24.6 \pm 0.4 \pm 1.6$ 80-120  $251\pm2\pm14$ 330-380  $12.90 \pm 0.30 \pm 0.93$ 120-160  $187\pm1\pm12$ 380-450  $6.06 \pm 0.19 \pm 0.49$ 160-200  $119.3 \pm 1.0 \pm 7.1$  $0.789 \pm 0.035 \pm 0.070$ 450-800 200-240  $72.3 \pm 0.8 \pm 4.7$  $1 < |y(t_{\rm h})| < 1.5$ 0-40  $68.5 \pm 0.9 \pm 4.5$ 240-280  $29.3 \pm 0.5 \pm 2.1$  $159.7 \pm 1.3 \pm 9.5$ 40-80 280-330  $16.2 \pm 0.3 \pm 1.2$ 80-120  $163\pm1\pm10$ 330-380  $8.06 \pm 0.23 \pm 0.67$ 120-160  $125.2 \pm 1.1 \pm 8.2$ 380-450  $3.50 \pm 0.14 \pm 0.35$ 160-200  $81.2 \pm 0.9 \pm 5.6$ 450-800  $0.507 \pm 0.029 \pm 0.075$ 200-240  $50.5 \pm 0.6 \pm 3.3$  $1.5 < |y(t_{\rm h})| < 2.5$ 0-40  $14.7 \pm 0.3 \pm 1.3$ 240-280  $6.80 \pm 0.17 \pm 0.66$ 40 - 80 $32.8 \pm 0.4 \pm 2.4$ 280-330  $3.84 \pm 0.12 \pm 0.45$ 80-120  $36.2 \pm 0.5 \pm 2.8$ 330-380  $1.87 \pm 0.08 \pm 0.29$ 120-160  $28.9 \pm 0.4 \pm 2.6$ 380-450  $0.81 \pm 0.05 \pm 0.15$ 160-200 450-800  $0.080 \pm 0.008 \pm 0.021$  $18.7 \pm 0.3 \pm 1.6$  $11.26 \pm 0.23 \pm 0.91$ 200-240 . . .

TABLE XXV. Double-differential cross section at the particle level as a function of  $|y(t_h)|$  vs.  $p_T(t_h)$ . The values are shown together with their statistical and systematic uncertainties.

$ y(t\bar{t}) $	$\frac{\mathrm{d}^2\sigma}{\mathrm{d}M(t\bar{t})\mathrm{d} y(t\bar{t}) } [\mathrm{fb} \mathrm{GeV^{-1}}]$	$ y(t\overline{t}) $	$\frac{\mathrm{d}^2\sigma}{\mathrm{d}M(t\bar{t})\mathrm{d} y(t\bar{t}) } \text{ [fb GeV}^{-1}\text{]}$
		$300 < M(t\bar{t}) < 450$	
0.0-0.2	$125.5 \pm 1.1 \pm 6.9$	1.0–1.2	$73.3 \pm 0.8 \pm 4.4$
0.2-0.4	$121.8 \pm 0.9 \pm 6.5$	1.2–1.4	$55.2 \pm 0.7 \pm 3.4$
0.4-0.6	$116.3 \pm 1.0 \pm 6.3$	1.4–1.6	$34.5 \pm 0.6 \pm 2.3$
0.6-0.8	$109.0 \pm 0.9 \pm 6.6$	1.6–2.4	$6.05 \pm 0.15 \pm 0.64$
0.8-1.0	$93.2\pm0.9\pm5.3$		
		$450 < M(t\bar{t}) < 625$	
0.0-0.2	$144.8 \pm 1.1 \pm 8.2$	1.0–1.2	$62.5 \pm 0.7 \pm 4.5$
0.2-0.4	$137.8 \pm 1.0 \pm 7.8$	1.2–1.4	$41.5 \pm 0.6 \pm 3.1$
0.4–0.6	$125.1 \pm 0.9 \pm 7.4$	1.4–1.6	$22.6 \pm 0.5 \pm 2.1$
0.6-0.8	$107.4 \pm 0.9 \pm 6.8$	1.6–2.4	$3.03 \pm 0.10 \pm 0.38$
0.8-1.0	$86.6\pm0.8\pm5.5$		
		$625 < M(t\bar{t}) < 850$	
0.0-0.2	$64.8 \pm 0.7 \pm 3.7$	1.0–1.2	$19.8 \pm 0.4 \pm 1.5$
0.2-0.4	$59.8 \pm 0.6 \pm 3.4$	1.2–1.4	$11.2 \pm 0.3 \pm 1.2$
0.4-0.6	$51.4 \pm 0.6 \pm 3.6$	1.4–1.6	$5.41 \pm 0.22 \pm 0.48$
0.6-0.8	$41.6 \pm 0.5 \pm 3.1$	1.6–2.4	$0.686 \pm 0.044 \pm 0.076$
0.8-1.0	$31.4\pm0.5\pm2.1$		
		$850 < M(t\bar{t}) < 2000$	
0.0-0.2	$6.81 \pm 0.11 \pm 0.44$	0.8–1.0	$2.35 \pm 0.07 \pm 0.18$
0.2-0.4	$6.39 \pm 0.11 \pm 0.46$	1.0–1.2	$1.44 \pm 0.06 \pm 0.12$
0.4-0.6	$5.22 \pm 0.10 \pm 0.36$	1.2–1.4	$0.703 \pm 0.041 \pm 0.090$
0.6–0.8	$3.80 \pm 0.09 \pm 0.29$	1.4–2.4	$0.062 \pm 0.006 \pm 0.011$

TABLE XXVI. Double-differential cross section at the particle level as a function of  $M(t\bar{t})$  vs.  $|y(t\bar{t})|$ . The values are shown together with their statistical and systematic uncertainties.

TABLE XXVII. Double-differential cross section at the particle level as a function of  $p_T(t_h)$  vs.  $M(t\bar{t})$ . The values are shown together with their statistical and systematic uncertainties.

$M(t\bar{t})$ [GeV]	$\frac{\mathrm{d}^2\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\mathrm{h}})\mathrm{d}M(t\bar{t})} [\mathrm{fb} \mathrm{GeV^{-2}}]$	$M(t\bar{t})$ [GeV]	$\frac{\mathrm{d}^2\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\mathrm{h}})\mathrm{d}M(t\bar{t})}$ [fb GeV <sup>-2</sup> ]
	$0 < p_{\rm T}$	$(t_{\rm h}) < 90$	
300-360	$0.737 \pm 0.009 \pm 0.069$	580–680	$0.242 \pm 0.003 \pm 0.017$
360-430	$1.424 \pm 0.009 \pm 0.084$	680-800	$0.1141 \pm 0.0019 \pm 0.0091$
430-500	$0.794 \pm 0.007 \pm 0.054$	800-1000	$0.0423 \pm 0.0011 \pm 0.0041$
500-580	$0.448 \pm 0.004 \pm 0.029$	1000-2000	$(4.14 \pm 0.23 \pm 0.73) \times 10^{-3}$
	$90 < p_{\rm T}$	$(t_{\rm h}) < 180$	
300-360	$0.0805 \pm 0.0021 \pm 0.0083$	580–680	$0.451 \pm 0.004 \pm 0.028$
360-430	$0.757 \pm 0.007 \pm 0.044$	680-800	$0.226 \pm 0.003 \pm 0.016$
430-500	$1.195 \pm 0.008 \pm 0.079$	800-1000	$0.0895 \pm 0.0016 \pm 0.0064$
500-580	$0.832 \pm 0.006 \pm 0.053$	1000-2000	$(8.7 \pm 0.3 \pm 1.2) \times 10^{-3}$
	$180 < p_{\rm T}$	$(t_{\rm h}) < 270$	
300-430	$0.0194 \pm 0.0009 \pm 0.0045$	680–800	$0.179 \pm 0.003 \pm 0.012$
430-500	$0.1235 \pm 0.0027 \pm 0.0098$	800-1000	$0.0751 \pm 0.0014 \pm 0.0057$
500-580	$0.325 \pm 0.004 \pm 0.020$	1000-1200	$0.0260 \pm 0.0009 \pm 0.0027$
580-680	$0.320 \pm 0.004 \pm 0.022$	1200-2000	$(3.79 \pm 0.24 \pm 0.62) \times 10^{-3}$
	$270 < p_{\rm T}$	$(t_{\rm h}) < 800$	
300-430	$(4.2 \pm 0.5 \pm 1.4) \times 10^{-4}$	680–800	$0.0170 \pm 0.0003 \pm 0.0011$
430-500	$(2.83 \pm 0.16 \pm 0.48) \times 10^{-3}$	800-1000	$0.01261 \pm 0.00021 \pm 0.00086$
500-580	$(5.18 \pm 0.21 \pm 0.84) \times 10^{-3}$	1000-1200	$(6.01 \pm 0.17 \pm 0.48) \times 10^{-3}$
580-680	$0.01043 \pm 0.00027 \pm 0.00085$	1200-2000	$(1.42 \pm 0.04 \pm 0.12) \times 10^{-3}$

$p_{\rm T}(t_{\rm h})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\mathrm{h}})}$ [fb GeV <sup>-1</sup> ]	$p_{\rm T}(t_{\rm h})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\mathrm{h}})}$ [fb GeV <sup>-1</sup> ]
	Add	itional jets: 0	
0–40	$98.4 \pm 0.9 \pm 5.9$	240-280	$32.7 \pm 0.4 \pm 2.0$
40-80	$223\pm1\pm11$	280-330	$16.8 \pm 0.3 \pm 1.2$
80-120	$230\pm1\pm13$	330–380	$8.44 \pm 0.18 \pm 0.63$
120-160	$167.7 \pm 1.0 \pm 8.9$	380-450	$3.47 \pm 0.11 \pm 0.36$
160-200	$103.3 \pm 0.7 \pm 5.6$	450-800	$0.470 \pm 0.021 \pm 0.052$
200-240	$58.6 \pm 0.5 \pm 3.5$		
	Add	itional jets: 1	
0–40	$43.6 \pm 0.4 \pm 3.4$	240-280	$22.9 \pm 0.3 \pm 1.5$
40-80	$103.5 \pm 0.6 \pm 7.4$	280-330	$12.96 \pm 0.21 \pm 0.89$
80-120	$109.1 \pm 0.6 \pm 6.9$	330-380	$6.44 \pm 0.14 \pm 0.57$
120-160	$85.4 \pm 0.5 \pm 5.4$	380-450	$2.99 \pm 0.09 \pm 0.25$
160-200	$57.7 \pm 0.5 \pm 3.6$	450-800	$0.431 \pm 0.019 \pm 0.043$
200-240	$36.9 \pm 0.4 \pm 2.6$		
	Add	itional jets: 2	
0–40	$14.3 \pm 0.2 \pm 1.5$	240–280	$9.71 \pm 0.17 \pm 0.76$
40-80	$34.7 \pm 0.3 \pm 2.8$	280-330	$6.02 \pm 0.12 \pm 0.56$
80-120	$38.1 \pm 0.3 \pm 3.1$	330–380	$3.39 \pm 0.10 \pm 0.33$
120-160	$30.5 \pm 0.3 \pm 2.7$	380-450	$1.60 \pm 0.06 \pm 0.14$
160-200	$22.0 \pm 0.2 \pm 1.8$	450-800	$0.217 \pm 0.012 \pm 0.025$
200-240	$14.7 \pm 0.2 \pm 1.4$		
	Addi	tional jets: $\geq 3$	
0–40	$5.82 \pm 0.10 \pm 0.55$	240-280	$4.77 \pm 0.11 \pm 0.59$
40-80	$14.1 \pm 0.2 \pm 1.5$	280-330	$3.30 \pm 0.09 \pm 0.41$
80-120	$15.5 \pm 0.2 \pm 1.6$	330-380	$2.07 \pm 0.07 \pm 0.23$
120-160	$13.0 \pm 0.2 \pm 1.3$	380-450	$1.09 \pm 0.05 \pm 0.12$
160-200	$9.6 \pm 0.1 \pm 1.1$	450-800	$0.162 \pm 0.010 \pm 0.026$
200-240	$6.72 \pm 0.13 \pm 0.71$		

TABLE XXVIII. Differential cross sections at the particle level as a function of  $p_{\rm T}(t_{\rm h})$  for different numbers of additional jets. The values are shown together with their statistical and systematic uncertainties.

TABLE XXIX. Differential cross sections at the particle level as a function of  $p_T(t\bar{t})$  for different numbers of additional jets. The values are shown together with their statistical and systematic uncertainties.

$p_{\rm T}(t\bar{t})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t\bar{t})}$ [pb GeV <sup>-1</sup> ]	$p_{\rm T}(t\bar{t})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t\bar{t})}$ [pb GeV <sup>-1</sup> ]
	Additio	onal jets: 0	
0–40	$0.665 \pm 0.003 \pm 0.037$	150-220	$(4.82 \pm 0.27 \pm 0.74) \times 10^{-3}$
40-80	$0.216 \pm 0.003 \pm 0.018$	220-300	$(7.2 \pm 1.0 \pm 2.0) \times 10^{-4}$
80-150	$0.0325 \pm 0.0007 \pm 0.0027$	300-1000	$(2.49 \pm 0.47 \pm 0.76) \times 10^{-5}$
	Additio	onal jets: 1	
0–40	$0.0794 \pm 0.0015 \pm 0.0089$	220-300	$0.01043 \pm 0.00034 \pm 0.00079$
40-80	$0.172 \pm 0.002 \pm 0.012$	300-380	$(3.89 \pm 0.21 \pm 0.66) \times 10^{-3}$
80-150	$0.0879 \pm 0.0011 \pm 0.0047$	380-1000	$(4.33 \pm 0.18 \pm 0.34) \times 10^{-4}$
150-220	$0.0306 \pm 0.0006 \pm 0.0017$		
	Additio	onal jets: 2	
0–40	$0.0168 \pm 0.0007 \pm 0.0029$	220-300	$(9.09 \pm 0.33 \pm 0.82) \times 10^{-3}$
40-80	$0.0367 \pm 0.0008 \pm 0.0037$	300-380	$(3.27 \pm 0.20 \pm 0.66) \times 10^{-3}$
80-150	$0.0358 \pm 0.0007 \pm 0.0032$	380-500	$(1.28 \pm 0.09 \pm 0.15) \times 10^{-3}$
150-220	$0.0181 \pm 0.0005 \pm 0.0016$	500-1000	$(1.19 \pm 0.12 \pm 0.18) \times 10^{-4}$
	Additio	nal jets: ≥3	
0–40	$(4.5 \pm 0.3 \pm 1.2) \times 10^{-3}$	220-300	$(6.30 \pm 0.25 \pm 0.89) \times 10^{-3}$
40-80	$0.0124 \pm 0.0005 \pm 0.0017$	300-380	$(2.42 \pm 0.17 \pm 0.44) \times 10^{-3}$
80-150	$0.0135 \pm 0.0004 \pm 0.0016$	380-500	$(1.16 \pm 0.08 \pm 0.20) \times 10^{-3}$
150-220	$(9.9 \pm 0.4 \pm 1.0) \times 10^{-3}$	500-1000	$(1.61 \pm 0.11 \pm 0.20) \times 10^{-4}$

$\overline{M(t\bar{t})}$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}M(t\bar{t})}$ [fb GeV <sup>-1</sup> ]	$M(t\bar{t})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}M(t\bar{t})}$ [fb GeV <sup>-1</sup> ]
	Add	ditional jets: 0	
300-360	$43.7 \pm 0.6 \pm 4.9$	680-800	$31.4 \pm 0.3 \pm 1.6$
360-430	$109.8 \pm 0.7 \pm 5.8$	800-1000	$14.27 \pm 0.17 \pm 0.91$
430-500	$104.2 \pm 0.7 \pm 6.0$	1000-1200	$5.24 \pm 0.12 \pm 0.50$
500-580	$80.9 \pm 0.5 \pm 4.4$	1200-2000	$0.989 \pm 0.034 \pm 0.086$
580-680	$53.8 \pm 0.4 \pm 3.0$		
	Add	ditional jets: 1	
300-360	$20.7 \pm 0.3 \pm 2.2$	680-800	$15.6 \pm 0.2 \pm 1.0$
360-430	$59.7 \pm 0.5 \pm 3.9$	800-1000	$6.79 \pm 0.11 \pm 0.46$
430-500	$57.3 \pm 0.4 \pm 4.1$	1000-1200	$2.43 \pm 0.07 \pm 0.25$
500-580	$42.9 \pm 0.3 \pm 2.8$	1200-2000	$0.385 \pm 0.017 \pm 0.043$
580-680	$27.9 \pm 0.3 \pm 2.0$		
	Add	ditional jets: 2	
300-360	$6.85 \pm 0.14 \pm 0.55$	680-800	$5.60 \pm 0.10 \pm 0.56$
360-430	$22.3 \pm 0.3 \pm 1.7$	800-1000	$2.44 \pm 0.06 \pm 0.20$
430-500	$21.2 \pm 0.2 \pm 2.1$	1000-1200	$0.85 \pm 0.04 \pm 0.10$
500-580	$15.9 \pm 0.2 \pm 1.4$	1200-2000	$0.135 \pm 0.009 \pm 0.019$
580-680	$10.06 \pm 0.14 \pm 0.95$		
	Add	itional jets: ≥3	
300-360	$2.52 \pm 0.08 \pm 0.33$	680-800	$2.49 \pm 0.06 \pm 0.36$
360-430	$9.5 \pm 0.2 \pm 1.0$	800-1000	$1.14 \pm 0.04 \pm 0.19$
430-500	$9.7 \pm 0.1 \pm 1.1$	1000-1200	$0.418 \pm 0.025 \pm 0.057$
500-580	$7.14 \pm 0.12 \pm 0.77$	1200-2000	$0.065 \pm 0.006 \pm 0.019$
580-680	$4.58 \pm 0.09 \pm 0.54$		

TABLE XXX. Differential cross sections at the particle level as a function of  $M(t\bar{t})$  for different numbers of additional jets. The values are shown together with their statistical and systematic uncertainties.

TABLE XXXI.	Differential cross sections at the particle level as a function of $p_{T}(jet)$ for jets. The values are shown together with their
statistical and sy	vstematic uncertainties.

$p_{\rm T}({\rm jet})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(\mathrm{jet})}$ [pb GeV <sup>-1</sup> ]	$p_{\rm T}({\rm jet})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(\mathrm{jet})}$ [pb GeV <sup>-1</sup> ]
		$p_{\mathrm{T}}(\mathbf{b}_{\ell})$	
30-50	$0.913 \pm 0.004 \pm 0.052$	100–150	$0.206 \pm 0.001 \pm 0.011$
50-75	$0.748 \pm 0.003 \pm 0.040$	150-200	$0.0643 \pm 0.0006 \pm 0.0036$
75–100	$0.466 \pm 0.002 \pm 0.026$	200–350	$(9.53 \pm 0.13 \pm 0.59) \times 10^{-3}$
		$p_{\mathrm{T}}(\mathbf{b}_{\mathrm{h}})$	
30–50	$0.858 \pm 0.004 \pm 0.045$	100–150	$0.211 \pm 0.001 \pm 0.013$
50-75	$0.771 \pm 0.003 \pm 0.040$	150-200	$0.0640 \pm 0.0006 \pm 0.0041$
75–100	$0.491 \pm 0.002 \pm 0.029$	200-350	$0.01103 \pm 0.00015 \pm 0.00075$
	I	$\mathcal{P}_{\mathrm{T}}(\mathbf{j}_{W1})$	
30-50	$0.861 \pm 0.004 \pm 0.042$	100-150	$0.213 \pm 0.001 \pm 0.012$
50-75	$0.864 \pm 0.003 \pm 0.047$	150-200	$0.0663 \pm 0.0007 \pm 0.0040$
75–100	$0.506 \pm 0.003 \pm 0.029$	200-350	$0.01270 \pm 0.00018 \pm 0.00085$
	I	$p_{\mathrm{T}}(\mathbf{j}_{W2})$	
30-50	$1.730 \pm 0.004 \pm 0.090$	75–100	$0.1223 \pm 0.0012 \pm 0.0077$
50-75	$0.443 \pm 0.002 \pm 0.028$	100-250	$0.01019 \pm 0.00017 \pm 0.00071$
		$p_{\mathrm{T}}(\mathbf{j}_1)$	
30–50	$0.410 \pm 0.002 \pm 0.029$	150-175	$0.0613 \pm 0.0007 \pm 0.0041$
50-75	$0.253 \pm 0.002 \pm 0.019$	175-200	$0.0432 \pm 0.0006 \pm 0.0029$
75–100	$0.174 \pm 0.001 \pm 0.012$	200–250	$0.0286 \pm 0.0004 \pm 0.0019$

$p_{\rm T}({\rm jet})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(\mathrm{jet})}$ [pb GeV <sup>-1</sup> ]	$p_{\rm T}({\rm jet})$ [GeV]	$\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(\mathrm{jet})}$ [pb GeV <sup>-1</sup> ]
100–125	$0.1207 \pm 0.0011 \pm 0.0089$	250-320	$0.0145 \pm 0.0002 \pm 0.0010$
125–150	$0.0840 \pm 0.0009 \pm 0.0056$	320-500	$(4.71 \pm 0.07 \pm 0.29) \times 10^{-3}$
	Ľ	$\mathbf{p}_{\mathrm{T}}(\mathbf{j}_{2})$	
30-50	$0.246 \pm 0.002 \pm 0.022$	125–150	$0.0138 \pm 0.0003 \pm 0.0014$
50-75	$0.103 \pm 0.001 \pm 0.011$	150-180	$(7.54 \pm 0.26 \pm 0.74) \times 10^{-3}$
75-100	$0.0501 \pm 0.0007 \pm 0.0052$	180-350	$(1.65 \pm 0.05 \pm 0.17) \times 10^{-3}$
100–125	$0.0258 \pm 0.0005 \pm 0.0029$		
	Į	$p_{\mathrm{T}}(\mathbf{j}_3)$	
30-50	$0.097 \pm 0.001 \pm 0.011$	75–100	$(10.0 \pm 0.3 \pm 1.6) \times 10^{-3}$
50–75	$0.0290 \pm 0.0005 \pm 0.0041$	100-250	$(1.35 \pm 0.05 \pm 0.19) \times 10^{-3}$
	Į	$\mathbf{p}_{\mathrm{T}}(\mathbf{j}_{4})$	
30-50	$0.0307 \pm 0.0006 \pm 0.0046$	75–100	$(1.75 \pm 0.11 \pm 0.37) \times 10^{-3}$
50-75	$(6.7\pm0.2\pm1.2) imes10^{-3}$	100-200	$(2.64 \pm 0.26 \pm 0.58) \times 10^{-4}$

## TABLE XXXI. (Continued)

TABLE XXXII.	Differential cross sections at the particle level as a function of $ n(iet) $ for jets. The values are shown together with
their statistical an	id systematic uncertainties.

$ \eta(\text{jet}) $	$\frac{\mathrm{d}\sigma}{\mathrm{d}\eta(\mathrm{jet})}$ [pb]	$ \eta({ m jet}) $	$\frac{\mathrm{d}\sigma}{\mathrm{d}\eta(\mathrm{jet})}$ [pb]
		$ \eta(\mathbf{b}_{\ell}) $	
0.00-0.25	$42.4 \pm 0.2 \pm 2.3$	1.25–1.50	$25.7 \pm 0.2 \pm 1.4$
0.25-0.50	$41.6 \pm 0.2 \pm 2.3$	1.50-1.75	$20.9 \pm 0.1 \pm 1.2$
0.50-0.75	$39.6 \pm 0.2 \pm 2.1$	1.75-2.00	$16.69 \pm 0.13 \pm 0.97$
0.75-1.00	$35.9 \pm 0.2 \pm 1.9$	2.00-2.25	$12.37 \pm 0.12 \pm 0.74$
1.00-1.25	$31.6 \pm 0.2 \pm 1.7$	2.25-2.50	$5.14 \pm 0.09 \pm 0.34$
		$ \eta({ m b_h}) $	
0.00-0.25	$44.9 \pm 0.2 \pm 2.3$	1.25-1.50	$24.8 \pm 0.2 \pm 1.4$
0.25-0.50	$43.6 \pm 0.2 \pm 2.3$	1.50-1.75	$19.6 \pm 0.1 \pm 1.1$
0.50-0.75	$40.6 \pm 0.2 \pm 2.1$	1.75-2.00	$15.3 \pm 0.1 \pm 1.0$
0.75-1.00	$36.8 \pm 0.2 \pm 1.9$	2.00-2.25	$10.93 \pm 0.12 \pm 0.73$
1.00-1.25	$30.8 \pm 0.2 \pm 1.7$	2.25-2.50	$4.54 \pm 0.08 \pm 0.34$
		$ \eta(\mathbf{j}_{W1}) $	
0.00-0.25	$43.1 \pm 0.2 \pm 2.3$	1.25–1.50	$25.5 \pm 0.2 \pm 1.4$
0.25-0.50	$42.0 \pm 0.2 \pm 2.3$	1.50-1.75	$20.9 \pm 0.1 \pm 1.2$
0.50-0.75	$39.1 \pm 0.2 \pm 2.0$	1.75-2.00	$16.6 \pm 0.1 \pm 1.0$
0.75-1.00	$35.7 \pm 0.2 \pm 1.9$	2.00-2.25	$12.52 \pm 0.12 \pm 0.77$
1.00-1.25	$32.0 \pm 0.2 \pm 1.8$	2.25–2.50	$5.66 \pm 0.08 \pm 0.38$
		$ \eta(\mathbf{j}_{W2}) $	
0.00-0.25	$40.6 \pm 0.2 \pm 2.1$	1.25-1.50	$26.6 \pm 0.2 \pm 1.4$
0.25-0.50	$39.4 \pm 0.2 \pm 2.0$	1.50-1.75	$22.3 \pm 0.2 \pm 1.3$
0.50-0.75	$37.1 \pm 0.2 \pm 1.9$	1.75-2.00	$18.6 \pm 0.1 \pm 1.1$
0.75-1.00	$34.7 \pm 0.2 \pm 1.8$	2.00-2.25	$15.00 \pm 0.12 \pm 0.94$
1.00-1.25	$31.4 \pm 0.2 \pm 1.6$	2.25–2.50	$7.07 \pm 0.09 \pm 0.50$
		$ \eta(j_1) $	
0.00-0.25	$13.76 \pm 0.11 \pm 0.95$	1.25-1.50	$12.45 \pm 0.10 \pm 0.84$
0.25-0.50	$13.72 \pm 0.11 \pm 0.97$	1.50-1.75	$11.84 \pm 0.10 \pm 0.83$
0.50-0.75	$13.57 \pm 0.11 \pm 0.88$	1.75-2.00	$11.54 \pm 0.10 \pm 0.86$
0.75-1.00	$13.73 \pm 0.11 \pm 0.85$	2.00-2.25	$10.33 \pm 0.09 \pm 0.76$
1.00–1.25	$13.11 \pm 0.10 \pm 0.96$	2.25–2.50	$5.57 \pm 0.06 \pm 0.41$

## TABLE XXXII. (Continued)

$ \eta(\text{jet}) $	$\frac{\mathrm{d}\sigma}{\mathrm{d}\eta(\mathrm{jet})}$ [pb]		$ \eta(\text{jet}) $	$\frac{\mathrm{d}\sigma}{\mathrm{d}\eta(\mathrm{jet})}$ [pb]
		$ n(\mathbf{i}_2) $		
0.00-0.25	$4.75 \pm 0.06 \pm 0.52$	17(02)	1.25-1.50	$4.28 \pm 0.06 \pm 0.39$
0.25-0.50	$4.90 \pm 0.06 \pm 0.46$		1.50-1.75	$4.15 \pm 0.05 \pm 0.39$
0.50-0.75	$4.62 \pm 0.06 \pm 0.51$		1.75-2.00	$3.92 \pm 0.05 \pm 0.37$
0.75-1.00	$4.64 \pm 0.06 \pm 0.49$		2.00-2.25	$3.52 \pm 0.05 \pm 0.32$
1.00-1.25	$4.58 \pm 0.06 \pm 0.46$		2.25-2.50	$1.91 \pm 0.04 \pm 0.18$
		$ \eta(\mathbf{i}_3) $		
0.0-0.5	$1.43 \pm 0.02 \pm 0.19$	11/05/1	1.5-2.0	$1.21 \pm 0.02 \pm 0.14$
0.5-1.0	$1.46 \pm 0.02 \pm 0.16$		2.0-2.5	$0.808 \pm 0.015 \pm 0.098$
1.0–1.5	$1.38 \pm 0.02 \pm 0.16$			
		$ \eta(\mathbf{i}_4) $		
0.0-0.5	$0.399 \pm 0.010 \pm 0.067$	1104/1	1.5-2.0	$0.320 \pm 0.009 \pm 0.057$
0.5-1.0	$0.408 \pm 0.010 \pm 0.060$		2.0-2.5	$0.216 \pm 0.008 \pm 0.040$
1.0–1.5	$0.402 \pm 0.011 \pm 0.053$			

TABLE XXXIII.	Differential cross sections at the particle level as a function of $\Delta R_{i}$ , for jets. The values are shown together with	h their
statistical and syst	matic uncertainties.	

$\Delta R_{j_t}$	$\frac{\mathrm{d}\sigma}{\mathrm{d}\Delta R_{j_{f}}}$ [fb]	$\Delta R_{j_r}$	$\frac{\mathrm{d}\sigma}{\mathrm{d}\Delta R_{j_{l}}}$ [fb]
		$\Delta R_{i} (b_{\ell})$	
0.4-0.6	$16400 \pm 200 \pm 1100$	1.4–1.6	$32600 \pm 200 \pm 1800$
0.6-0.8	$27300 \pm 200 \pm 1600$	1.6–2.0	$31300 \pm 100 \pm 1700$
0.8-1.0	$28800 \pm 200 \pm 1600$	2.0–2.5	$25600 \pm 100 \pm 1400$
1.0-1.2	$31400 \pm 200 \pm 1700$	2.5-4.5	$4450\pm20\pm230$
1.2–1.4	$32800 \pm 200 \pm 1800$		
		$\Delta R_{i_{\ell}}(\mathbf{b}_{\mathrm{h}})$	
0.4-0.6	$21800 \pm 200 \pm 1300$	1.4–1.6	$41600 \pm 200 \pm 2200$
0.6-0.8	$36500 \pm 200 \pm 2000$	1.6-2.0	$30800 \pm 100 \pm 1700$
0.8-1.0	$41800 \pm 200 \pm 2200$	2.0-2.5	$14340 \pm 100 \pm 840$
1.0-1.2	$46100 \pm 200 \pm 2400$	2.5-4.5	$980 \pm 15 \pm 75$
1.2–1.4	$45800 \pm 200 \pm 2500$		
		$\Delta R_{\rm i.}({\rm j}_{W1})$	
0.4-0.6	$23400 \pm 200 \pm 1200$	1.4–1.6	$40100 \pm 200 \pm 2300$
0.6-0.8	$39300 \pm 200 \pm 1900$	1.6-2.0	$27400 \pm 100 \pm 1500$
0.8-1.0	$44600 \pm 200 \pm 2300$	2.0-2.5	$12550 \pm 90 \pm 710$
1.0-1.2	$48800 \pm 300 \pm 2500$	2.5-4.5	$1330\pm17\pm93$
1.2–1.4	$46600 \pm 200 \pm 2500$		
		$\Delta R_{i_{\ell}}(j_{W2})$	
0.4–0.6	$25500 \pm 200 \pm 1400$	1.4–1.6	$39900 \pm 200 \pm 2200$
0.6-0.8	$41300 \pm 200 \pm 2100$	1.6-2.0	$26500 \pm 100 \pm 1500$
0.8-1.0	$44800 \pm 300 \pm 2200$	2.0-2.5	$11890 \pm 90 \pm 700$
1.0-1.2	$48200 \pm 300 \pm 2600$	2.5-4.5	$1250\pm16\pm81$
1.2–1.4	$46300 \pm 300 \pm 2400$		
		$\Delta R_{i}(j_1)$	
0.4-0.6	$13920 \pm 130 \pm 980$	1.4–1.6	$13720 \pm 130 \pm 950$
0.6-0.8	$18000 \pm 100 \pm 1300$	1.6-2.0	$11460 \pm 80 \pm 780$
0.8-1.0	$16100 \pm 100 \pm 1100$	2.0–2.5	$8110\pm60\pm520$
1.0-1.2	$15500 \pm 100 \pm 1100$	2.5-4.5	$1459\pm12\pm97$
1.2–1.4	$14500 \pm 100 \pm 1100$		

$\overline{\Delta R_{j_t}}$	$\frac{\mathrm{d}\sigma}{\mathrm{d}\Delta R_{j_{t}}}$ [fb]	$\Delta R_{\mathrm{j}_{r}}$	$\frac{\mathrm{d}\sigma}{\mathrm{d}\Delta R_{\mathrm{j}_{t}}}$ [fb]
		$\Delta R_{\rm i}$ (i <sub>2</sub> )	
0.4–0.6	$5240 \pm 70 \pm 490$	1.4-1.6	$4510 \pm 70 \pm 400$
0.6–0.8	$6780 \pm 80 \pm 640$	1.6-2.0	$3770 \pm 50 \pm 350$
0.8-1.0	$5870 \pm 80 \pm 530$	2.0-2.5	$2530 \pm 30 \pm 230$
1.0-1.2	$5500\pm70\pm490$	2.5-4.5	$463\pm7\pm41$
1.2–1.4	$5050\pm70\pm450$		
		$\Delta R_{i}(j_{3})$	
0.4-0.8	$1780 \pm 30 \pm 220$	1.6–2.0	$1170 \pm 20 \pm 150$
0.8-1.2	$1720 \pm 30 \pm 190$	2.0-2.5	$759\pm17\pm89$
1.2–1.6	$1490\pm30\pm160$	2.5–4.5	$148\pm4\pm15$
		$\Delta R_{i}(i_{A})$	
0.4–0.8	$477 \pm 13 \pm 68$	1.6–2.0	$319\pm11\pm56$
0.8-1.2	$483\pm13\pm67$	2.0-2.5	$221\pm9\pm35$
1.2–1.6	$404\pm12\pm58$	2.5–4.5	$40.3 \pm 1.9 \pm 6.2$

#### TABLE XXXIII. (Continued)

TABLE XXXIV. Differential cross sections at the particle level as a function of  $\Delta R_t$  for jets. The values are shown together with their statistical and systematic uncertainties.

$\Delta R_t$	$\frac{\mathrm{d}\sigma}{\mathrm{d}\Delta R_t}$ [fb]	$\Delta R_t$	$\frac{\mathrm{d}\sigma}{\mathrm{d}\Delta R_t}$ [fb]
		$\Delta R_t(\mathbf{b}_{\ell})$	
0.0-0.3	$18000 \pm 100 \pm 1100$	1.2–1.5	$32300 \pm 100 \pm 1800$
0.3-0.6	$38300 \pm 200 \pm 2200$	1.5–2.0	$21000 \pm 100 \pm 1200$
0.6-0.9	$41800 \pm 200 \pm 2300$	2.0-2.5	$9110 \pm 70 \pm 540$
0.9–1.2	$38300 \pm 200 \pm 2100$	2.5–4.5	$1318\pm16\pm88$
		$\Delta R_t(\mathbf{b_h})$	
0.0-0.3	$18300 \pm 100 \pm 1100$	1.2–1.5	$32800 \pm 200 \pm 1700$
0.3-0.6	$37200 \pm 200 \pm 2000$	1.5-2.0	$21900 \pm 100 \pm 1200$
0.6-0.9	$40500 \pm 200 \pm 2100$	2.0-2.5	$9440\pm80\pm580$
0.9–1.2	$37400 \pm 200 \pm 2000$	2.5–4.5	$1334\pm16\pm89$
		$\Delta R_t(\mathbf{j}_{W1})$	
0.0-0.3	$25800 \pm 200 \pm 1300$	1.2–1.5	$26800 \pm 100 \pm 1500$
0.3–0.6	$47200 \pm 200 \pm 2500$	1.5-2.0	$16860 \pm 90 \pm 930$
0.6–0.9	$44300 \pm 200 \pm 2400$	2.0-2.5	$7630 \pm 60 \pm 430$
0.9–1.2	$35300 \pm 200 \pm 2000$	2.5–4.5	$1187\pm14\pm78$
		$\Delta R_t(\mathbf{j}_{W2})$	
0.0-0.3	$8980 \pm 100 \pm 480$	1.2–1.5	$36000 \pm 200 \pm 2000$
0.3–0.6	$26700 \pm 200 \pm 1300$	1.5-2.0	$26100 \pm 100 \pm 1400$
0.6–0.9	$37100 \pm 200 \pm 1900$	2.0-2.5	$12970 \pm 90 \pm 720$
0.9–1.2	$38600 \pm 200 \pm 2100$	2.5–4.5	$2230\pm20\pm140$
		$\Delta R_t(j_1)$	
0.0-0.3	$1160 \pm 30 \pm 110$	1.2–1.5	$9210\pm80\pm680$
0.3–0.6	$3480\pm50\pm280$	1.5-2.0	$11380 \pm 70 \pm 820$
0.6–0.9	$5950\pm60\pm460$	2.0-2.5	$11600 \pm 80 \pm 790$
0.9–1.2	$7610\pm70\pm550$	2.5–4.5	$5020\pm30\pm330$
		$\Delta R_t(j_2)$	
0.0-0.3	$482\pm15\pm53$	1.2–1.5	$3720 \pm 40 \pm 350$
0.3–0.6	$1550\pm30\pm150$	1.5-2.0	$4140\pm40\pm380$
0.6–0.9	$2640\pm40\pm260$	2.0-2.5	$3820\pm40\pm380$
0.9–1.2	$3260\pm40\pm300$	2.5–4.5	$1380\pm10\pm120$

#### TABLE XXXIV. (Continued)

$\Delta R_t$	$\frac{\mathrm{d}\sigma}{\mathrm{d}\Delta R_t}$ [fb]	$\Delta R_t$	$\frac{\mathrm{d}\sigma}{\mathrm{d}\Delta R_{t}}$ [fb]
		$\Delta R_{\star}(\mathbf{i}_{2})$	
0.0-0.4	$181 \pm 7 \pm 31$	1.5–2.0	$1280\pm20\pm150$
0.4-0.8	$642\pm14\pm79$	2.0-2.5	$1160 \pm 20 \pm 150$
0.8-1.2	$1000 \pm 20 \pm 120$	2.5-4.5	$408\pm7\pm46$
1.2–1.5	$1160\pm20\pm140$		
		$\Delta R_t(j_4)$	
0.0-0.4	$42.7 \pm 2.9 \pm 9.2$	1.5–2.0	$359\pm10\pm55$
0.4–0.8	$163\pm 6\pm 23$	2.0-2.5	$322\pm9\pm55$
0.8-1.2	$273\pm9\pm38$	2.5-4.5	$113\pm3\pm18$
1.2–1.5	$324\pm10\pm53$		

#### APPENDIX C: TABLES OF NORMALIZED PARTON-LEVEL CROSS SECTIONS

The measured normalized differential cross sections at the parton level as a function of all the measured variables are listed in Tables XXXV–XLIV. The results are shown together with their statistical and systematic uncertainties.

TABLE XXXV. Differential cross section at the parton level as a function of  $p_{\rm T}(t_{\rm high})$  normalized to the cross section  $\sigma_{\rm norm}$  in the measured range. The values are shown together with their statistical and systematic uncertainties.

$p_{\rm T}(t_{\rm high})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\text{high}})}  [\mathrm{GeV}^{-1}]$	$p_{\rm T}(t_{\rm high})$ [GeV]	$\frac{1}{\sigma_{\rm norm}} \frac{{\rm d}\sigma}{{\rm d}p_{\rm T}(t_{\rm high})}  [{ m GeV^{-1}}]$
0-40	$(1.364 \pm 0.032 \pm 0.092) \times 10^{-3}$	240-280	$(1.056 \pm 0.013 \pm 0.039) \times 10^{-3}$
40-80	$(5.10 \pm 0.04 \pm 0.16) \times 10^{-3}$	280-330	$(5.53 \pm 0.08 \pm 0.24) \times 10^{-4}$
80-120	$(6.00 \pm 0.05 \pm 0.15) \times 10^{-3}$	330-380	$(2.75 \pm 0.05 \pm 0.18) \times 10^{-4}$
120-160	$(4.97 \pm 0.04 \pm 0.14) \times 10^{-3}$	380-430	$(1.41 \pm 0.04 \pm 0.14) \times 10^{-4}$
160-200	$(3.183 \pm 0.027 \pm 0.076) \times 10^{-3}$	430-500	$(6.45 \pm 0.24 \pm 0.56) \times 10^{-5}$
200-240	$(1.918 \pm 0.019 \pm 0.051) \times 10^{-3}$	500-800	$(1.30 \pm 0.04 \pm 0.11) \times 10^{-5}$

TABLE XXXVI. Differential cross section at the parton level as a function of  $p_T(t_{low})$  normalized to the cross section  $\sigma_{norm}$  in the measured range. The values are shown together with their statistical and systematic uncertainties.

$p_{\rm T}(t_{\rm low})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\mathrm{low}})}  [\mathrm{GeV}^{-1}]$	$p_{\rm T}(t_{\rm low})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\text{low}})}  [\mathrm{GeV}^{-1}]$
0-40	$(4.35 \pm 0.03 \pm 0.14) \times 10^{-3}$	240-280	$(4.76 \pm 0.06 \pm 0.25) \times 10^{-4}$
40-80	$(7.307 \pm 0.032 \pm 0.095) \times 10^{-3}$	280-330	$(2.24 \pm 0.04 \pm 0.11) \times 10^{-4}$
80-120	$(5.88 \pm 0.03 \pm 0.12) \times 10^{-3}$	330-380	$(1.004 \pm 0.025 \pm 0.059) \times 10^{-4}$
120-160	$(3.593 \pm 0.022 \pm 0.075) \times 10^{-3}$	380-430	$(4.62 \pm 0.17 \pm 0.45) \times 10^{-5}$
160-200	$(1.909 \pm 0.015 \pm 0.051) \times 10^{-3}$	430-500	$(2.20 \pm 0.12 \pm 0.20) \times 10^{-5}$
200-240	$(9.58 \pm 0.10 \pm 0.20) \times 10^{-4}$	500-800	$(3.81 \pm 0.32 \pm 0.75) \times 10^{-6}$

TABLE XXXVII. Differential cross section at the parton level as a function of  $p_T(t_h)$  normalized to the cross section  $\sigma_{norm}$  in the measured range. The values are shown together with their statistical and systematic uncertainties.

$p_{\rm T}(t_{\rm h})$ [GeV]	$rac{1}{\sigma_{ m norm}}rac{{ m d}\sigma}{{ m d}p_{ m T}(t_{ m h})}$ [GeV <sup>-1</sup> ]	$p_{\rm T}(t_{\rm h})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\mathrm{h}})}  [\mathrm{GeV}^{-1}]$
0-40	$(2.84 \pm 0.03 \pm 0.12) \times 10^{-3}$	240-280	$(7.76 \pm 0.09 \pm 0.24) \times 10^{-4}$
40-80	$(6.17 \pm 0.03 \pm 0.12) \times 10^{-3}$	280-330	$(3.95 \pm 0.05 \pm 0.14) \times 10^{-4}$
80-120	$(6.011 \pm 0.032 \pm 0.085) \times 10^{-3}$	330-380	$(1.95 \pm 0.04 \pm 0.11) \times 10^{-4}$
120-160	$(4.22 \pm 0.03 \pm 0.12) \times 10^{-3}$	380-430	$(9.46 \pm 0.26 \pm 0.61) \times 10^{-5}$
160-200	$(2.565 \pm 0.018 \pm 0.049) \times 10^{-3}$	430-500	$(4.14 \pm 0.16 \pm 0.39) \times 10^{-5}$
200-240	$(1.431 \pm 0.013 \pm 0.036) \times 10^{-3}$	500-800	$(8.9 \pm 0.4 \pm 1.2) \times 10^{-6}$

$ y(t_{\rm h}) $	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d} y(t_{\mathrm{h}}) }$	$ y(t_{\mathrm{h}}) $	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d} y(t_{\text{h}}) }$
0.0–0.2	$0.631 \pm 0.004 \pm 0.014$	1.2–1.4	$0.404 \pm 0.003 \pm 0.010$
0.2–0.4	$0.626 \pm 0.004 \pm 0.013$	1.4–1.6	$0.338 \pm 0.003 \pm 0.014$
0.4-0.6	$0.5938 \pm 0.0037 \pm 0.0091$	1.6-1.8	$0.290 \pm 0.003 \pm 0.010$
0.6-0.8	$0.562 \pm 0.004 \pm 0.015$	1.8-2.0	$0.230 \pm 0.003 \pm 0.011$
0.8-1.0	$0.5072 \pm 0.0035 \pm 0.0090$	2.0-2.5	$0.1424 \pm 0.0026 \pm 0.0072$
1.0-1.2	$0.4615 \pm 0.0034 \pm 0.0064$		

TABLE XXXVIII. Differential cross section at the parton level as a function of  $|y(t_h)|$  normalized to the cross section  $\sigma_{norm}$  in the measured range. The values are shown together with their statistical and systematic uncertainties.

TABLE XXXIX. Differential cross section at the parton level as a function of  $p_{\rm T}(t\bar{t})$  normalized to the cross section  $\sigma_{\rm norm}$  in the measured range. The values are shown together with their statistical and systematic uncertainties.

$p_{\rm T}(t\bar{t})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t\overline{t})} \ [\mathrm{GeV}^{-1}]$	$p_{\mathrm{T}}(t\bar{t})$ [GeV]	$\frac{1}{\sigma_{\text{nom}}} \frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t\overline{t})}  \left[\mathrm{GeV}^{-1}\right]$
0-40	$0.01227 \pm 0.00007 \pm 0.00039$	220-300	$(3.26 \pm 0.08 \pm 0.24) \times 10^{-4}$
40-80	$(6.11 \pm 0.08 \pm 0.35) \times 10^{-3}$	300-380	$(1.111 \pm 0.047 \pm 0.086) \times 10^{-4}$
80-150	$(2.371 \pm 0.026 \pm 0.082) \times 10^{-3}$	380-500	$(4.22 \pm 0.18 \pm 0.31) \times 10^{-5}$
150-220	$(8.07 \pm 0.15 \pm 0.29) \times 10^{-4}$	500-1000	$(4.99 \pm 0.22 \pm 0.33) \times 10^{-6}$

TABLE XL. Differential cross section at the parton level as a function of  $|y(t\bar{t})|$  normalized to the cross section  $\sigma_{\text{norm}}$  in the measured range. The values are shown together with their statistical and systematic uncertainties.

$ y(t\bar{t}) $	$\frac{1}{\sigma_{\mathrm{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d} y(t\tilde{t}) }$	$ y(t\bar{t}) $	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d} y(t\overline{t}) }$
0.0-0.2	$0.740 \pm 0.005 \pm 0.012$	1.0–1.2	$0.451 \pm 0.005 \pm 0.012$
0.2–0.4	$0.719 \pm 0.006 \pm 0.016$	1.2–1.4	$0.386 \pm 0.005 \pm 0.010$
0.4-0.6	$0.674 \pm 0.005 \pm 0.018$	1.4–1.6	$0.305 \pm 0.006 \pm 0.015$
0.6-0.8	$0.620 \pm 0.005 \pm 0.019$	1.6–1.8	$0.217 \pm 0.006 \pm 0.023$
0.8–1.0	$0.549 \pm 0.005 \pm 0.012$	1.8–2.4	$0.1129 \pm 0.0043 \pm 0.0098$

TABLE XLI. Differential cross section at the parton level as a function of  $M(t\bar{t})$  normalized to the cross section  $\sigma_{\text{norm}}$  in the measured range. The values are shown together with their statistical and systematic uncertainties.

$M(t\bar{t})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}M(t\bar{t})}  \left[\mathrm{GeV}^{-1}\right]$	$M(t\bar{t})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}M(t\bar{t})}  [\mathrm{GeV}^{-1}]$
300-360	$(1.03 \pm 0.03 \pm 0.27) \times 10^{-3}$	680-800	$(5.18 \pm 0.09 \pm 0.24) \times 10^{-4}$
360-430	$(4.50 \pm 0.04 \pm 0.14) \times 10^{-3}$	800-1000	$(1.98 \pm 0.04 \pm 0.11) \times 10^{-4}$
430-500	$(3.29 \pm 0.03 \pm 0.13) \times 10^{-3}$	1000-1200	$(6.77 \pm 0.24 \pm 0.34) \times 10^{-5}$
500-580	$(2.016 \pm 0.025 \pm 0.056) \times 10^{-3}$	1200-1500	$(2.02 \pm 0.11 \pm 0.17) \times 10^{-5}$
580-680	$(1.084 \pm 0.015 \pm 0.037) \times 10^{-3}$	1500-2500	$(2.56 \pm 0.21 \pm 0.50) \times 10^{-6}$

TABLE XLII. Double-differential cross section at the parton level as a function of  $|y(t_h)|$  vs.  $p_T(t_h)$  normalized to the cross section  $\sigma_{\text{norm}}$  in the measured in the two-dimensional range. The values are shown together with their statistical and systematic uncertainties.

$p_{\rm T}(t_{\rm h})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}^2 \sigma}{\mathrm{d}  y(t_h)  \mathrm{d} p_{\mathrm{T}}(t_h)} [\mathrm{GeV}^{-1}]$	$p_{\rm T}(t_{\rm h})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{d^2 \sigma}{d y(t_h)  dp_{\text{T}}(t_h)} \ [\text{GeV}^{-1}]$
	0 <  y(t)	$  _{h} = 0.5$	
0–40	$(1.628 \pm 0.018 \pm 0.063) \times 10^{-3}$	240–280	$(5.44 \pm 0.07 \pm 0.19)  imes 10^{-4}$
40-80	$(3.63 \pm 0.02 \pm 0.10) \times 10^{-3}$	280-330	$(2.85 \pm 0.05 \pm 0.12) \times 10^{-4}$
80-120	$(3.669 \pm 0.024 \pm 0.085) \times 10^{-3}$	330-380	$(1.462 \pm 0.034 \pm 0.081) \times 10^{-4}$
120-160	$(2.653 \pm 0.019 \pm 0.071) \times 10^{-3}$	380-450	$(6.40 \pm 0.21 \pm 0.56) \times 10^{-5}$
160-200	$(1.679 \pm 0.015 \pm 0.038) \times 10^{-3}$	450-800	$(1.11 \pm 0.05 \pm 0.10) \times 10^{-5}$
200-240	$(9.62 \pm 0.10 \pm 0.33) \times 10^{-4}$		· · · · · · · · · · · · · · · · · · ·

#### TABLE XLII. (Continued)

$p_{\rm T}(t_{\rm h})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{d^2 \sigma}{d y(t_h)  dp_{\text{T}}(t_h)} [\text{GeV}^{-1}]$	$p_{\rm T}(t_{\rm h})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{d^2 \sigma}{d y(t_h) dp_T(t_h)} [\text{GeV}^{-1}]$
	0.5 <  y	$(t_{\rm h})  < 1$	
0–40	$(1.440 \pm 0.017 \pm 0.072) \times 10^{-3}$	240–280	$(4.52 \pm 0.07 \pm 0.23) \times 10^{-4}$
40-80	$(3.239 \pm 0.024 \pm 0.089) \times 10^{-3}$	280-330	$(2.397 \pm 0.044 \pm 0.094) \times 10^{-4}$
80-120	$(3.266 \pm 0.023 \pm 0.054) \times 10^{-3}$	330-380	$(1.224 \pm 0.031 \pm 0.086) \times 10^{-4}$
120-160	$(2.339 \pm 0.019 \pm 0.081) \times 10^{-3}$	380-450	$(5.60 \pm 0.20 \pm 0.54) \times 10^{-5}$
160-200	$(1.426 \pm 0.014 \pm 0.039) \times 10^{-3}$	450-800	$(7.57 \pm 0.42 \pm 0.78)  imes 10^{-6}$
200-240	$(8.17 \pm 0.10 \pm 0.36) \times 10^{-4}$		····
	$1 <  y(t_{1}) $	< 1.5	
0-40	$(1.147 \pm 0.016 \pm 0.064) \times 10^{-3}$	240–280	$(3.28 \pm 0.06 \pm 0.14) \times 10^{-4}$
40-80	$(2.574 \pm 0.023 \pm 0.074) \times 10^{-3}$	280-330	$(1.631 \pm 0.037 \pm 0.083) \times 10^{-4}$
80-120	$(2.487 \pm 0.022 \pm 0.065) \times 10^{-3}$	330-380	$(7.52 \pm 0.24 \pm 0.49) \times 10^{-5}$
120-160	$(1.765 \pm 0.017 \pm 0.065) \times 10^{-3}$	380-450	$(3.26 \pm 0.15 \pm 0.28) \times 10^{-5}$
160-200	$(1.074 \pm 0.012 \pm 0.033) \times 10^{-3}$	450-800	$(5.01 \pm 0.35 \pm 0.82) \times 10^{-6}$
200-240	$(6.11 \pm 0.09 \pm 0.18) \times 10^{-4}$		····
	1.5 <  y	$ t_{\rm h}   < 2.5$	
0–40	$(6.41 \pm 0.12 \pm 0.45) \times 10^{-4}$	240–280	$(1.276 \pm 0.034 \pm 0.099) \times 10^{-4}$
40-80	$(1.356 \pm 0.016 \pm 0.055) \times 10^{-3}$	280-330	$(6.15 \pm 0.20 \pm 0.52) \times 10^{-5}$
80-120	$(1.317 \pm 0.015 \pm 0.051) \times 10^{-3}$	330-380	$(2.55 \pm 0.12 \pm 0.41) \times 10^{-5}$
120-160	$(9.14 \pm 0.12 \pm 0.56) \times 10^{-4}$	380-450	$(1.00 \pm 0.07 \pm 0.18) \times 10^{-5}$
160-200	$(5.06 \pm 0.08 \pm 0.31) \times 10^{-4}$	450-800	$(1.12 \pm 0.13 \pm 0.21) \times 10^{-6}$
200-240	$(2.54 \pm 0.05 \pm 0.14) \times 10^{-4}$		

TABLE XLIII. Double-differential cross section at the parton level as a function of  $M(t\bar{t})$  vs.  $|y(t\bar{t})|$  normalized to the cross section  $\sigma_{\text{norm}}$  in the measured in the two-dimensional range. The values are shown together with their statistical and systematic uncertainties.

$ y(t\overline{t}) $	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}^2 \sigma}{\mathrm{d} M(t\bar{t}) \mathrm{d}  y(t\bar{t}) } \ [\text{GeV}^{-1}]$	$ y(t\overline{t}) $	$\frac{1}{\sigma_{\text{norm}}} \frac{d^2 \sigma}{dM(t\bar{t}) d y(t\bar{t}) } \ [\text{GeV}^{-1}]$
	300 < M(	$(t\bar{t}) < 450$	
0.0-0.2	$(2.024 \pm 0.019 \pm 0.075) \times 10^{-3}$	1.0–1.2	$(1.383 \pm 0.016 \pm 0.047) \times 10^{-3}$
0.2-0.4	$(1.968 \pm 0.015 \pm 0.067) \times 10^{-3}$	1.2-1.4	$(1.208 \pm 0.016 \pm 0.049) \times 10^{-3}$
0.4–0.6	$(1.886 \pm 0.016 \pm 0.060) \times 10^{-3}$	1.4-1.6	$(1.020 \pm 0.016 \pm 0.048) \times 10^{-3}$
0.6-0.8	$(1.799 \pm 0.016 \pm 0.070) \times 10^{-3}$	1.6-2.4	$(5.47 \pm 0.12 \pm 0.41) \times 10^{-4}$
0.8-1.0	$(1.620 \pm 0.016 \pm 0.060) \times 10^{-3}$		•••
	450 < M(	$(t\bar{t}) < 625$	
0.0-0.2	$(1.624 \pm 0.015 \pm 0.029) \times 10^{-3}$	1.0–1.2	$(9.80 \pm 0.13 \pm 0.35) \times 10^{-4}$
0.2-0.4	$(1.575 \pm 0.013 \pm 0.033) \times 10^{-3}$	1.2-1.4	$(8.30 \pm 0.13 \pm 0.33) \times 10^{-4}$
0.4-0.6	$(1.472 \pm 0.013 \pm 0.034) \times 10^{-3}$	1.4-1.6	$(6.46 \pm 0.14 \pm 0.44) \times 10^{-4}$
0.6-0.8	$(1.328 \pm 0.013 \pm 0.048) \times 10^{-3}$	1.6-2.4	$(2.58 \pm 0.07 \pm 0.27) \times 10^{-4}$
0.8–1.0	$(1.177 \pm 0.013 \pm 0.029) \times 10^{-3}$		•••
	625 < M	$(t\bar{t}) < 850$	
0.0-0.2	$(4.86 \pm 0.07 \pm 0.21)  imes 10^{-4}$	1.0–1.2	$(2.52 \pm 0.07 \pm 0.17) \times 10^{-4}$
0.2-0.4	$(4.63 \pm 0.07 \pm 0.13) \times 10^{-4}$	1.2-1.4	$(1.87 \pm 0.07 \pm 0.14) \times 10^{-4}$
0.4-0.6	$(4.27 \pm 0.07 \pm 0.24) \times 10^{-4}$	1.4-1.6	$(1.29 \pm 0.07 \pm 0.11) \times 10^{-4}$
0.6-0.8	$(3.80 \pm 0.07 \pm 0.22) \times 10^{-4}$	1.6-2.4	$(4.11 \pm 0.31 \pm 0.49) \times 10^{-5}$
0.8-1.0	$(3.24 \pm 0.07 \pm 0.16) \times 10^{-4}$		•••
	850 < M(	$(t\bar{t}) < 2000$	
0.0-0.2	$(3.94 \pm 0.09 \pm 0.23) \times 10^{-5}$	0.8–1.0	$(2.14 \pm 0.09 \pm 0.20) \times 10^{-5}$
0.2-0.4	$(4.01 \pm 0.10 \pm 0.29) \times 10^{-5}$	1.0-1.2	$(1.83 \pm 0.10 \pm 0.18) \times 10^{-5}$
0.4-0.6	$(3.59 \pm 0.10 \pm 0.23) \times 10^{-5}$	1.2-1.4	$(1.16 \pm 0.10 \pm 0.25) \times 10^{-5}$
0.6–0.8	$(2.97 \pm 0.10 \pm 0.17) \times 10^{-5}$	1.4–2.4	$(1.85 \pm 0.24 \pm 0.35) \times 10^{-6}$

$\overline{M(t\overline{t}) \text{ [GeV]}}$	$\frac{1}{\sigma_{\text{norm}}} \frac{d^2 \sigma}{d y(t_h)  dM(t\bar{t})} \ [\text{GeV}^{-2}]$	$M(t\bar{t})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{d^2 \sigma}{d y(t_h)  dM(t\bar{t})} \ [\text{GeV}^{-2}]$
	$0 < p_{\mathrm{T}}($	$(t_{\rm h}) < 90$	
300-360	$(9.5 \pm 0.2 \pm 2.0) \times 10^{-6}$	580-680	$(2.69 \pm 0.06 \pm 0.16) \times 10^{-6}$
360-430	$(3.33 \pm 0.02 \pm 0.11) \times 10^{-5}$	680-800	$(1.149 \pm 0.039 \pm 0.100) \times 10^{-6}$
430-500	$(1.228 \pm 0.015 \pm 0.092) \times 10^{-5}$	800-1000	$(3.95 \pm 0.21 \pm 0.64) \times 10^{-7}$
500-580	$(5.65 \pm 0.09 \pm 0.31) \times 10^{-6}$	1000-2000	$(4.7 \pm 0.6 \pm 1.4) \times 10^{-8}$
	$90 < p_{\rm T}$	$t_{\rm h}) < 180$	
300-360	$(7.6 \pm 0.3 \pm 1.3) \times 10^{-7}$	580-680	$(4.72 \pm 0.07 \pm 0.30) \times 10^{-6}$
360-430	$(1.604 \pm 0.017 \pm 0.063) \times 10^{-5}$	680-800	$(2.02 \pm 0.05 \pm 0.17) \times 10^{-6}$
430-500	$(2.157 \pm 0.018 \pm 0.074) \times 10^{-5}$	800-1000	$(7.08 \pm 0.25 \pm 0.51) \times 10^{-7}$
500-580	$(1.068 \pm 0.011 \pm 0.042) \times 10^{-5}$	1000-2000	$(7.0 \pm 0.5 \pm 1.5) \times 10^{-8}$
	$180 < p_{\rm T}$	$(t_{\rm h}) < 270$	
300-430	$(4.3 \pm 0.2 \pm 1.1) \times 10^{-7}$	680–800	$(1.595 \pm 0.035 \pm 0.090) \times 10^{-6}$
430-500	$(2.364 \pm 0.058 \pm 0.094) \times 10^{-6}$	800-1000	$(5.53 \pm 0.17 \pm 0.46) \times 10^{-7}$
500-580	$(5.48 \pm 0.07 \pm 0.27) \times 10^{-6}$	1000-1200	$(1.80 \pm 0.11 \pm 0.26) \times 10^{-7}$
580-680	$(3.86 \pm 0.05 \pm 0.18) \times 10^{-6}$	1200-2000	$(2.16 \pm 0.24 \pm 0.59) \times 10^{-8}$
	$270 < p_{\rm T}$	$(t_{\rm h}) < 800$	
300-430	$(1.30 \pm 0.16 \pm 0.45) \times 10^{-8}$	680–800	$(1.91 \pm 0.04 \pm 0.12) \times 10^{-7}$
430-500	$(5.81 \pm 0.36 \pm 0.95) \times 10^{-8}$	800-1000	$(1.070 \pm 0.022 \pm 0.062) \times 10^{-7}$
500-580	$(8.1 \pm 0.4 \pm 1.2) \times 10^{-8}$	1000-1200	$(4.24 \pm 0.16 \pm 0.35) \times 10^{-8}$
580-680	$(1.48 \pm 0.04 \pm 0.11) \times 10^{-7}$	1200-2000	$(8.32 \pm 0.32 \pm 0.75) \times 10^{-9}$

TABLE XLIV. Double-differential cross section at the parton level as a function of  $p_T(t_h)$  vs.  $M(t\bar{t})$  normalized to the cross section  $\sigma_{norm}$  in the measured in the two-dimensional range. The values are shown together with their statistical and systematic uncertainties.

### APPENDIX D: TABLES OF NORMALIZED PARTICLE-LEVEL CROSS SECTIONS

The measured normalized differential cross sections at the particle level as a function of all the measured variables are listed in Tables XLV–LXII. The results are shown together with their statistical and systematic uncertainties.

TABLE XLV.	Differential	cross secti	on at the	particle	level	l as a	function	of	$p_{\rm T}(t_{\rm h})$	) normali	zed	to the	e cross	section	$\sigma_{ m norm}$	in t	he
measured range	. The values	are shown	together	with th	eir sta	atistica	and system	sten	natic u	incertaint	ies.						

$p_{\rm T}(t_{\rm h})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\mathrm{h}})}  [\mathrm{GeV}^{-1}]$	$p_{\rm T}(t_{\rm h})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\mathrm{h}})}   [\mathrm{GeV}^{-1}]$
0-40	$(2.397 \pm 0.018 \pm 0.074) \times 10^{-3}$	240-280	$(1.027 \pm 0.010 \pm 0.021) \times 10^{-3}$
40-80	$(5.508 \pm 0.024 \pm 0.099) \times 10^{-3}$	280-330	$(5.73 \pm 0.07 \pm 0.19) \times 10^{-4}$
80-120	$(5.735 \pm 0.025 \pm 0.074) \times 10^{-3}$	330-380	$(3.00 \pm 0.05 \pm 0.12) \times 10^{-4}$
120-160	$(4.322 \pm 0.022 \pm 0.069) \times 10^{-3}$	380-430	$(1.520 \pm 0.035 \pm 0.075) \times 10^{-4}$
160-200	$(2.816 \pm 0.017 \pm 0.041) \times 10^{-3}$	430–500	$(6.80 \pm 0.22 \pm 0.41) \times 10^{-5}$
200-240	$(1.707 \pm 0.013 \pm 0.038) \times 10^{-3}$	500-800	$(1.19 \pm 0.05 \pm 0.15) \times 10^{-5}$

TABLE XLVI. Differential cross section at the particle level as a function of  $|y(t_h)|$  normalized to the cross section  $\sigma_{norm}$  in the measured range. The values are shown together with their statistical and systematic uncertainties.

$ y(t_{\rm h}) $	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d} y(t_{\mathrm{h}}) }$	$ y(t_{\rm h}) $	$\frac{1}{\sigma_{\rm norm}} \frac{{\rm d}\sigma}{{\rm d} y(t_{\rm h}) }$
0.0-0.2	$0.777 \pm 0.003 \pm 0.012$	1.2–1.4	$0.3990 \pm 0.0026 \pm 0.0083$
0.2-0.4	$0.759 \pm 0.003 \pm 0.011$	1.4–1.6	$0.2928 \pm 0.0023 \pm 0.0096$
0.4-0.6	$0.7093 \pm 0.0033 \pm 0.0081$	1.6–1.8	$0.1924 \pm 0.0019 \pm 0.0065$
0.6-0.8	$0.6600 \pm 0.0032 \pm 0.0095$	1.8-2.0	$0.0999 \pm 0.0014 \pm 0.0041$
0.8-1.0	$0.5755 \pm 0.0030 \pm 0.0093$	2.0-2.5	$0.01485 \pm 0.00035 \pm 0.00087$
1.0-1.2	$0.4977 \pm 0.0028 \pm 0.0048$		

$p_{\mathrm{T}}(t_{\ell})$ [GeV]	$rac{1}{\sigma_{ m norm}}rac{{ m d}\sigma}{{ m d}p_{ m T}(t_\ell)}$ [GeV <sup>-1</sup> ]	$p_{\mathrm{T}}(t_{\ell})$ [GeV]	$rac{1}{\sigma_{ m norm}}rac{{ m d}\sigma}{{ m d}p_{ m T}(t_\ell)}$ [GeV <sup>-1</sup> ]
0-40	$(2.212 \pm 0.035 \pm 0.090) \times 10^{-3}$	240-280	$(1.105 \pm 0.023 \pm 0.066) \times 10^{-3}$
40-80	$(5.23 \pm 0.06 \pm 0.13) \times 10^{-3}$	280-330	$(6.33 \pm 0.14 \pm 0.29) \times 10^{-4}$
80-120	$(5.39 \pm 0.06 \pm 0.12) \times 10^{-3}$	330-380	$(3.23 \pm 0.11 \pm 0.29) \times 10^{-4}$
120-160	$(4.619 \pm 0.048 \pm 0.082) \times 10^{-3}$	380-430	$(1.63 \pm 0.09 \pm 0.23) \times 10^{-4}$
160-200	$(2.857 \pm 0.037 \pm 0.079) \times 10^{-3}$	430-500	$(8.46 \pm 0.42 \pm 0.95) \times 10^{-5}$
200-240	$(1.935 \pm 0.030 \pm 0.070) \times 10^{-3}$	500-800	$(1.43 \pm 0.05 \pm 0.13) \times 10^{-5}$

TABLE XLVII. Differential cross section at the particle level as a function of  $p_{\rm T}(t_{\ell})$  normalized to the cross section  $\sigma_{\rm norm}$  in the measured range. The values are shown together with their statistical and systematic uncertainties.

TABLE XLVIII. Differential cross section at the particle level as a function of  $|y(t_{\ell})|$  normalized to the cross section  $\sigma_{\text{norm}}$  in the measured range. The values are shown together with their statistical and systematic uncertainties.

$ y(t_{\ell}) $	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d} y(t_{\ell}) }$	$ y(t_\ell) $	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d} y(t_\ell) }$
0.0-0.2	$0.735 \pm 0.007 \pm 0.015$	1.2–1.4	$0.412 \pm 0.007 \pm 0.018$
0.2-0.4	$0.717 \pm 0.009 \pm 0.012$	1.4–1.6	$0.283 \pm 0.006 \pm 0.017$
0.4-0.6	$0.700 \pm 0.009 \pm 0.012$	1.6–1.8	$0.214 \pm 0.005 \pm 0.012$
0.6–0.8	$0.651 \pm 0.009 \pm 0.021$	1.8-2.0	$0.129 \pm 0.005 \pm 0.012$
0.8-1.0	$0.575 \pm 0.008 \pm 0.016$	2.0-2.5	$0.0344 \pm 0.0015 \pm 0.0036$
1.0-1.2	$0.499 \pm 0.008 \pm 0.012$		

TABLE XLIX. Differential cross section at the particle level as a function of  $p_{\rm T}(t\bar{t})$  normalized to the cross section  $\sigma_{\rm norm}$  in the measured range. The values are shown together with their statistical and systematic uncertainties.

$p_{\rm T}(t\bar{t})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t\tilde{t})}  [\mathrm{GeV}^{-1}]$	$p_{\rm T}(t\bar{t})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t\bar{t})}   [\mathrm{GeV}^{-1}]$
0–40	$0.01126 \pm 0.00004 \pm 0.00024$	220-300	$(3.87 \pm 0.08 \pm 0.17) \times 10^{-4}$
40-80	$(6.40 \pm 0.06 \pm 0.22) \times 10^{-3}$	300-380	$(1.407 \pm 0.049 \pm 0.088) \times 10^{-4}$
80-150	$(2.520 \pm 0.022 \pm 0.068) \times 10^{-3}$	380-500	$(5.81 \pm 0.20 \pm 0.30) \times 10^{-5}$
150-220	$(9.26 \pm 0.13 \pm 0.25) \times 10^{-4}$	500-1000	$(6.56 \pm 0.25 \pm 0.39) \times 10^{-6}$

TABLE L. Differential cross section at the particle level as a function of  $|y(t\bar{t})|$  normalized to the cross section  $\sigma_{\text{norm}}$  in the measured range. The values are shown together with their statistical and systematic uncertainties.

$ y(t\bar{t}) $	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d} y(t\bar{t}) }$	$ y(t\bar{t}) $	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d} y(t\bar{t}) }$
0.0-0.2	$0.987 \pm 0.005 \pm 0.014$	1.0-1.2	$0.4099 \pm 0.0039 \pm 0.0092$
0.2-0.4	$0.933 \pm 0.006 \pm 0.015$	1.2–1.4	$0.2799 \pm 0.0033 \pm 0.0090$
0.4-0.6	$0.839 \pm 0.005 \pm 0.014$	1.4–1.6	$0.1559 \pm 0.0026 \pm 0.0062$
0.6–0.8	$0.723 \pm 0.005 \pm 0.015$	1.6–1.8	$0.0673 \pm 0.0018 \pm 0.0062$
0.8–1.0	$0.577 \pm 0.005 \pm 0.011$	1.8–2.4	$(9.5\pm0.4\pm1.1) imes10^{-3}$

TABLE LI. Differential cross section at the particle level as a function of  $M(t\bar{t})$  normalized to the cross section  $\sigma_{\text{norm}}$  in the measured range. The values are shown together with their statistical and systematic uncertainties.

$M(t\bar{t})$ [GeV]	$\frac{1}{\sigma_{\rm nom}} \frac{{\rm d}\sigma}{{\rm d}M(t\bar{t})}   [{\rm GeV^{-1}}]$	$M(t\bar{t})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}M(t\tilde{t})}  \left[\mathrm{GeV}^{-1}\right]$
300–360	$(1.12 \pm 0.02 \pm 0.14) \times 10^{-3}$	680-800	$(8.11 \pm 0.08 \pm 0.21) \times 10^{-4}$
360-430	$(2.941 \pm 0.018 \pm 0.072) \times 10^{-3}$	800-1000	$(3.62 \pm 0.04 \pm 0.11) \times 10^{-4}$
430-500	$(2.807 \pm 0.019 \pm 0.071) \times 10^{-3}$	1000-1200	$(1.311 \pm 0.031 \pm 0.058) \times 10^{-4}$
500-580	$(2.165 \pm 0.015 \pm 0.038) \times 10^{-3}$	1200-1500	$(4.45 \pm 0.16 \pm 0.31) \times 10^{-5}$
580-680	$(1.417 \pm 0.011 \pm 0.027) \times 10^{-3}$	1500-2500	$(6.14 \pm 0.36 \pm 0.63) \times 10^{-6}$

Additional jets	$\frac{1}{\sigma_{\text{norm}}}\sigma$	Additional jets	$\frac{1}{\sigma_{\text{norm}}}\sigma$
0	$0.5586 \pm 0.0010 \pm 0.0099$	3	$0.0343 \pm 0.0005 \pm 0.0019$
1	$0.2897 \pm 0.0012 \pm 0.0043$	4	$(9.24 \pm 0.25 \pm 0.92) \times 10^{-3}$
2	$0.1046 \pm 0.0008 \pm 0.0041$	≥5	$(3.58 \pm 0.12 \pm 0.38) \times 10^{-3}$

TABLE LII. Cross sections at the particle level for different numbers of additional jets normalized to the cross section  $\sigma_{norm}$  in the measured range. The values are shown together with their statistical and systematic uncertainties.

TABLE LIII. Double-differential cross section at the particle level as a function of  $|y(t_h)|$  vs.  $p_T(t_h)$  normalized to the cross section  $\sigma_{\text{norm}}$  in the measured in the two-dimensional range. The values are shown together with their statistical and systematic uncertainties.

$p_{\rm T}(t_{\rm h})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}^2 \sigma}{\mathrm{d}   y(t_h)   \mathrm{d} p_{\mathrm{T}}(t_h)} \ [\mathrm{GeV}^{-1}]$	$p_{\rm T}(t_{\rm h})$ [GeV]	$rac{1}{\sigma_{ m norm}}rac{{ m d}^2\sigma}{{ m d} y(t_{ m h}) { m d}p_{ m T}(t_{ m h})} \; [{ m GeV^{-1}}]$
	$0 <  y(t_i) $	$ h_{\rm h}  < 0.5$	
0-40	$(1.787 \pm 0.016 \pm 0.062) \times 10^{-3}$	240–280	$(7.89 \pm 0.10 \pm 0.21) \times 10^{-4}$
40-80	$(4.16 \pm 0.02 \pm 0.11) \times 10^{-3}$	280-330	$(4.35 \pm 0.07 \pm 0.17) \times 10^{-4}$
80-120	$(4.371 \pm 0.024 \pm 0.087) \times 10^{-3}$	330-380	$(2.330 \pm 0.050 \pm 0.095) \times 10^{-4}$
120-160	$(3.261 \pm 0.021 \pm 0.063) \times 10^{-3}$	380-450	$(1.046 \pm 0.030 \pm 0.067) \times 10^{-4}$
160-200	$(2.147 \pm 0.017 \pm 0.037) \times 10^{-3}$	450-800	$(1.64 \pm 0.06 \pm 0.13) \times 10^{-5}$
200–240	$(1.288 \pm 0.013 \pm 0.036) \times 10^{-3}$		····
	0.5 <  y	$(t_{\rm h})  < 1$	
0–40	$(1.512 \pm 0.015 \pm 0.078) \times 10^{-3}$	240–280	$(6.32 \pm 0.09 \pm 0.21)  imes 10^{-4}$
40-80	$(3.525 \pm 0.022 \pm 0.068) \times 10^{-3}$	280-330	$(3.61 \pm 0.06 \pm 0.15) \times 10^{-4}$
80-120	$(3.680 \pm 0.022 \pm 0.039) \times 10^{-3}$	330-380	$(1.89 \pm 0.04 \pm 0.10) \times 10^{-4}$
120-160	$(2.748 \pm 0.019 \pm 0.076) \times 10^{-3}$	380-450	$(8.88 \pm 0.28 \pm 0.58) \times 10^{-5}$
160-200	$(1.749 \pm 0.015 \pm 0.036) \times 10^{-3}$	450-800	$(1.157 \pm 0.051 \pm 0.078) \times 10^{-5}$
200-240	$(1.059 \pm 0.011 \pm 0.040) \times 10^{-3}$		
	$1 <  y(t_{1}) $	h  < 1.5	
0–40	$(1.005 \pm 0.013 \pm 0.043) \times 10^{-3}$	240–280	$(4.30 \pm 0.07 \pm 0.19) \times 10^{-4}$
40-80	$(2.341 \pm 0.019 \pm 0.061) \times 10^{-3}$	280-330	$(2.375 \pm 0.048 \pm 0.098) \times 10^{-4}$
80-120	$(2.395 \pm 0.019 \pm 0.053) \times 10^{-3}$	330–380	$(1.182 \pm 0.034 \pm 0.070) \times 10^{-4}$
120-160	$(1.836 \pm 0.016 \pm 0.050) \times 10^{-3}$	380-450	$(5.12 \pm 0.20 \pm 0.41) \times 10^{-5}$
160-200	$(1.191 \pm 0.013 \pm 0.043) \times 10^{-3}$	450-800	$(7.4 \pm 0.4 \pm 1.0) \times 10^{-6}$
200-240	$(7.40 \pm 0.09 \pm 0.23) \times 10^{-4}$		
	1.5 <  y	$ t_{\rm h})  < 2.5$	
0–40	$(2.15 \pm 0.05 \pm 0.16) \times 10^{-4}$	240–280	$(9.96 \pm 0.25 \pm 0.74) \times 10^{-5}$
40-80	$(4.81 \pm 0.06 \pm 0.21) \times 10^{-4}$	280-330	$(5.63 \pm 0.18 \pm 0.55) \times 10^{-5}$
80-120	$(5.31 \pm 0.07 \pm 0.25)  imes 10^{-4}$	330–380	$(2.75 \pm 0.12 \pm 0.38) \times 10^{-5}$
120-160	$(4.23 \pm 0.06 \pm 0.27) \times 10^{-4}$	380-450	$(1.19 \pm 0.07 \pm 0.21) \times 10^{-5}$
160-200	$(2.74 \pm 0.04 \pm 0.15)  imes 10^{-4}$	450-800	$(1.17 \pm 0.12 \pm 0.29) \times 10^{-6}$
200-240	$(1.651 \pm 0.033 \pm 0.089) \times 10^{-4}$		

TABLE LIV. Double-differential cross section at the particle level as a function of  $M(t\bar{t})$  vs.  $|y(t\bar{t})|$  normalized to the cross section  $\sigma_{\text{norm}}$  in the measured in the two-dimensional range. The values are shown together with their statistical and systematic uncertainties.

$ y(t\bar{t}) $	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}^2 \sigma}{\mathrm{d} M(t\bar{t}) \mathrm{d}  y(t\bar{t}) }   [\text{GeV}^{-1}]$	$ y(t\overline{t}) $	$\frac{1}{\sigma_{\text{norm}}} \frac{d^2 \sigma}{dM(t\bar{t}) d y(t\bar{t}) } [\text{GeV}^{-1}]$
	300 < M(	$(t\bar{t}) < 450$	
0.0-0.2	$(1.855 \pm 0.017 \pm 0.059) \times 10^{-3}$	1.0–1.2	$(1.083 \pm 0.012 \pm 0.035) \times 10^{-3}$
0.2-0.4	$(1.800 \pm 0.013 \pm 0.050) \times 10^{-3}$	1.2-1.4	$(8.15 \pm 0.11 \pm 0.28) \times 10^{-4}$
0.4-0.6	$(1.719 \pm 0.014 \pm 0.051) \times 10^{-3}$	1.4-1.6	$(5.09 \pm 0.09 \pm 0.22) \times 10^{-4}$
0.6-0.8	$(1.611 \pm 0.014 \pm 0.068) \times 10^{-3}$	1.6-2.4	$(8.94 \pm 0.23 \pm 0.84) \times 10^{-5}$
0.8 - 1.0	$(1.378 \pm 0.013 \pm 0.049) \times 10^{-3}$		

#### TABLE LIV. (Continued)

$ y(t\bar{t}) $	$\frac{1}{\sigma_{\text{norm}}} \frac{d^2 \sigma}{dM(t\bar{t}) d y(t\bar{t}) } \ [\text{GeV}^{-1}]$	$ y(t\bar{t}) $	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}^2 \sigma}{\mathrm{d} M(t \tilde{t}) \mathrm{d}  y(t \tilde{t}) } \left[ \text{GeV}^{-1} \right]$
	450 < M	$(t\bar{t}) < 625$	
0.0-0.2	$(2.139 \pm 0.016 \pm 0.035) \times 10^{-3}$	1.0–1.2	$(9.23 \pm 0.11 \pm 0.34) \times 10^{-4}$
0.2-0.4	$(2.036 \pm 0.014 \pm 0.029) \times 10^{-3}$	1.2-1.4	$(6.13 \pm 0.09 \pm 0.24) \times 10^{-4}$
0.4-0.6	$(1.848 \pm 0.014 \pm 0.031) \times 10^{-3}$	1.4-1.6	$(3.33 \pm 0.07 \pm 0.20) \times 10^{-4}$
0.6-0.8	$(1.586 \pm 0.013 \pm 0.034) \times 10^{-3}$	1.6-2.4	$(4.47 \pm 0.14 \pm 0.44) \times 10^{-5}$
0.8–1.0	$(1.279 \pm 0.012 \pm 0.029) \times 10^{-3}$		••••
	625 < M	$(t\bar{t}) < 850$	
0.0-0.2	$(9.57 \pm 0.10 \pm 0.20) \times 10^{-4}$	1.0–1.2	$(2.92 \pm 0.06 \pm 0.13) \times 10^{-4}$
0.2-0.4	$(8.84 \pm 0.09 \pm 0.17) \times 10^{-4}$	1.2-1.4	$(1.65 \pm 0.04 \pm 0.14) \times 10^{-4}$
0.4-0.6	$(7.60 \pm 0.08 \pm 0.31) \times 10^{-4}$	1.4-1.6	$(8.00 \pm 0.32 \pm 0.52) \times 10^{-5}$
0.6-0.8	$(6.14 \pm 0.08 \pm 0.28) \times 10^{-4}$	1.6-2.4	$(1.013 \pm 0.065 \pm 0.098) \times 10^{-5}$
0.8–1.0	$(4.64 \pm 0.07 \pm 0.17) \times 10^{-4}$		
	850 < M(	$(t\bar{t}) < 2000$	
0.0-0.2	$(1.006 \pm 0.017 \pm 0.036) \times 10^{-4}$	0.8–1.0	$(3.48 \pm 0.10 \pm 0.20) \times 10^{-5}$
0.2-0.4	$(9.44 \pm 0.16 \pm 0.45) \times 10^{-5}$	1.0-1.2	$(2.12 \pm 0.08 \pm 0.13) \times 10^{-5}$
0.4-0.6	$(7.71 \pm 0.15 \pm 0.32) \times 10^{-5}$	1.2-1.4	$(1.04 \pm 0.06 \pm 0.12) \times 10^{-5}$
0.6–0.8	$(5.62 \pm 0.13 \pm 0.28) \times 10^{-5}$	1.4-2.4	$(9.2 \pm 0.9 \pm 1.5) \times 10^{-7}$

TABLE LV. Double-differential cross section at the particle level as a function of  $p_{\rm T}(t_{\rm h})$  vs.  $M(t\bar{t})$  normalized to the cross section  $\sigma_{\rm norm}$  in the measured in the two-dimensional range. The values are shown together with their statistical and systematic uncertainties.

$M(t\bar{t})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}}\frac{\mathrm{d}^2\sigma}{\mathrm{d} y(t_{\text{h}}) \mathrm{d}M(t\bar{t})}  [\text{GeV}^{-2}]$	$M(t\bar{t})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}^2 \sigma}{\mathrm{d}   y(t_{\mathrm{h}})   \mathrm{d} M(t\bar{t})}  \left[ \mathrm{GeV}^{-2} \right]$
	$0 < p_{\rm T}$	$(t_{\rm h}) < 90$	
300-360	$(1.08 \pm 0.01 \pm 0.11) \times 10^{-5}$	580-680	$(3.55 \pm 0.04 \pm 0.17) \times 10^{-6}$
360-430	$(2.090 \pm 0.012 \pm 0.050) \times 10^{-5}$	680-800	$(1.675 \pm 0.028 \pm 0.086) \times 10^{-6}$
430-500	$(1.165 \pm 0.010 \pm 0.032) \times 10^{-5}$	800-1000	$(6.21 \pm 0.16 \pm 0.45) \times 10^{-7}$
500-580	$(6.58 \pm 0.06 \pm 0.18) \times 10^{-6}$	1000-2000	$(6.1 \pm 0.3 \pm 1.0) \times 10^{-8}$
	$90 < p_{\rm T}$	$(t_{\rm h}) < 180$	
300-360	$(1.18 \pm 0.03 \pm 0.12) \times 10^{-6}$	580-680	$(6.61 \pm 0.06 \pm 0.18) \times 10^{-6}$
360-430	$(1.111 \pm 0.010 \pm 0.031) \times 10^{-5}$	680-800	$(3.32 \pm 0.04 \pm 0.17) \times 10^{-6}$
430-500	$(1.753 \pm 0.012 \pm 0.049) \times 10^{-5}$	800-1000	$(1.313 \pm 0.023 \pm 0.067) \times 10^{-6}$
500-580	$(1.221 \pm 0.009 \pm 0.031) \times 10^{-5}$	1000-2000	$(1.27 \pm 0.05 \pm 0.15) \times 10^{-7}$
	$180 < p_{\rm T}$	$(t_{\rm h}) < 270$	
300-430	$(2.85 \pm 0.13 \pm 0.63) \times 10^{-7}$	680–800	$(2.622 \pm 0.037 \pm 0.097) \times 10^{-6}$
430-500	$(1.81 \pm 0.04 \pm 0.10) \times 10^{-6}$	800-1000	$(1.102 \pm 0.021 \pm 0.061) \times 10^{-6}$
500-580	$(4.77 \pm 0.06 \pm 0.16) \times 10^{-6}$	1000-1200	$(3.82 \pm 0.14 \pm 0.34) \times 10^{-7}$
580-680	$(4.69 \pm 0.05 \pm 0.17) \times 10^{-6}$	1200-2000	$(5.56 \pm 0.35 \pm 0.83) \times 10^{-8}$
	$270 < p_{\rm T}$	$(t_{\rm h}) < 800$	
300-430	$(6.2 \pm 0.7 \pm 2.0) \times 10^{-9}$	680-800	$(2.492 \pm 0.046 \pm 0.093) \times 10^{-7}$
430-500	$(4.15 \pm 0.24 \pm 0.68) \times 10^{-8}$	800-1000	$(1.850 \pm 0.030 \pm 0.083) \times 10^{-7}$
500-580	$(7.6 \pm 0.3 \pm 1.2) \times 10^{-8}$	1000-1200	$(8.82 \pm 0.25 \pm 0.49) \times 10^{-8}$
580-680	$(1.530 \pm 0.040 \pm 0.092) \times 10^{-7}$	1200-2000	$(2.09 \pm 0.06 \pm 0.14) \times 10^{-8}$
$p_{\rm T}(t_{\rm h})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\mathrm{h}})}  [\mathrm{GeV}^{-1}]$	$p_{\rm T}(t_{\rm h})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t_{\mathrm{h}})}   [\mathrm{GeV}^{-1}]$
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	Addition	al jets: 0	
0–40	$(1.440 \pm 0.012 \pm 0.072) \times 10^{-3}$	240–280	$(4.78 \pm 0.06 \pm 0.19)  imes 10^{-4}$
40-80	$(3.261 \pm 0.016 \pm 0.090) \times 10^{-3}$	280-330	$(2.46 \pm 0.04 \pm 0.13) \times 10^{-4}$
80-120	$(3.367 \pm 0.016 \pm 0.091) \times 10^{-3}$	330–380	$(1.235 \pm 0.027 \pm 0.078) \times 10^{-4}$
120-160	$(2.455 \pm 0.014 \pm 0.051) \times 10^{-3}$	380-450	$(5.08 \pm 0.16 \pm 0.47) \times 10^{-5}$
160-200	$(1.512 \pm 0.010 \pm 0.036) \times 10^{-3}$	450-800	$(6.88 \pm 0.31 \pm 0.64) \times 10^{-6}$
200-240	$(8.57 \pm 0.08 \pm 0.34) \times 10^{-4}$		
	Addition	al jets: 1	
0–40	$(6.38 \pm 0.06 \pm 0.38)  imes 10^{-4}$	240–280	$(3.35\pm0.04\pm0.14) imes10^{-4}$
40-80	$(1.515 \pm 0.009 \pm 0.071) \times 10^{-3}$	280-330	$(1.897 \pm 0.030 \pm 0.083) \times 10^{-4}$
80-120	$(1.598 \pm 0.009 \pm 0.036) \times 10^{-3}$	330–380	$(9.43 \pm 0.21 \pm 0.66) \times 10^{-5}$
120-160	$(1.251 \pm 0.008 \pm 0.029) \times 10^{-3}$	380-450	$(4.38 \pm 0.13 \pm 0.29) \times 10^{-5}$
160-200	$(8.44 \pm 0.07 \pm 0.22)  imes 10^{-4}$	450-800	$(6.31 \pm 0.27 \pm 0.56) \times 10^{-6}$
200-240	$(5.41 \pm 0.05 \pm 0.26) \times 10^{-4}$		
	Addition	al jets: 2	
0–40	$(2.09 \pm 0.02 \pm 0.17) \times 10^{-4}$	240-280	$(1.421 \pm 0.025 \pm 0.072) \times 10^{-4}$
40-80	$(5.08 \pm 0.04 \pm 0.23) \times 10^{-4}$	280-330	$(8.82\pm0.18\pm0.65) imes10^{-5}$
80-120	$(5.58 \pm 0.04 \pm 0.25)  imes 10^{-4}$	330–380	$(4.96 \pm 0.14 \pm 0.38)  imes 10^{-5}$
120-160	$(4.47 \pm 0.04 \pm 0.24)  imes 10^{-4}$	380-450	$(2.34 \pm 0.09 \pm 0.15)  imes 10^{-5}$
160-200	$(3.23 \pm 0.04 \pm 0.15) \times 10^{-4}$	450-800	$(3.18 \pm 0.18 \pm 0.31)  imes 10^{-6}$
200-240	$(2.16 \pm 0.03 \pm 0.15) \times 10^{-4}$		
	Additiona	al jets: ≥3	
0–40	$(8.52 \pm 0.14 \pm 0.55) \times 10^{-5}$	240–280	$(6.99 \pm 0.16 \pm 0.70)  imes 10^{-5}$
40-80	$(2.07 \pm 0.03 \pm 0.17) \times 10^{-4}$	280-330	$(4.83 \pm 0.13 \pm 0.50) \times 10^{-5}$
80-120	$(2.28 \pm 0.03 \pm 0.15) \times 10^{-4}$	330-380	$(3.03 \pm 0.11 \pm 0.27) \times 10^{-5}$
120-160	$(1.90 \pm 0.02 \pm 0.14)  imes 10^{-4}$	380-450	$(1.59\pm0.07\pm0.14) imes10^{-5}$
160-200	$(1.40 \pm 0.02 \pm 0.11)  imes 10^{-4}$	450-800	$(2.38 \pm 0.15 \pm 0.34)  imes 10^{-6}$
200-240	$(9.84 \pm 0.19 \pm 0.73)  imes 10^{-5}$		•••

TABLE LVI. Differential cross sections at the particle level as a function of  $p_{\rm T}(t_{\rm h})$  for different numbers of additional jets normalized to the sum of the cross sections  $\sigma_{\rm norm}$  in the measured ranges. The values are shown together with their statistical and systematic uncertainties.

TABLE LVII. Differential cross sections at the particle level as a function of  $p_T(t\bar{t})$  for different numbers of additional jets normalized to the sum of the cross sections  $\sigma_{norm}$  in the measured ranges. The values are shown together with their statistical and systematic uncertainties.

$p_{\rm T}(t\bar{t})$ [GeV]	$rac{1}{\sigma_{ m norm}}rac{{ m d}\sigma}{{ m d}p_{ m T}(tar t)}$ [GeV <sup>-1</sup> ]	$p_{\rm T}(t\bar{t})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{d\sigma}{dp_{\text{T}}(t\bar{t})} [\text{GeV}^{-1}]$
	Addition	nal jets: 0	
0-40	$(9.77 \pm 0.04 \pm 0.22) \times 10^{-3}$	150-220	$(7.1 \pm 0.4 \pm 1.0) \times 10^{-5}$
40-80	$(3.18 \pm 0.04 \pm 0.26) \times 10^{-3}$	220-300	$(1.05 \pm 0.15 \pm 0.30) \times 10^{-5}$
80–150	$(4.77 \pm 0.11 \pm 0.37) \times 10^{-4}$	300-1000	$(3.7 \pm 0.7 \pm 1.1) \times 10^{-7}$
	Addition	nal jets: 1	
0–40	$(1.166 \pm 0.022 \pm 0.097) \times 10^{-3}$	220-300	$(1.533 \pm 0.050 \pm 0.097) \times 10^{-4}$
40-80	$(2.531 \pm 0.027 \pm 0.074) \times 10^{-3}$	300-380	$(5.71 \pm 0.30 \pm 0.93) \times 10^{-5}$
80-150	$(1.292 \pm 0.016 \pm 0.024) \times 10^{-3}$	380-1000	$(6.36 \pm 0.27 \pm 0.44) \times 10^{-6}$
150-220	$(4.50 \pm 0.09 \pm 0.16) \times 10^{-4}$		····
	Addition	nal jets: 2	
0–40	$(2.47 \pm 0.10 \pm 0.37) \times 10^{-4}$	220-300	$(1.336 \pm 0.048 \pm 0.098) \times 10^{-4}$
40-80	$(5.39 \pm 0.12 \pm 0.37) \times 10^{-4}$	300-380	$(4.80 \pm 0.30 \pm 0.92) \times 10^{-5}$
80-150	$(5.26 \pm 0.10 \pm 0.32) \times 10^{-4}$	380-500	$(1.87 \pm 0.13 \pm 0.18) \times 10^{-5}$
150-220	$(2.65 \pm 0.08 \pm 0.17) \times 10^{-4}$	500-1000	$(1.75 \pm 0.18 \pm 0.25) \times 10^{-6}$

## TABLE LVII. (Continued)

$p_{\rm T}(t\bar{t})$ [GeV]	$\frac{1}{\sigma_{\rm norm}} \frac{{\rm d}\sigma}{{\rm d}p_{\rm T}(t\bar{t})} [{ m GeV^{-1}}]$	$p_{\rm T}(t\bar{t})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(t\bar{t})}  [\mathrm{GeV}^{-1}]$
	Addition	nal jets: ≥3	
0–40	$(6.6 \pm 0.4 \pm 1.7) \times 10^{-5}$	220-300	$(9.3 \pm 0.4 \pm 1.1) \times 10^{-5}$
40-80	$(1.83 \pm 0.07 \pm 0.21) \times 10^{-4}$	300-380	$(3.55 \pm 0.25 \pm 0.60) \times 10^{-5}$
80-150	$(1.98 \pm 0.06 \pm 0.18) \times 10^{-4}$	380-500	$(1.71 \pm 0.12 \pm 0.28) \times 10^{-5}$
150-220	$(1.45 \pm 0.05 \pm 0.12) \times 10^{-4}$	500-1000	$(2.36 \pm 0.17 \pm 0.26) \times 10^{-6}$

TABLE LVIII. Differential cross sections at the particle level as a function of  $M(t\bar{t})$  for different numbers of additional jets normalized to the sum of the cross sections  $\sigma_{norm}$  in the measured ranges. The values are shown together with their statistical and systematic uncertainties.

$M(t\bar{t})$ [GeV]	$rac{1}{\sigma_{ m norm}}rac{{ m d}\sigma}{{ m d}M(t ilde{t})}$ [GeV <sup>-1</sup> ]	$M(t\bar{t})$ [GeV]	$\frac{1}{\sigma_{\rm norm}} \frac{{\rm d}\sigma}{{\rm d}M(t\bar{t})}   [{\rm GeV^{-1}}]$
	Addition	nal jets: 0	
300-360	$(6.43 \pm 0.09 \pm 0.78)  imes 10^{-4}$	680-800	$(4.62 \pm 0.04 \pm 0.11) \times 10^{-4}$
360-430	$(1.615 \pm 0.010 \pm 0.053) \times 10^{-3}$	800-1000	$(2.101 \pm 0.025 \pm 0.087) \times 10^{-4}$
430-500	$(1.534 \pm 0.010 \pm 0.032) \times 10^{-3}$	1000-1200	$(7.72 \pm 0.18 \pm 0.62) \times 10^{-5}$
500-580	$(1.190 \pm 0.008 \pm 0.026) \times 10^{-3}$	1200-2000	$(1.46 \pm 0.05 \pm 0.10) \times 10^{-5}$
580-680	$(7.92 \pm 0.06 \pm 0.24) \times 10^{-4}$		
	Addition	nal jets: 1	
300-360	$(3.05 \pm 0.04 \pm 0.32) \times 10^{-4}$	680-800	$(2.296 \pm 0.027 \pm 0.083) \times 10^{-4}$
360-430	$(8.79 \pm 0.07 \pm 0.32) \times 10^{-4}$	800-1000	$(9.99 \pm 0.15 \pm 0.44) \times 10^{-5}$
430-500	$(8.43 \pm 0.06 \pm 0.31) \times 10^{-4}$	1000-1200	$(3.58 \pm 0.10 \pm 0.31) \times 10^{-5}$
500-580	$(6.31 \pm 0.05 \pm 0.18) \times 10^{-4}$	1200-2000	$(5.67 \pm 0.25 \pm 0.54) \times 10^{-6}$
580-680	$(4.10 \pm 0.04 \pm 0.17) \times 10^{-4}$		
	Addition	nal jets: 2	
300-360	$(1.008 \pm 0.021 \pm 0.068) \times 10^{-4}$	680-800	$(8.24 \pm 0.15 \pm 0.59)  imes 10^{-5}$
360-430	$(3.27 \pm 0.04 \pm 0.14) \times 10^{-4}$	800-1000	$(3.59 \pm 0.09 \pm 0.17) \times 10^{-5}$
430-500	$(3.12 \pm 0.03 \pm 0.22) \times 10^{-4}$	1000-1200	$(1.25 \pm 0.05 \pm 0.12) \times 10^{-5}$
500-580	$(2.34 \pm 0.03 \pm 0.13) \times 10^{-4}$	1200-2000	$(1.99 \pm 0.13 \pm 0.26) \times 10^{-6}$
580-680	$(1.481 \pm 0.021 \pm 0.094) \times 10^{-4}$		
	Additiona	al jets: ≥3	
300-360	$(3.72 \pm 0.11 \pm 0.44) \times 10^{-5}$	680-800	$(3.67 \pm 0.09 \pm 0.44) \times 10^{-5}$
360-430	$(1.40 \pm 0.02 \pm 0.11) \times 10^{-4}$	800-1000	$(1.68 \pm 0.06 \pm 0.25) \times 10^{-5}$
430-500	$(1.42 \pm 0.02 \pm 0.12) \times 10^{-4}$	1000-1200	$(6.16 \pm 0.36 \pm 0.71) \times 10^{-6}$
500-580	$(1.050 \pm 0.017 \pm 0.082) \times 10^{-4}$	1200-2000	$(9.5 \pm 0.9 \pm 2.8) \times 10^{-7}$
580-680	$(6.73 \pm 0.13 \pm 0.62) \times 10^{-5}$		

TABLE LIX. Differential cross sections at the particle level as a function of  $p_{\rm T}(\text{jet})$  of jets normalized to the sum of the cross sections  $\sigma_{\rm norm}$  of all jets in the measured ranges. The values are shown together with their statistical and systematic uncertainties.

$p_{\rm T}({\rm jet})$ [GeV]	$rac{1}{\sigma_{ m norm}}rac{{ m d}\sigma}{{ m d}p_{ m T}({ m jet})}  [{ m GeV^{-1}}]$	$p_{\rm T}({\rm jet})$ [GeV]	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}p_{\mathrm{T}}(\mathrm{jet})}   [\mathrm{GeV}^{-1}]$
	р	$T_{T}(b_{\ell})$	
30-50	$(3.155 \pm 0.013 \pm 0.070) \times 10^{-3}$	100–150	$(7.13 \pm 0.03 \pm 0.12) \times 10^{-4}$
50-75	$(2.583 \pm 0.010 \pm 0.029) \times 10^{-3}$	150-200	$(2.221 \pm 0.021 \pm 0.070) \times 10^{-4}$
75–100	$(1.611 \pm 0.008 \pm 0.023) \times 10^{-3}$	200–350	$(3.29 \pm 0.04 \pm 0.14) \times 10^{-5}$
	р	$\mathbf{b}_{\mathrm{T}}(\mathbf{b}_{\mathrm{h}})$	
30-50	$(2.966 \pm 0.013 \pm 0.088) \times 10^{-3}$	100–150	$(7.28 \pm 0.04 \pm 0.13) \times 10^{-4}$
50-75	$(2.665 \pm 0.010 \pm 0.031) \times 10^{-3}$	150-200	$(2.211 \pm 0.022 \pm 0.067) \times 10^{-4}$
75–100	$(1.698 \pm 0.009 \pm 0.025) \times 10^{-3}$	200–350	$(3.81 \pm 0.05 \pm 0.14) \times 10^{-5}$

TABLE LIX.	(Continued)
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$p_{\rm T}({\rm jet})$ [GeV]	$rac{1}{\sigma_{ m norm}}rac{d\sigma}{dp_{ m T}( m jet)}$ [GeV <sup>-1</sup> ]	$p_{\rm T}({\rm jet})$ [GeV]	$\frac{1}{\sigma_{\rm norm}} \frac{{\rm d}\sigma}{{\rm d}p_{\rm T}({\rm jet})} \ [{\rm GeV}^{-1}]$
		$p_{\mathrm{T}}(\mathbf{j}_{W1})$	
30–50	$(2.974 \pm 0.013 \pm 0.090) \times 10^{-3}$	100–150	$(7.369 \pm 0.039 \pm 0.097) \times 10^{-4}$
50-75	$(2.987 \pm 0.011 \pm 0.034) \times 10^{-3}$	150-200	$(2.290 \pm 0.024 \pm 0.075) \times 10^{-4}$
75–100	$(1.748 \pm 0.009 \pm 0.026) \times 10^{-3}$	200–350	$(4.39 \pm 0.06 \pm 0.22) \times 10^{-5}$
		$p_{\mathrm{T}}(\mathbf{j}_{W2})$	
30-50	$(5.977 \pm 0.015 \pm 0.070) \times 10^{-3}$	75–100	$(4.23 \pm 0.04 \pm 0.12) \times 10^{-4}$
50-75	$(1.531 \pm 0.008 \pm 0.039) \times 10^{-3}$	100–250	$(3.52 \pm 0.06 \pm 0.16) \times 10^{-5}$
		$p_{\mathrm{T}}(\mathbf{j}_{1})$	
30-50	$(1.417 \pm 0.008 \pm 0.043) \times 10^{-3}$	150–175	$(2.118 \pm 0.026 \pm 0.056) \times 10^{-4}$
50-75	$(8.73 \pm 0.06 \pm 0.27) \times 10^{-4}$	175-200	$(1.491 \pm 0.021 \pm 0.042) \times 10^{-4}$
75-100	$(6.01 \pm 0.05 \pm 0.15) \times 10^{-4}$	200-250	$(9.88 \pm 0.14 \pm 0.33) \times 10^{-5}$
100-125	$(4.17 \pm 0.04 \pm 0.13) \times 10^{-4}$	250-320	$(5.01 \pm 0.08 \pm 0.21) \times 10^{-5}$
125–150	$(2.903 \pm 0.032 \pm 0.070) \times 10^{-4}$	320-500	$(1.629 \pm 0.024 \pm 0.053) \times 10^{-5}$
		$p_{\mathrm{T}}(\mathbf{j}_2)$	
30-50	$(8.50 \pm 0.06 \pm 0.42) \times 10^{-4}$	125–150	$(4.75 \pm 0.12 \pm 0.36) \times 10^{-5}$
50-75	$(3.55 \pm 0.03 \pm 0.24) \times 10^{-4}$	150-180	$(2.60 \pm 0.09 \pm 0.18) \times 10^{-5}$
75-100	$(1.73 \pm 0.02 \pm 0.12) \times 10^{-4}$	180-350	$(5.72 \pm 0.19 \pm 0.44) \times 10^{-6}$
100–125	$(8.92 \pm 0.17 \pm 0.71) \times 10^{-5}$		
		$p_{\mathrm{T}}(\mathbf{j}_3)$	
30-50	$(3.37 \pm 0.04 \pm 0.26) \times 10^{-4}$	75–100	$(3.44 \pm 0.10 \pm 0.44) \times 10^{-5}$
50-75	$(1.00 \pm 0.02 \pm 0.11) \times 10^{-4}$	100-250	$(4.68 \pm 0.17 \pm 0.55) \times 10^{-6}$
		$p_{\mathrm{T}}(\mathrm{j}_4)$	
30-50	$(1.06 \pm 0.02 \pm 0.12) \times 10^{-4}$	75–100	$(6.1 \pm 0.4 \pm 1.1) \times 10^{-6}$
50-75	$(2.32 \pm 0.08 \pm 0.36) \times 10^{-5}$	100-200	$(9.1 \pm 0.9 \pm 1.9) \times 10^{-7}$

TABLE LX.	Differential cross sections at the particle level as a function of $ \eta(jet) $ of jets normalized to the sum of the cross sections
$\sigma_{\rm norm}$ of all je	ets in the measured ranges. The values are shown together with their statistical and systematic uncertainties.

$ \eta(\text{jet}) $	$\frac{1}{\sigma_{\rm norm}} \frac{{\rm d}\sigma}{{\rm d}\eta({ m jet})}$	$ \eta(\text{jet}) $	$\frac{1}{\sigma_{ m norm}} \frac{{ m d}\sigma}{{ m d}\eta( m jet)}$
		$ \eta(\mathbf{b}_{\ell}) $	
0.00-0.25	$0.1340 \pm 0.0006 \pm 0.0014$	1.25–1.50	$0.0813 \pm 0.0005 \pm 0.0013$
0.25-0.50	$0.1313 \pm 0.0006 \pm 0.0016$	1.50-1.75	$0.06614 \pm 0.00045 \pm 0.00081$
0.50-0.75	$0.1252 \pm 0.0006 \pm 0.0016$	1.75-2.00	$0.05272 \pm 0.00042 \pm 0.00086$
0.75-1.00	$0.1134 \pm 0.0005 \pm 0.0013$	2.00-2.25	$0.03908 \pm 0.00038 \pm 0.00082$
1.00-1.25	$0.0997 \pm 0.0005 \pm 0.0011$	2.25-2.50	$0.01624 \pm 0.00028 \pm 0.00043$
		$ \eta(\mathbf{b_h}) $	
0.00-0.25	$0.1419 \pm 0.0006 \pm 0.0017$	1.25–1.50	$0.0782 \pm 0.0005 \pm 0.0013$
0.25-0.50	$0.1378 \pm 0.0006 \pm 0.0013$	1.50-1.75	$0.06182 \pm 0.00044 \pm 0.00085$
0.50-0.75	$0.1281 \pm 0.0006 \pm 0.0014$	1.75-2.00	$0.0484 \pm 0.0004 \pm 0.0014$
0.75-1.00	$0.1164 \pm 0.0006 \pm 0.0014$	2.00-2.25	$0.03451 \pm 0.00037 \pm 0.00096$
1.00-1.25	$0.0973 \pm 0.0005 \pm 0.0011$	2.25-2.50	$0.01433 \pm 0.00026 \pm 0.00054$
		$ \eta(\mathbf{j}_{W1}) $	
0.00-0.25	$0.1362 \pm 0.0006 \pm 0.0020$	1.25–1.50	$0.0806 \pm 0.0005 \pm 0.0011$
0.25-0.50	$0.1325 \pm 0.0006 \pm 0.0021$	1.50-1.75	$0.0659 \pm 0.0004 \pm 0.0014$
0.50-0.75	$0.1233 \pm 0.0006 \pm 0.0017$	1.75-2.00	$0.0523 \pm 0.0004 \pm 0.0013$
0.75-1.00	$0.1126 \pm 0.0006 \pm 0.0016$	2.00-2.25	$0.0395 \pm 0.0004 \pm 0.0013$
1.00–1.25	$0.1011 \pm 0.0005 \pm 0.0027$	2.25-2.50	$0.01786 \pm 0.00025 \pm 0.00077$

## TABLE LX. (Continued)

$ \eta(\text{jet}) $	$\frac{1}{\sigma_{\rm norm}} \frac{{ m d}\sigma}{{ m d}\eta({ m jet})}$	$ \eta(\text{jet}) $	$rac{1}{\sigma_{ m nom}}rac{{ m d}\sigma}{{ m d}\eta( m jet)}$
		$ n(\mathbf{i}_{W2}) $	
0.00-0.25	$0.1281 \pm 0.0006 \pm 0.0024$	1.25–1.50	$0.0840 \pm 0.0005 \pm 0.0011$
0.25-0.50	$0.1243 \pm 0.0006 \pm 0.0017$	1.50-1.75	$0.0704 \pm 0.0005 \pm 0.0014$
0.50-0.75	$0.1172 \pm 0.0006 \pm 0.0017$	1.75-2.00	$0.0589 \pm 0.0004 \pm 0.0011$
0.75-1.00	$0.1097 \pm 0.0006 \pm 0.0016$	2.00-2.25	$0.0474 \pm 0.0004 \pm 0.0013$
1.00-1.25	$0.0993 \pm 0.0006 \pm 0.0013$	2.25-2.50	$0.02233 \pm 0.00027 \pm 0.00088$
		$ \eta(j_1) $	
0.00-0.25	$0.0435 \pm 0.0003 \pm 0.0012$	1.25–1.50	$0.03931 \pm 0.00032 \pm 0.00090$
0.25-0.50	$0.0433 \pm 0.0003 \pm 0.0012$	1.50-1.75	$0.0374 \pm 0.0003 \pm 0.0010$
0.50-0.75	$0.04287 \pm 0.00033 \pm 0.00094$	1.75-2.00	$0.0364 \pm 0.0003 \pm 0.0013$
0.75-1.00	$0.04337 \pm 0.00034 \pm 0.00088$	2.00-2.25	$0.0326 \pm 0.0003 \pm 0.0010$
1.00-1.25	$0.0414 \pm 0.0003 \pm 0.0014$	2.25-2.50	$0.01758 \pm 0.00020 \pm 0.00057$
		$ \eta(j_2) $	
0.00-0.25	$0.0150 \pm 0.0002 \pm 0.0011$	1.25-1.50	$0.01351 \pm 0.00017 \pm 0.00071$
0.25-0.50	$0.01547 \pm 0.00019 \pm 0.00091$	1.50-1.75	$0.01310 \pm 0.00017 \pm 0.00072$
0.50-0.75	$0.0146 \pm 0.0002 \pm 0.0011$	1.75-2.00	$0.01237 \pm 0.00017 \pm 0.00079$
0.75-1.00	$0.0147 \pm 0.0002 \pm 0.0011$	2.00-2.25	$0.01112 \pm 0.00016 \pm 0.00059$
1.00-1.25	$0.01446 \pm 0.00018 \pm 0.00098$	2.25-2.50	$(6.03 \pm 0.12 \pm 0.35) \times 10^{-3}$
		$ \eta(j_3) $	
0.0-0.5	$(4.53 \pm 0.06 \pm 0.46) \times 10^{-3}$	1.5-2.0	$(3.83 \pm 0.06 \pm 0.31) \times 10^{-3}$
0.5-1.0	$(4.63 \pm 0.06 \pm 0.35) \times 10^{-3}$	2.0–2.5	$(2.55 \pm 0.05 \pm 0.22) \times 10^{-3}$
1.0–1.5	$(4.37 \pm 0.06 \pm 0.36) \times 10^{-3}$		
		$ \eta(j_4) $	
0.0-0.5	$(1.26 \pm 0.03 \pm 0.18)  imes 10^{-3}$	1.5-2.0	$(1.01 \pm 0.03 \pm 0.15) \times 10^{-3}$
0.5-1.0	$(1.29 \pm 0.03 \pm 0.15)  imes 10^{-3}$	2.0-2.5	$(6.8 \pm 0.2 \pm 1.1) \times 10^{-4}$
1.0-1.5	$(1.27 \pm 0.03 \pm 0.13) \times 10^{-3}$		

TABLE LXI. Differential cross sections at the particle level as a function of  $\Delta R_{j_t}$  of jets normalized to the sum of the cross sections  $\sigma_{\text{norm}}$  of all jets in the measured ranges. The values are shown together with their statistical and systematic uncertainties.

$\Delta R_{j_t}$	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}\Delta R_{j_{f}}}$	$\Delta R_{j_t}$	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}\Delta R_{j_t}}$
		$\Delta R_{i}(b_{\ell})$	
0.4-0.6	$0.0517 \pm 0.0005 \pm 0.0014$	1.4–1.6	$0.1026 \pm 0.0007 \pm 0.0010$
0.6-0.8	$0.0860 \pm 0.0007 \pm 0.0015$	1.6-2.0	$0.0988 \pm 0.0004 \pm 0.0012$
0.8-1.0	$0.0909 \pm 0.0007 \pm 0.0010$	2.0-2.5	$0.08080 \pm 0.00033 \pm 0.00099$
1.0-1.2	$0.0989 \pm 0.0007 \pm 0.0016$	2.5-4.5	$0.01403 \pm 0.00007 \pm 0.00021$
1.2–1.4	$0.1035 \pm 0.0007 \pm 0.0016$		
		$\Delta R_{\rm i}({\rm b_h})$	
0.4-0.6	$0.0688 \pm 0.0005 \pm 0.0012$	1.4–1.6	$0.1313 \pm 0.0007 \pm 0.0015$
0.6-0.8	$0.1152 \pm 0.0007 \pm 0.0017$	1.6–2.0	$0.0972 \pm 0.0005 \pm 0.0013$
0.8-1.0	$0.1316 \pm 0.0007 \pm 0.0019$	2.0-2.5	$0.04520 \pm 0.00031 \pm 0.00086$
1.0-1.2	$0.1454 \pm 0.0008 \pm 0.0012$	2.5-4.5	$(3.09 \pm 0.05 \pm 0.16) \times 10^{-3}$
1.2–1.4	$0.1444 \pm 0.0008 \pm 0.0019$		•••
		$\Delta R_{i}(j_{W1})$	
0.4-0.6	$0.0737 \pm 0.0006 \pm 0.0015$	1.4–1.6	$0.1265 \pm 0.0007 \pm 0.0017$
0.6-0.8	$0.1241 \pm 0.0007 \pm 0.0018$	1.6-2.0	$0.08623 \pm 0.00044 \pm 0.00098$
0.8-1.0	$0.1406 \pm 0.0007 \pm 0.0019$	2.0-2.5	$0.03957 \pm 0.00029 \pm 0.00070$
1.0-1.2	$0.1538 \pm 0.0008 \pm 0.0020$	2.5-4.5	$(4.19 \pm 0.05 \pm 0.22)  imes 10^{-3}$
1.2–1.4	$0.1468 \pm 0.0008 \pm 0.0013$		· · · · · · · · · · · · · · · · · · ·

## TABLE LXI. (Continued)

$\Delta R_{j_t}$	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}\Delta R_{j_{f}}}$	$\Delta R_{\mathrm{j}_t}$	$\frac{1}{\sigma_{ m norm}} \frac{{ m d}\sigma}{{ m d}\Delta R_{ m j_f}}$
		$\Delta R_{\rm i}$ (j <sub>W2</sub> )	
0.4-0.6	$0.0805 \pm 0.0006 \pm 0.0016$	1.4-1.6	$0.1257 \pm 0.0008 \pm 0.0019$
0.6-0.8	$0.1303 \pm 0.0008 \pm 0.0019$	1.6-2.0	$0.0836 \pm 0.0005 \pm 0.0010$
0.8-1.0	$0.1411 \pm 0.0008 \pm 0.0021$	2.0-2.5	$0.03747 \pm 0.00028 \pm 0.00060$
1.0-1.2	$0.1520 \pm 0.0008 \pm 0.0028$	2.5-4.5	$(3.94 \pm 0.05 \pm 0.15) \times 10^{-3}$
1.2–1.4	$0.1459 \pm 0.0008 \pm 0.0015$		···· /
		$\Delta R_{i}(j_{1})$	
0.4-0.6	$0.0439 \pm 0.0004 \pm 0.0012$	1.4–1.6	$0.0432 \pm 0.0004 \pm 0.0011$
0.6-0.8	$0.0566 \pm 0.0005 \pm 0.0015$	1.6-2.0	$0.03614 \pm 0.00026 \pm 0.00087$
0.8-1.0	$0.0509 \pm 0.0004 \pm 0.0013$	2.0-2.5	$0.02556 \pm 0.00019 \pm 0.00055$
1.0-1.2	$0.0490 \pm 0.0004 \pm 0.0015$	2.5-4.5	$(4.60 \pm 0.04 \pm 0.12) \times 10^{-3}$
1.2–1.4	$0.0458 \pm 0.0004 \pm 0.0015$		···· /
		$\Delta R_{\rm i}({\rm j}_2)$	
0.4-0.6	$0.01653 \pm 0.00023 \pm 0.00092$	1.4–1.6	$0.01423 \pm 0.00021 \pm 0.00072$
0.6-0.8	$0.0214 \pm 0.0003 \pm 0.0012$	1.6-2.0	$0.01189 \pm 0.00015 \pm 0.00061$
0.8-1.0	$0.01852 \pm 0.00024 \pm 0.00097$	2.0-2.5	$(7.97 \pm 0.11 \pm 0.41) \times 10^{-3}$
1.0-1.2	$0.01733 \pm 0.00023 \pm 0.00085$	2.5-4.5	$(1.459 \pm 0.023 \pm 0.079) \times 10^{-3}$
1.2–1.4	$0.01593 \pm 0.00022 \pm 0.00081$		
		$\Delta R_{\rm i}({\rm j}_3)$	
0.4-0.8	$(5.61 \pm 0.08 \pm 0.50)  imes 10^{-3}$	1.6–2.0	$(3.70 \pm 0.07 \pm 0.34) \times 10^{-3}$
0.8-1.2	$(5.41 \pm 0.08 \pm 0.39) \times 10^{-3}$	2.0-2.5	$(2.39 \pm 0.05 \pm 0.19) \times 10^{-3}$
1.2–1.6	$(4.69 \pm 0.08 \pm 0.34) \times 10^{-3}$	2.5-4.5	$(4.67 \pm 0.12 \pm 0.32) \times 10^{-4}$
		$\Delta R_{i}(j_4)$	
0.4–0.8	$(1.50 \pm 0.04 \pm 0.16) \times 10^{-3}$	1.6–2.0	$(1.01 \pm 0.03 \pm 0.15) \times 10^{-3}$
0.8-1.2	$(1.52 \pm 0.04 \pm 0.16) \times 10^{-3}$	2.0-2.5	$(6.96 \pm 0.27 \pm 0.91) \times 10^{-4}$
1.2–1.6	$(1.27 \pm 0.04 \pm 0.14) \times 10^{-3}$	2.5-4.5	$(1.27 \pm 0.06 \pm 0.16) \times 10^{-4}$

TABLE LXII. Differential cross sections at the particle level as a function of  $\Delta R_t$  of jets normalized to the sum of the cross sections  $\sigma_{\text{norm}}$  of all jets in the measured ranges. The values are shown together with their statistical and systematic uncertainties.

$\Delta R_t$	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}\Delta R_t}$	$\Delta R_t$	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}\Delta R_t}$
		$\Delta R_t(\mathbf{b}_{\ell})$	
0.0-0.3	$0.0566 \pm 0.0004 \pm 0.0022$	1.2–1.5	$0.1018 \pm 0.0005 \pm 0.0016$
0.3-0.6	$0.1208 \pm 0.0005 \pm 0.0022$	1.5-2.0	$0.0663 \pm 0.0003 \pm 0.0014$
0.6-0.9	$0.1319 \pm 0.0006 \pm 0.0014$	2.0-2.5	$0.02873 \pm 0.00022 \pm 0.00089$
0.9–1.2	$0.1208 \pm 0.0005 \pm 0.0017$	2.5-4.5	$(4.16 \pm 0.05 \pm 0.19) \times 10^{-3}$
		$\Delta R_t(\mathbf{b_h})$	
0.0-0.3	$0.0576 \pm 0.0004 \pm 0.0015$	1.2–1.5	$0.1034 \pm 0.0006 \pm 0.0014$
0.3-0.6	$0.1173 \pm 0.0006 \pm 0.0016$	1.5-2.0	$0.06910 \pm 0.00037 \pm 0.00084$
0.6-0.9	$0.1276 \pm 0.0006 \pm 0.0013$	2.0-2.5	$0.02976 \pm 0.00024 \pm 0.00077$
0.9–1.2	$0.1179 \pm 0.0006 \pm 0.0016$	2.5-4.5	$(4.21 \pm 0.05 \pm 0.13) \times 10^{-3}$
		$\Delta R_t(\mathbf{j}_{W1})$	
0.0-0.3	$0.0813 \pm 0.0005 \pm 0.0015$	1.2–1.5	$0.0847 \pm 0.0005 \pm 0.0011$
0.3-0.6	$0.1490 \pm 0.0007 \pm 0.0025$	1.5-2.0	$0.05319 \pm 0.00030 \pm 0.00094$
0.6-0.9	$0.1396 \pm 0.0007 \pm 0.0016$	2.0-2.5	$0.02405 \pm 0.00018 \pm 0.00057$
0.9–1.2	$0.1113 \pm 0.0006 \pm 0.0020$	2.5-4.5	$(3.74 \pm 0.04 \pm 0.16) \times 10^{-3}$
		$\Delta R_t(j_{W2})$	
0.0-0.3	$0.02833 \pm 0.00031 \pm 0.00085$	1.2–1.5	$0.1135 \pm 0.0006 \pm 0.0012$
0.3–0.6	$0.0842 \pm 0.0005 \pm 0.0016$	1.5-2.0	$0.08220 \pm 0.00041 \pm 0.00086$

## TABLE LXII. (Continued)

$\Delta R_t$	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}\Delta R_t}$	$\Delta R_t$	$\frac{1}{\sigma_{\text{norm}}} \frac{\mathrm{d}\sigma}{\mathrm{d}\Delta R_t}$
0.6–0.9	$0.1171 \pm 0.0006 \pm 0.0016$	2.0–2.5	$0.04091 \pm 0.00029 \pm 0.00068$
0.9–1.2	$0.1218 \pm 0.0006 \pm 0.0021$	2.5-4.5	$(7.04 \pm 0.07 \pm 0.24) \times 10^{-3}$
		$\Delta R_t(\mathbf{j}_1)$	
0.0-0.3	$(3.66 \pm 0.09 \pm 0.23) \times 10^{-3}$	1.2–1.5	$0.02904 \pm 0.00025 \pm 0.00097$
0.3-0.6	$0.01099 \pm 0.00015 \pm 0.00047$	1.5-2.0	$0.0359 \pm 0.0002 \pm 0.0011$
0.6-0.9	$0.01875 \pm 0.00020 \pm 0.00071$	2.0-2.5	$0.03657 \pm 0.00024 \pm 0.00084$
0.9–1.2	$0.02400 \pm 0.00022 \pm 0.00073$	2.5-4.5	$0.01584 \pm 0.00008 \pm 0.00038$
		$\Delta R_t(j_2)$	
0.0-0.3	$(1.52\pm0.05\pm0.12) imes10^{-3}$	1.2–1.5	$0.01172 \pm 0.00014 \pm 0.00065$
0.3-0.6	$(4.89 \pm 0.09 \pm 0.28) \times 10^{-3}$	1.5-2.0	$0.01304 \pm 0.00013 \pm 0.00070$
0.6-0.9	$(8.31 \pm 0.12 \pm 0.55) \times 10^{-3}$	2.0-2.5	$0.01203 \pm 0.00013 \pm 0.00076$
0.9–1.2	$0.01028 \pm 0.00013 \pm 0.00055$	2.5-4.5	$(4.36 \pm 0.04 \pm 0.21) \times 10^{-3}$
		$\Delta R_t(j_3)$	
0.0-0.4	$(5.71\pm0.22\pm0.82) imes10^{-4}$	1.5–2.0	$(4.04 \pm 0.06 \pm 0.33) \times 10^{-3}$
0.4-0.8	$(2.02 \pm 0.05 \pm 0.18) \times 10^{-3}$	2.0-2.5	$(3.67 \pm 0.06 \pm 0.34) \times 10^{-3}$
0.8-1.2	$(3.14 \pm 0.06 \pm 0.25) \times 10^{-3}$	2.5-4.5	$(1.288 \pm 0.021 \pm 0.099) \times 10^{-3}$
1.2–1.5	$(3.67 \pm 0.07 \pm 0.31) \times 10^{-3}$		
		$\Delta R_t(j_4)$	
0.0-0.4	$(1.35 \pm 0.09 \pm 0.26) \times 10^{-4}$	1.5–2.0	$(1.13 \pm 0.03 \pm 0.14) \times 10^{-3}$
0.4-0.8	$(5.14 \pm 0.20 \pm 0.59) \times 10^{-4}$	2.0-2.5	$(1.02 \pm 0.03 \pm 0.14) \times 10^{-3}$
0.8-1.2	$(8.60 \pm 0.28 \pm 0.93) \times 10^{-4}$	2.5-4.5	$(3.58 \pm 0.11 \pm 0.45) \times 10^{-4}$
1.2–1.5	$(1.02 \pm 0.03 \pm 0.14) \times 10^{-3}$		••••

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A. M. Sirunyan,<sup>1</sup> A. Tumasyan,<sup>1</sup> W. Adam,<sup>2</sup> F. Ambrogi,<sup>2</sup> E. Asilar,<sup>2</sup> T. Bergauer,<sup>2</sup> J. Brandstetter,<sup>2</sup> E. Brondolin,<sup>2</sup> M. Dragicevic,<sup>2</sup> J. Erö,<sup>2</sup> A. Escalante Del Valle,<sup>2</sup> M. Flechl,<sup>2</sup> M. Friedl,<sup>2</sup> R. Frühwirth,<sup>2,b</sup> V. M. Ghete,<sup>2</sup> J. Hrubec,<sup>2</sup> M. Jeitler,<sup>2,b</sup> N. Krammer,<sup>2</sup> I. Krätschmer,<sup>2</sup> D. Liko,<sup>2</sup> T. Madlener,<sup>2</sup> I. Mikulec,<sup>2</sup> N. Rad,<sup>2</sup> H. Rohringer,<sup>2</sup> J. Schieck,<sup>2,b</sup> R. Schöfbeck,<sup>2</sup> M. Spanring,<sup>2</sup> D. Spitzbart,<sup>2</sup> A. Taurok,<sup>2</sup> W. Waltenberger,<sup>2</sup> J. Wittmann,<sup>2</sup> C.-E. Wulz,<sup>2,b</sup> M. Zarucki,<sup>2</sup> V. Chekhovsky,<sup>3</sup> V. Mossolov,<sup>3</sup> J. Suarez Gonzalez,<sup>3</sup> E. A. De Wolf,<sup>4</sup> D. Di Croce,<sup>4</sup> X. Janssen,<sup>4</sup> J. Lauwers,<sup>4</sup> M. Pieters,<sup>4</sup> M. Van De Klundert,<sup>4</sup> H. Van Haevermaet,<sup>4</sup> P. Van Mechelen,<sup>4</sup> N. Van Remortel,<sup>4</sup> S. Abu Zeid,<sup>5</sup> F. Blekman,<sup>5</sup> J. D'Hondt,<sup>5</sup> I. De Bruyn,<sup>5</sup> J. De Clercq,<sup>5</sup> K. Deroover,<sup>5</sup> G. Flouris,<sup>5</sup> D. Lontkovskyi,<sup>5</sup> S. Lowette,<sup>5</sup> I. Marchesini,<sup>5</sup> S. Moortgat,<sup>5</sup> L. Moreels,<sup>5</sup> Q. Python,<sup>5</sup> K. Skovpen,<sup>5</sup> S. Tavernier,<sup>5</sup> W. Van Doninck,<sup>5</sup> P. Van Mulders,<sup>5</sup> I. Van Parijs,<sup>5</sup> D. Beghin,<sup>6</sup> B. Bilin,<sup>6</sup> H. Brun,<sup>6</sup> B. Clerbaux,<sup>6</sup> G. De Lentdecker,<sup>6</sup> H. Delannoy,<sup>6</sup> B. Dorney,<sup>6</sup> G. Fasanella,<sup>6</sup> L. Favart,<sup>6</sup> R. Goldouzian,<sup>6</sup> A. Grebenyuk,<sup>6</sup> A. K. Kalsi,<sup>6</sup> T. Lenzi,<sup>6</sup> J. Luetic,<sup>6</sup> T. Seva,<sup>6</sup> E. Starling,<sup>6</sup> C. Vander Velde,<sup>6</sup> P. Vanlaer,<sup>6</sup> D. Vannerom,<sup>6</sup> R. Yonamine,<sup>6</sup> T. Cornelis,<sup>7</sup> D. Dobur,<sup>7</sup> A. Fagot,<sup>7</sup> M. Gul,<sup>7</sup> I. Khvastunov,<sup>7,c</sup> D. Poyraz,<sup>7</sup> C. Roskas,<sup>7</sup> D. Trocino,<sup>7</sup> M. Tytgat,<sup>7</sup> W. Verbeke,<sup>7</sup> B. Vermassen,<sup>7</sup> M. Vit,<sup>7</sup> N. Zaganidis,<sup>7</sup> H. Bakhshiansohi,<sup>8</sup> O. Bondu,<sup>8</sup> S. Brochet,<sup>8</sup> G. Bruno,<sup>8</sup> C. Caputo,<sup>8</sup> A. Caudron,<sup>8</sup> P. David,<sup>8</sup> S. De Visscher,<sup>8</sup> C. Delaere,<sup>8</sup> M. Delcourt,<sup>8</sup> B. Francois,<sup>8</sup> A. Giammanco,<sup>8</sup> G. Krintiras,<sup>8</sup> V. Lemaitre,<sup>8</sup> A. Magitteri,<sup>8</sup> A. Mertens,<sup>8</sup> M. Musich,<sup>8</sup> K. Piotrzkowski,<sup>8</sup> L. Quertenmont,<sup>8</sup> A. Saggio,<sup>8</sup> M. Vidal Marono,<sup>8</sup> S. Wertz,<sup>8</sup> J. 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Fernandez Perez Tomei,<sup>11a</sup> E. M. Gregores,<sup>11b</sup> P. G. Mercadante,<sup>11b</sup> S. Anuja, C. A. Bernardes, L. Calligaris, T. R. Fernandez Perez Tomei, E. M. Gregores, P. G. Mercadante, S. F. Novaes, <sup>11a</sup> Sandra S. Padula, <sup>11a</sup> D. Romero Abad, <sup>11b</sup> J. C. Ruiz Vargas, <sup>11a</sup> A. Aleksandrov, <sup>12</sup> R. Hadjiiska, <sup>12</sup> P. Iaydjiev, <sup>12</sup> A. Marinov, <sup>12</sup> M. Misheva, <sup>12</sup> M. Rodozov, <sup>12</sup> M. Shopova, <sup>12</sup> G. Sultanov, <sup>12</sup> A. Dimitrov, <sup>13</sup> L. Litov, <sup>13</sup> B. Pavlov, <sup>13</sup> P. Petkov, <sup>13</sup> W. Fang, <sup>14,g</sup> X. Gao, <sup>14,g</sup> L. Yuan, <sup>14</sup> M. Ahmad, <sup>15</sup> J. G. Bian, <sup>15</sup> G. M. Chen, <sup>15</sup> H. S. Chen, <sup>15</sup> M. Chen, <sup>15</sup> Y. Chen, <sup>15</sup> C. H. Jiang, <sup>15</sup> D. Leggat, <sup>15</sup> H. Liao, <sup>15</sup> Z. Liu, <sup>15</sup> F. Romeo, <sup>15</sup> S. M. 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Mohammed,<sup>25,1</sup>
S. Bhowmik,<sup>26</sup> R. K. Dewanjee,<sup>26</sup> M. Kadastik,<sup>26</sup> L. Perrini,<sup>26</sup> M. Raidal,<sup>26</sup> C. Veelken,<sup>26</sup> P. Eerola,<sup>27</sup> H. Kirschenmann,<sup>27</sup> J. Pekkanen,<sup>27</sup> M. Voutilainen,<sup>27</sup> J. Havukainen,<sup>28</sup> J. K. Heikkilä,<sup>28</sup> T. Järvinen,<sup>28</sup> V. Karimäki,<sup>28</sup> R. Kinnunen,<sup>28</sup>

T. Lampén,<sup>28</sup> K. Lassila-Perini,<sup>28</sup> S. Laurila,<sup>28</sup> S. Lehti,<sup>28</sup> T. Lindén,<sup>28</sup> P. Luukka,<sup>28</sup> T. Mäenpää,<sup>28</sup> H. Siikonen,<sup>28</sup> E. Tuominen,<sup>28</sup> J. Tuominiemi,<sup>28</sup> T. Tuuva,<sup>29</sup> M. Besancon,<sup>30</sup> F. Couderc,<sup>30</sup> M. Dejardin,<sup>30</sup> D. Denegri,<sup>30</sup> J. L. Faure,<sup>30</sup> F. Ferri,<sup>30</sup> S. Ganjour,<sup>30</sup> S. Ghosh,<sup>30</sup> A. Givernaud,<sup>30</sup> P. Gras,<sup>30</sup> G. Hamel de Monchenault,<sup>30</sup> P. Jarry,<sup>30</sup> C. Leloup,<sup>30</sup> E. Locci,<sup>30</sup> M. Machet,<sup>30</sup> J. Malcles,<sup>30</sup> G. Negro,<sup>30</sup> J. Rander,<sup>30</sup> A. Rosowsky,<sup>30</sup> M. Ö. Sahin,<sup>30</sup> M. Titov,<sup>30</sup> A. Abdulsalam,<sup>31,m</sup> C. Amendola,<sup>31</sup> I. Antropov,<sup>31</sup> S. Baffioni,<sup>31</sup> F. Beaudette,<sup>31</sup> P. Busson,<sup>31</sup> L. Cadamuro,<sup>31</sup> C. Charlot,<sup>31</sup> R. Granier de Cassagnac,<sup>31</sup> M. Jo,<sup>31</sup> I. Kucher,<sup>31</sup> S. Lisniak,<sup>31</sup> A. Lobanov,<sup>31</sup> J. Martin Blanco,<sup>31</sup> M. Nguyen,<sup>31</sup> C. Ochando,<sup>31</sup> G. Ortona,<sup>31</sup> P. Paganini,<sup>31</sup> P. Pigard,<sup>31</sup> R. Salerno,<sup>31</sup> J. B. Sauvan,<sup>31</sup> Y. Sirois,<sup>31</sup> A. G. Stahl Leiton,<sup>31</sup> Y. Yilmaz,<sup>31</sup> A. Zabi,<sup>31</sup> A. Zghiche,<sup>31</sup> J.-L. Agram,<sup>32,n</sup> J. Andrea,<sup>32</sup> D. Bloch,<sup>32</sup> J.-M. Brom,<sup>32</sup> E. C. Chabert,<sup>32</sup> C. Collard,<sup>32</sup> E. Conte,<sup>32,n</sup> X. Coubez,<sup>32</sup> F. Drouhin,<sup>32,n</sup> J.-C. Fontaine,<sup>32,n</sup> D. Gelé,<sup>32</sup> U. Goerlach,<sup>32</sup> M. Jansová,<sup>32</sup> P. Juillot,<sup>32</sup> A.-C. Le Bihan,<sup>32</sup> N. Tonon,<sup>32</sup> P. Van Hove,<sup>32</sup> S. Gadrat,<sup>33</sup> S. Beauceron,<sup>34</sup> C. Bernet,<sup>34</sup> G. Boudoul,<sup>34</sup> N. Chanon,<sup>34</sup> R. Chierici,<sup>34</sup> D. Contardo,<sup>34</sup> P. Depasse,<sup>34</sup> H. El Mamouni,<sup>34</sup> J. Fay,<sup>34</sup> L. Finco,<sup>34</sup> S. Gascon,<sup>34</sup> M. Gouzevitch,<sup>34</sup> G. Grenier,<sup>34</sup> B. Ille,<sup>34</sup> F. Lagarde,<sup>34</sup> I. B. Laktineh,<sup>34</sup> H. Lattaud,<sup>34</sup> M. Lethuillier,<sup>34</sup> L. Mirabito,<sup>34</sup> A. L. Pequegnot,<sup>34</sup> S. Perries, <sup>34</sup> A. Popov, <sup>34,0</sup> V. Sordini, <sup>34</sup> M. Vander Donckt, <sup>34</sup> S. Viret, <sup>34</sup> S. Zhang, <sup>34</sup> T. Toriashvili, <sup>35,p</sup> Z. Tsamalaidze, <sup>36,i</sup> C. Autermann, <sup>37</sup> L. Feld, <sup>37</sup> M. K. Kiesel, <sup>37</sup> K. Klein, <sup>37</sup> M. Lipinski, <sup>37</sup> M. Preuten, <sup>37</sup> M. P. Rauch, <sup>37</sup> C. Schomakers, <sup>37</sup> J. Schulz,<sup>37</sup> M. Teroerde,<sup>37</sup> B. Wittmer,<sup>37</sup> V. Zhukov,<sup>37,o</sup> A. Albert,<sup>38</sup> D. Duchardt,<sup>38</sup> M. Endres,<sup>38</sup> M. Erdmann,<sup>38</sup> S. Erdweg,<sup>38</sup> T. Esch,<sup>38</sup> R. Fischer,<sup>38</sup> A. Güth,<sup>38</sup> T. Hebbeker,<sup>38</sup> C. Heidemann,<sup>38</sup> K. Hoepfner,<sup>38</sup> S. Knutzen,<sup>38</sup> M. Merschmeyer,<sup>38</sup> A. Meyer,<sup>38</sup> P. Millet,<sup>38</sup> S. Mukherjee,<sup>38</sup> T. Pook,<sup>38</sup> M. Radziej,<sup>38</sup> H. Reithler,<sup>38</sup> M. Rieger,<sup>38</sup> F. Scheuch,<sup>38</sup> D. Teyssier,<sup>38</sup> S. Thüer,<sup>38</sup> G. Flügge,<sup>39</sup> B. Kargoll,<sup>39</sup> T. Kress,<sup>39</sup> A. Künsken,<sup>39</sup> T. Müller,<sup>39</sup> A. Nehrkorn,<sup>39</sup> A. Nowack,<sup>39</sup> C. Pistone,<sup>39</sup> O. Pooth,<sup>39</sup> A. Stahl,<sup>39,q</sup> M. Aldaya Martin,<sup>40</sup> T. Arndt,<sup>40</sup> C. Asawatangtrakuldee,<sup>40</sup> K. Beernaert,<sup>40</sup> O. Behnke,<sup>40</sup> U. Behrens,<sup>40</sup> A. Bermúdez Martínez,<sup>40</sup> A. A. Bin Anuar,<sup>40</sup> K. Borras,<sup>40,r</sup> V. Botta,<sup>40</sup> A. Campbell,<sup>40</sup> P. Connor,<sup>40</sup> C. Contreras-Campana,<sup>40</sup> F. Costanza,<sup>40</sup> V. Danilov,<sup>40</sup> A. De Wit,<sup>40</sup> C. Diez Pardos,<sup>40</sup> D. Domínguez Damiani,<sup>40</sup> G. Eckerlin,<sup>40</sup> D. Eckstein,<sup>40</sup> T. Eichhorn,<sup>40</sup> A. Elwood,<sup>40</sup> E. Eren,<sup>40</sup> E. Gallo,<sup>40,s</sup> J. Garay Garcia,<sup>40</sup> A. Geiser,<sup>40</sup> J. M. Grados Luyando,<sup>40</sup> A. Grohsjean,<sup>40</sup> P. Gunnellini,<sup>40</sup> M. Guthoff,<sup>40</sup> A. Harb,<sup>40</sup> J. Hauk,<sup>40</sup> H. Jung,<sup>40</sup> M. Kasemann,<sup>40</sup> J. Keaveney,<sup>40</sup> C. Kleinwort,<sup>40</sup> J. Knolle,<sup>40</sup> I. Korol,<sup>40</sup> D. Krücker,<sup>40</sup> W. Lange,<sup>40</sup> A. Lelek,<sup>40</sup> T. Lenz,<sup>40</sup> K. Lipka,<sup>40</sup> W. Lohmann,<sup>40,t</sup> R. Mankel,<sup>40</sup> I.-A. Melzer-Pellmann,<sup>40</sup> A. B. Meyer,<sup>40</sup> M. Meyer,<sup>40</sup> M. Missiroli,<sup>40</sup> G. Mittag,<sup>40</sup> J. Mnich,<sup>40</sup> A. Mussgiller,<sup>40</sup> D. Pitzl,<sup>40</sup> A. Raspereza,<sup>40</sup> M. Savitskyi,<sup>40</sup> P. Saxena,<sup>40</sup> R. Shevchenko,<sup>40</sup> N. Stefaniuk,<sup>40</sup> H. Tholen,<sup>40</sup> G. P. Van Onsem,<sup>40</sup> R. Walsh,<sup>40</sup> Y. Wen,<sup>40</sup> K. Wichmann,<sup>40</sup> C. Wissing,<sup>40</sup> O. Zenaiev,<sup>40</sup> R. Aggleton,<sup>41</sup> S. Bein,<sup>41</sup> V. Blobel,<sup>41</sup> M. Centis Vignali,<sup>41</sup> T. Dreyer,<sup>41</sup> E. Garutti,<sup>41</sup> D. Gonzalez,<sup>41</sup> J. Haller,<sup>41</sup> A. Hinzmann,<sup>41</sup> M. Hoffmann,<sup>41</sup> A. Karavdina,<sup>41</sup> G. Kasieczka,<sup>41</sup> R. Klanner,<sup>41</sup> R. Kogler,<sup>41</sup> N. Kovalchuk,<sup>41</sup> S. Kurz,<sup>41</sup> V. Kutzner,<sup>41</sup> J. 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Mallios,<sup>46</sup> N. Manthos,<sup>46</sup> I. Papadopoulos,<sup>46</sup> E. Paradas,<sup>46</sup> J. Strologas,<sup>46</sup> F. A. Triantis,<sup>46</sup> D. Tsitsonis,<sup>46</sup> M. Csanad,<sup>47</sup> N. Filipovic,<sup>47</sup> G. Pasztor,<sup>47</sup> O. Surányi,<sup>47</sup> G. I. Veres,<sup>47</sup> G. Bencze,<sup>48</sup> C. Hajdu,<sup>48</sup> D. Horvath,<sup>48,u</sup> Á. Hunyadi,<sup>48</sup> F. Sikler,<sup>48</sup> V. Veszpremi,<sup>48</sup> G. Vesztergombi,<sup>48,a</sup> T. Á. Vámi,<sup>48</sup> N. Beni,<sup>49</sup> S. Czellar,<sup>49</sup> J. Karancsi,<sup>49,v</sup> A. Makovec,<sup>49</sup> J. Molnar,<sup>49</sup> Z. Szillasi,<sup>49</sup> M. Bartók,<sup>50,w</sup> P. Raics,<sup>50</sup> Z. L. Trocsanyi,<sup>50</sup> B. Ujvari,<sup>50</sup> S. Choudhury,<sup>51</sup> J. R. Komaragiri,<sup>51</sup> S. Bahinipati,<sup>52,x</sup> P. Mal,<sup>52</sup> K. Mandal,<sup>52</sup> A. Nayak,<sup>52,y</sup> D. K. Sahoo,<sup>52,x</sup> S. K. Swain,<sup>52</sup> S. Bansal,<sup>53</sup> S. B. Beri,<sup>53</sup> V. Bhatnagar,<sup>53</sup> S. Chauhan,<sup>53</sup> R. Chawla,<sup>53</sup> N. Dhingra,<sup>53</sup> R. Gupta,<sup>53</sup> A. Kaur,<sup>53</sup> M. Kaur,<sup>53</sup> S. Kaur,<sup>53</sup> R. Kumar,<sup>53</sup> P. Kumari,<sup>53</sup> M. Lohan,<sup>53</sup> A. Mehta,<sup>53</sup> S. Sharma,<sup>53</sup> J. B. Singh,<sup>53</sup> G. Walia,<sup>53</sup> Ashok Kumar,<sup>54</sup> Aashaq Shah,<sup>54</sup> A. Bhardwaj,<sup>54</sup> B. C. Choudhary,<sup>54</sup> R. B. Garg,<sup>54</sup> S. Keshri,<sup>54</sup> A. Kumar,<sup>54</sup> S. Malhotra,<sup>54</sup> M. Naimuddin,<sup>54</sup> K. Ranjan,<sup>54</sup> R. Sharma,<sup>54</sup> R. Bhardwaj,<sup>55,z</sup> R. Bhattacharya,<sup>55</sup> S. Bhattacharya,<sup>55</sup> U. Bhawandeep,<sup>55,z</sup> D. Bhowmik,<sup>55</sup> S. Dey,<sup>55</sup> S. Dutt,<sup>55,z</sup> S. Dutta,<sup>55</sup> S. Ghosh,<sup>55</sup> N. Majumdar,<sup>55</sup> K. Mondal,<sup>55</sup> S. Mukhopadhyay,<sup>55</sup> S. 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M. Sharan,<sup>55</sup> B. Singh,<sup>55</sup> S. Thakur,<sup>55,z</sup> P. K. Behera,<sup>56</sup> R. Chudasama,<sup>57</sup> D. Dutta,<sup>57</sup> V. Jha,<sup>57</sup> V. Kumar,<sup>57</sup> A. K. Mohanty,<sup>57,q</sup> P. K. Netrakanti,<sup>57</sup> L. M. Pant,<sup>57</sup> P. Shukla,<sup>57</sup> A. Topkar,<sup>57</sup> T. Aziz,<sup>58</sup> S. Dugad,<sup>58</sup> B. Mahakud,<sup>58</sup> S. Mitra,<sup>58</sup> G. B. Mohanty,<sup>58</sup> N. Sur,<sup>58</sup> B. Sutar,<sup>58</sup> S. Banerjee,<sup>59</sup> S. Bhattacharya,<sup>59</sup> S. Chatterjee,<sup>59</sup> P. Das,<sup>59</sup> M. Guchait,<sup>59</sup> Sa. Jain,<sup>59</sup> S. Kumar,<sup>59</sup> M. Maity,<sup>59,aa</sup> G. Majumder,<sup>59</sup> K. Mazumdar,<sup>59</sup> N. Sahoo,<sup>59</sup> T. Sarkar,<sup>59,aa</sup> N. Wickramage,<sup>59,bb</sup> S. Chauhan,<sup>60</sup> S. Dube,<sup>60</sup> V. Hegde,<sup>60</sup> A. Kapoor,<sup>60</sup> K. Kothekar,<sup>60</sup> S. Pandey,<sup>60</sup> A. Rane,<sup>60</sup> S. Sharma,<sup>60</sup> S. Chenarani,<sup>61,cc</sup> E. Eskandari Tadavani,<sup>61</sup> S. M. Etesami,<sup>61,cc</sup> M. Khakzad,<sup>61</sup> M. Mohammadi Najafabadi,<sup>61</sup> M. Naseri,<sup>61</sup> S. Paktinat Mehdiabadi,<sup>61,dd</sup> S. M. Elesanii, M. Khakzad, M. Wonaniniadi Najarabadi, M. Naseri, S. Faktinar Mendiabadi,
F. Rezaei Hosseinabadi,<sup>61</sup> B. Safarzadeh,<sup>61,ee</sup> M. Zeinali,<sup>61</sup> M. Felcini,<sup>62</sup> M. Grunewald,<sup>62</sup> M. Abbrescia,<sup>63a,63b</sup>
C. Calabria,<sup>63a,63b</sup> A. Colaleo,<sup>63a</sup> D. Creanza,<sup>63a,63c</sup> L. Cristella,<sup>63a,63b</sup> N. De Filippis,<sup>63a,63c</sup> M. De Palma,<sup>63a,63b</sup>
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G. Sguazzoni,<sup>66a</sup> D. Strom,<sup>66a</sup> L. Viliani,<sup>66a</sup> L. Benussi,<sup>67</sup> S. Bianco,<sup>67</sup> F. Fabbri,<sup>67</sup> D. Piccolo,<sup>67</sup> F. Primavera,<sup>67,q</sup>
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F. Brivio,<sup>69a,69b</sup> V. Ciriolo,<sup>69a,69b,q</sup> M. E. Dinardo,<sup>69a,69b</sup> S. Fiorendi,<sup>69a,69b</sup> S. Gennai,<sup>69a</sup> A. Ghezzi,<sup>69a,69b</sup> P. Govoni,<sup>69a,69b</sup> M. Malberti, <sup>69a,69b</sup> S. Malvezzi, <sup>69a</sup> R. A. Manzoni, <sup>69a,69b</sup> D. Menasce, <sup>69a</sup> L. Moroni, <sup>69a</sup> M. Paganoni, <sup>69a,69b</sup> K. Pauwels, <sup>69a,69b</sup> D. Pedrini, <sup>69a</sup> S. Pigazzini, <sup>69a,69b,gg</sup> S. Ragazzi, <sup>69a,69b</sup> T. Tabarelli de Fatis, <sup>69a,69b</sup> S. Buontempo, <sup>70a</sup> N. Cavallo, <sup>70a,70c</sup> S. Di Guida, <sup>70a,70d,q</sup> F. Fabozzi, <sup>70a,70c</sup> F. Fienga, <sup>70a,70b</sup> G. Galati, <sup>70a,70b</sup> A. O. M. Iorio, <sup>70a,70b</sup> W. A. Khan, <sup>70a</sup> L. Lista, <sup>70a</sup> S. Meola, <sup>70a,70d,q</sup> P. Paolucci, <sup>70a,q</sup> C. Sciacca, <sup>70a,70b</sup> F. Thyssen, <sup>70a</sup> E. Voevodina, <sup>70a,70b</sup> P. Azzi, <sup>71a</sup> N. Bacchetta, <sup>71a</sup> L. Benato, <sup>71a,71b</sup> A. Boletti, <sup>71a,71b</sup> R. Carlin, <sup>71a,71b</sup> A. Carvalho Antunes De Oliveira, <sup>71a,71b</sup> P. Checchia, <sup>71a</sup> L. Benato, Navio A. Boletti, Navio R. Carlin, Navio A. Carvalho Antunes De Oliveira, Navio P. Checchia, Navio A. Dall'Osso, <sup>71a,71b</sup> P. De Castro Manzano, <sup>71a</sup> T. Dorigo, <sup>71a</sup> U. Dosselli, <sup>71a</sup> F. Gasparini, <sup>71a,71b</sup> U. Gasparini, <sup>71a,71b</sup> A. Gozzelino, <sup>71a</sup> S. Lacaprara, <sup>71a</sup> P. Lujan, <sup>71a</sup> M. Margoni, <sup>71a,71b</sup> A. T. Meneguzzo, <sup>71a,71b</sup> N. Pozzobon, <sup>71a,71b</sup> P. Ronchese, <sup>71a,71b</sup> R. Rossin, <sup>71a,71b</sup> F. Simonetto, <sup>71a,71b</sup> A. Tiko, <sup>71a</sup> E. Torassa, <sup>71a</sup> M. Zanetti, <sup>71a,71b</sup> P. Zotto, <sup>71a,71b</sup> G. Zumerle, <sup>71a,71b</sup> A. Braghieri, <sup>72a</sup> A. Magnani, <sup>72a</sup> P. Montagna, <sup>72a,72b</sup> S. P. Ratti, <sup>72a,72b</sup> V. Re, <sup>72a</sup> M. Ressegotti, <sup>72a,72b</sup> C. Riccardi, <sup>72a,72b</sup> P. Salvini, <sup>72a</sup> I. Vai, <sup>72a,72b</sup> P. Vitulo, <sup>72a,72b</sup> L. Alunni Solestizi, <sup>73a,73b</sup> M. Biasini, <sup>73a,73b</sup> G. M. Bilei, <sup>73a</sup> C. Cecchi, <sup>73a,73b</sup> D. Ciangottini, <sup>73a,73b</sup> L. Fanò, <sup>73a,73b</sup> A. Santocchia, <sup>73a,73b</sup> D. Spiga, <sup>73a</sup> K. Androsov, <sup>74a</sup> C. Eadi, <sup>74a</sup> T. Bocceli, <sup>74a</sup> L. Bocceli, <sup>74a</sup> A. Carculi, <sup>74a</sup> C. Eadi, C. Cecchi, D. Changoluni, E. Frano, F. Eanceta, K. Leonardi, E. Manoni, C. Manovin, G. Manovaln, V. Mariani, <sup>73a,73b</sup> M. Menichelli, <sup>73a</sup> A. Rossi, <sup>73a,73b</sup> A. Santocchia, <sup>73a,73b</sup> D. Spiga, <sup>73a</sup> K. Androsov, <sup>74a</sup> P. Azzurri, <sup>74a</sup> G. Bagliesi, <sup>74a</sup> L. Bianchini, <sup>74a</sup> T. Boccali, <sup>74a</sup> L. Borrello, <sup>74a</sup> R. Castaldi, <sup>74a</sup> M. A. Ciocci, <sup>74a,74b</sup> R. Dell'Orso, <sup>74a</sup> G. Fedi, <sup>74a</sup> L. Giannini, <sup>74a,74c</sup> A. Giassi, <sup>74a</sup> M. T. Grippo, <sup>74a</sup> F. Ligabue, <sup>74a,74c</sup> T. Lomtadze, <sup>74a</sup> E. Manca, <sup>74a,74c</sup> G. Mandorli, <sup>74a,74c</sup> A. Messineo, <sup>74a,74b</sup> F. Palla, <sup>74a</sup> A. Rizzi, <sup>74a,74b</sup> P. Spagnolo, <sup>74a</sup> R. Tenchini, <sup>74a</sup> G. Tonelli, <sup>74a,74b</sup> A. Venturi, <sup>74a</sup> P. G. Verdini, <sup>74a</sup> L. Barone, <sup>75a,75b</sup> F. Cavallari, <sup>75a</sup> M. Cipriani, <sup>75a,75b</sup> P. Meridiani, <sup>75a</sup> D. Del Re, <sup>75a,75b</sup> E. Di Marco, <sup>75a,75b</sup> M. Diemoz, <sup>75a</sup> S. Gelli, <sup>75a,75b</sup> E. Longo, <sup>75a,75b</sup> B. Marzocchi, <sup>75a,75b</sup> P. Meridiani, <sup>75a</sup> G. Organtini, <sup>75a,75b</sup> F. Pandolfi, <sup>75a</sup> R. Paramatti, <sup>75a,75b</sup> F. Preiato, <sup>75a,75b</sup> S. Rahatlou, <sup>75a,75b</sup> C. Rovelli, <sup>75a</sup> F. Santanastasio, <sup>75a,75b</sup> N. Amapane, <sup>76a,76a</sup> R. Arcidiacono, <sup>76a,76c</sup> S. Argiro, <sup>76a,76b</sup> M. Costa, <sup>76a,76b</sup> R. Covarelli, <sup>75a</sup> F. Santanastasio, <sup>75a,75b</sup> N. Manpane, <sup>76a,76a</sup> R. Castello, <sup>76a,76b</sup> F. Cenna, <sup>76a,76b</sup> M. Costa, <sup>76a,76b</sup> R. Covarelli, <sup>76a,76b</sup> A. Degano, <sup>76a,76b</sup> N. Demaria, <sup>76a</sup> B. Kiani, <sup>76a,76b</sup> C. Mariotti, <sup>76a</sup> S. Maselli, <sup>76a</sup> M. Costa, <sup>76a,76b</sup> R. Covarelli, <sup>76a,76b</sup> A. Degano, <sup>76a,76b</sup> M. Monteno, <sup>76a,76c</sup> R. Sacchi, <sup>76a,76b</sup> N. Pastrone, <sup>76a</sup> M. Pelliccioni, <sup>76a</sup> G. L. Pinna Angioni, <sup>76a,76b</sup> A. Romero, <sup>76a,76b</sup> M. Ruspa, <sup>76a,76c</sup> R. Sacchi, <sup>77a,77a</sup> S. Shchelina, <sup>76a,76b</sup> A. Solano, <sup>76a,76b</sup> A. Staiano, <sup>76a</sup> S. Belforte, <sup>77a</sup> M. Casarsa, <sup>77a</sup> F. Cossutti, <sup>77a</sup> G. Della Ricca, <sup>77a,77b</sup> A. Zanetti, <sup>77a</sup> D. H. Kim, <sup>78</sup> G. N. Kim, <sup>78</sup> M. S. Kim, <sup>78</sup> J. Lee, <sup>78</sup> S. Lee, <sup>78</sup> S. W. Lee, <sup>81</sup> S. S. Moon, <sup>81</sup> Y. Doh, <sup>81</sup> S. K. Park, <sup>81</sup> Y. Go,<sup>81</sup> D. Gyun, <sup>81</sup> S. Ha,<sup>81</sup> B. Hong,<sup>81</sup> Y. Jo,<sup>81</sup> Y. Kim,<sup>81</sup>

Y. Choi,<sup>84</sup> C. Hwang,<sup>84</sup> J. Lee,<sup>84</sup> I. Yu,<sup>84</sup> V. Dudenas,<sup>85</sup> A. Juodagalvis,<sup>85</sup> J. Vaitkus,<sup>85</sup> I. Ahmed,<sup>86</sup> Z. A. Ibrahim,<sup>86</sup> M. A. B. Md Ali,<sup>86,hh</sup> F. Mohamad Idris,<sup>86,ii</sup> W. A. T. Wan Abdullah,<sup>86</sup> M. N. Yusli,<sup>86</sup> Z. Zolkapli,<sup>86</sup> R Reyes-Almanza,<sup>87</sup> G. Ramirez-Sanchez,<sup>87</sup> M. C. Duran-Osuna,<sup>87</sup> H. Castilla-Valdez,<sup>87</sup> E. De La Cruz-Burelo,<sup>87</sup> I. Heredia-De La Cruz,<sup>87,jj</sup> R. I. Rabadan-Trejo,<sup>87</sup> R. Lopez-Fernandez,<sup>87</sup> J. Mejia Guisao,<sup>87</sup> A. Sanchez-Hernandez,<sup>87</sup> S. Carrillo Moreno,<sup>88</sup> C. Oropeza Barrera,<sup>88</sup> F. Vazquez Valencia,<sup>88</sup> J. Eysermans,<sup>89</sup> I. Pedraza,<sup>89</sup> H. A. Salazar Ibarguen,<sup>89</sup> C. Uribe Estrada,<sup>89</sup> A. Morelos Pineda,<sup>90</sup> D. Krofcheck,<sup>91</sup> S. Bheesette,<sup>92</sup> P. H. Butler,<sup>92</sup> A. Ahmad,<sup>93</sup> M. Ahmad,<sup>93</sup> Q. Hassan,<sup>93</sup> H. R. Hoorani,<sup>93</sup> A. Saddique,<sup>93</sup> M. A. Shah,<sup>93</sup> M. Shoaib,<sup>93</sup> M. Waqas,<sup>93</sup> H. Bialkowska,<sup>94</sup> M. Bluj,<sup>94</sup> B. Boimska,<sup>94</sup> H. R. Hoorani, <sup>7</sup> A. Saddique, <sup>7</sup> M. A. Snan, <sup>M.</sup> Snoaib, <sup>M.</sup> waqas, <sup>H.</sup> Biaikowska, <sup>M.</sup> Biuj, <sup>B.</sup> Boiniska, T. Frueboes, <sup>94</sup> M. Górski, <sup>94</sup> M. Kazana, <sup>94</sup> K. Nawrocki, <sup>94</sup> M. Szleper, <sup>94</sup> P. Traczyk, <sup>94</sup> P. Zalewski, <sup>94</sup> K. Bunkowski, <sup>95</sup> A. Byszuk, <sup>95,kk</sup> K. Doroba, <sup>95</sup> A. Kalinowski, <sup>95</sup> M. Konecki, <sup>95</sup> J. Krolikowski, <sup>95</sup> M. Misiura, <sup>95</sup> M. Olszewski, <sup>95</sup> A. Pyskir, <sup>95</sup> M. Walczak, <sup>95</sup> P. Bargassa, <sup>96</sup> C. Beirão Da Cruz E Silva, <sup>96</sup> A. Di Francesco, <sup>96</sup> P. Faccioli, <sup>96</sup> B. Galinhas, <sup>96</sup> M. Gallinaro, <sup>96</sup> J. Hollar, <sup>96</sup> N. Leonardo, <sup>96</sup> L. Lloret Iglesias, <sup>96</sup> M. V. Nemallapudi, <sup>96</sup> J. Seixas, <sup>96</sup> G. Strong, <sup>96</sup> O. Toldaiev, <sup>96</sup> D. Vadruccio, <sup>96</sup> J. Varela,<sup>96</sup> S. Afanasiev,<sup>97</sup> P. Bunin,<sup>97</sup> M. Gavrilenko,<sup>97</sup> I. Golutvin,<sup>97</sup> I. Gorbunov,<sup>97</sup> A. Kamenev,<sup>97</sup> V. Karjavin,<sup>97</sup> A. Lanev,<sup>97</sup> A. Malakhov,<sup>97</sup> V. Matveev,<sup>97,II,mm</sup> P. Moisenz,<sup>97</sup> V. Palichik,<sup>97</sup> V. Perelygin,<sup>97</sup> S. Shmatov,<sup>97</sup> S. Shulha,<sup>97</sup>
 N. Skatchkov,<sup>97</sup> V. Smirnov,<sup>97</sup> N. Voytishin,<sup>97</sup> A. Zarubin,<sup>97</sup> Y. Ivanov,<sup>98</sup> V. Kim,<sup>98,m</sup> E. Kuznetsova,<sup>98,00</sup> P. Levchenko,<sup>98</sup>
 V. Murzin,<sup>98</sup> V. Oreshkin,<sup>98</sup> I. Smirnov,<sup>98</sup> D. Sosnov,<sup>98</sup> V. Sulimov,<sup>98</sup> L. Uvarov,<sup>98</sup> S. Vavilov,<sup>98</sup> A. Vorobyev,<sup>98</sup> Yu. Andreev,<sup>99</sup> A. Dermenev,<sup>99</sup> S. Gninenko,<sup>99</sup> N. Golubev,<sup>99</sup> A. Karneyeu,<sup>99</sup> M. Kirsanov,<sup>99</sup> N. Krasnikov,<sup>99</sup> A. Pashenkov,<sup>99</sup> D. Tlisov,<sup>99</sup> A. Toropin,<sup>99</sup> V. Epshteyn,<sup>100</sup> V. Gavrilov,<sup>100</sup> N. Lychkovskaya,<sup>100</sup> V. Popov,<sup>100</sup> I. Pozdnyakov,<sup>100</sup> G. Safronov,<sup>100</sup> A. Spiridonov,<sup>100</sup> A. Stepennov,<sup>100</sup> V. Stolin,<sup>100</sup> M. Toms,<sup>100</sup> E. Vlasov,<sup>100</sup> A. Zhokin,<sup>100</sup> I. Pozdnyakov, <sup>100</sup> G. Safronov, <sup>100</sup> A. Spiridonov, <sup>100</sup> A. Stepennov, <sup>100</sup> V. Stolin, <sup>100</sup> M. Toms, <sup>100</sup> E. Vlasov, <sup>100</sup> A. Zhokin, <sup>100</sup> T. Aushev, <sup>101</sup> A. Bylinkin, <sup>101,mm</sup> R. Chistov, <sup>102,pp</sup> M. Danilov, <sup>102,pp</sup> P. Parygin, <sup>102</sup> D. Philippov, <sup>102</sup> S. Polikarpov, <sup>102</sup> E. Tarkovskii, <sup>102</sup> V. Andreev, <sup>103</sup> M. Azarkin, <sup>103,mm</sup> I. Dremin, <sup>103,mm</sup> M. Kirakosyan, <sup>103,mm</sup> S. V. Rusakov, <sup>103</sup> A. Terkulov, <sup>103</sup> A. Baskakov, <sup>104</sup> A. Belyaev, <sup>104</sup> E. Boos, <sup>104</sup> V. Bunichev, <sup>104</sup> M. Dubinin, <sup>104,qq</sup> L. Dudko, <sup>104</sup> V. Klyukhin, <sup>104</sup> O. Kodolova, <sup>104</sup> N. Korneeva, <sup>104</sup> I. Lokhtin, <sup>104</sup> I. Miagkov, <sup>104</sup> S. Obraztsov, <sup>104</sup> M. Perfilov, <sup>104</sup> V. Savrin, <sup>104</sup> P. Volkov, <sup>104</sup> V. Blinov, <sup>105,rr</sup> D. Shtol, <sup>105,rr</sup> Y. Skovpen, <sup>105,rr</sup> I. Azhgirey, <sup>106</sup> I. Bayshev, <sup>106</sup> S. Bitioukov, <sup>106</sup> D. Elumakhov, <sup>106</sup> A. Godizov, <sup>106</sup> V. Kachanov, <sup>106</sup> A. Kalinin, <sup>106</sup> D. Konstantinov, <sup>106</sup> P. Mandrik, <sup>106</sup> V. Petrov, <sup>106</sup> R. Ryutin, <sup>106</sup> A. Sobol, <sup>106</sup> S. Troshin, <sup>106</sup> N. Tyurin, <sup>106</sup> A. Uzunian, <sup>106</sup> A. Volkov, <sup>106</sup> A. Babaev, <sup>107</sup> P. Adzic, <sup>108,ss</sup> P. Cirkovic, <sup>108</sup> D. Devetak, <sup>108</sup> M. Dordevic, <sup>108</sup> J. Alcaraz Maestre, <sup>109</sup> I. Bachiller, <sup>109</sup> M. Barrio Luna, <sup>109</sup> M. Cerrada, <sup>109</sup> N. Colino, <sup>109</sup> B. De La Cruz, <sup>109</sup> A. Dalagda Baris, <sup>109</sup> C. Fargendag Padaga <sup>109</sup> L. P. Fargéndag Pagaga <sup>109</sup> L. Fliv, <sup>109</sup> M. C. Fauglaga Lapaga <sup>109</sup> P. Cargadag Lapaga <sup>109</sup> A. Delgado Peris,<sup>109</sup> C. Fernandez Bedoya,<sup>109</sup> J. P. Fernández Ramos,<sup>109</sup> J. Flix,<sup>109</sup> M. C. Fouz,<sup>109</sup> O. Gonzalez Lopez,<sup>109</sup>
 S. Goy Lopez,<sup>109</sup> J. M. Hernandez,<sup>109</sup> M. I. Josa,<sup>109</sup> D. Moran,<sup>109</sup> A. Pérez-Calero Yzquierdo,<sup>109</sup> J. Puerta Pelayo,<sup>109</sup>
 I. Redondo,<sup>109</sup> L. Romero,<sup>109</sup> M. S. Soares,<sup>109</sup> A. Triossi,<sup>109</sup> A. Álvarez Fernández,<sup>109</sup> C. Albajar,<sup>110</sup> J. F. de Trocóniz,<sup>110</sup> I. Redondo,<sup>109</sup> L. Romero,<sup>109</sup> M. S. Soares,<sup>109</sup> A. Triossi,<sup>109</sup> A. Álvarez Fernández,<sup>109</sup> C. Albajar,<sup>110</sup> J. F. de Trocóniz,<sup>110</sup> J. Cuevas,<sup>111</sup> C. Erice,<sup>111</sup> J. Fernandez Menendez,<sup>111</sup> S. Folgueras,<sup>111</sup> I. Gonzalez Caballero,<sup>111</sup> J. R. González Fernández,<sup>111</sup> E. Palencia Cortezon,<sup>111</sup> S. Sanchez Cruz,<sup>111</sup> P. Vischia,<sup>111</sup> J. M. Vizan Garcia,<sup>111</sup> I. J. Cabrillo,<sup>112</sup> A. Calderon,<sup>112</sup> B. Chazin Quero,<sup>112</sup> J. Duarte Campderros,<sup>112</sup> M. Fernandez,<sup>112</sup> P. J. Fernández Manteca,<sup>112</sup> J. Garcia-Ferrero,<sup>112</sup> A. García Alonso,<sup>112</sup> G. Gomez,<sup>112</sup> A. Lopez Virto,<sup>112</sup> J. Marco,<sup>112</sup> C. Martinez Rivero,<sup>112</sup> P. Martinez Ruiz del Arbol,<sup>112</sup> F. Matorras,<sup>112</sup> J. Piedra Gomez,<sup>112</sup> C. Prieels,<sup>112</sup> T. Rodrigo,<sup>112</sup> A. Ruiz-Jimeno,<sup>112</sup> L. Scodellaro,<sup>112</sup> N. Trevisani,<sup>112</sup> I. Vila,<sup>112</sup> R. Vilar Cortabitarte,<sup>112</sup> D. Abbaneo,<sup>113</sup> B. Akgun,<sup>113</sup> E. Auffray,<sup>113</sup> P. Baillon,<sup>113</sup> A. H. Ball,<sup>113</sup> D. Barney,<sup>113</sup> J. Bendavid,<sup>113</sup> J. F. Benitez,<sup>113</sup> M. Bianco,<sup>113</sup> A. Bocci,<sup>113</sup> C. Botta,<sup>113</sup> T. Camporesi,<sup>113</sup> M. Cepeda,<sup>113</sup> G. Cerminara,<sup>113</sup> E. Chapon,<sup>113</sup> Y. Chen,<sup>113</sup> D. d'Enterria,<sup>113</sup> A. Dabrowski,<sup>113</sup> V. Daponte,<sup>113</sup> A. Duvid,<sup>113</sup> M. De Gruttola,<sup>113</sup> A. De Roeck,<sup>113</sup> N. Deelen,<sup>113</sup> M. Dobson,<sup>113</sup> T. du Pree,<sup>113</sup> M. Dünser,<sup>113</sup> N. Dupont,<sup>113</sup> A. Elliott-Peisert,<sup>113</sup> F. Sellavollita,<sup>113,14</sup> G. Franzoni,<sup>113</sup> J. Fulcher,<sup>113</sup> W. Funk,<sup>113</sup> D. Gigi,<sup>113</sup> A. Gilbert,<sup>113</sup> K. Gill,<sup>113</sup> F. Glege,<sup>113</sup> D. Gulhan,<sup>113</sup> J. Hegeman,<sup>113</sup> V. Innocente,<sup>113</sup> A. Jafari,<sup>113</sup> P. Janot,<sup>113</sup> O. Karacheban,<sup>113</sup> I. Kieseler,<sup>113</sup> V. Knünz,<sup>113</sup> A. Kornmayer,<sup>113</sup> M. Krammer,<sup>113,15</sup> C. Lange,<sup>113</sup> P. Janot,<sup>113</sup> C. Lourenço,<sup>113</sup> M. T. Lucchini,<sup>113</sup> L. Malgeri,<sup>113</sup> M. Mulders,<sup>113</sup> H. Neugebauer,<sup>113</sup> J. A. Merlin,<sup>113</sup> S. Mersi,<sup>113</sup> E. Meschi,<sup>113</sup> P. Milenovic,<sup>113,4</sup> I. Moortgat,<sup>113</sup> M. Peruzzi,<sup>113</sup> A. Petrilli,<sup>113</sup> G. Petrucciani,<sup>113</sup> A. Pfeiffer,<sup>113</sup> M. Pierini,<sup>113</sup> F. M. Pitters,<sup>113</sup> D. Rabady,<sup>113</sup> A. Racz,<sup>113</sup> M. Peruzzi,<sup>113</sup> A. Petrilli,<sup>113</sup> G. Petrucciani,<sup>113</sup> A. M. Mulders, H. Neugebauer, J. Ngadluba, S. Ortanelli, E. L. Orsini, F. Pantaleo, <sup>113</sup> L. Pape, <sup>115</sup> E. Perez, <sup>113</sup> M. Peruzzi, <sup>113</sup> A. Petrilli, <sup>113</sup> G. Petrucciani, <sup>113</sup> A. Pfeiffer, <sup>113</sup> M. Pierini, <sup>113</sup> F. M. Pitters, <sup>113</sup> D. Rabady, <sup>113</sup> A. Racz, <sup>113</sup> T. Reis, <sup>113</sup> G. Rolandi, <sup>113,vv</sup> M. Rovere, <sup>113</sup> H. Sakulin, <sup>113</sup> C. Schäfer, <sup>113</sup> C. Schwick, <sup>113</sup> M. Seidel, <sup>113</sup> M. Selvaggi, <sup>113</sup> A. Sharma, <sup>113</sup> P. Silva, <sup>113</sup> P. Sphicas, <sup>113,ww</sup> A. Stakia, <sup>113</sup> J. Steggemann, <sup>113</sup> M. Stoye, <sup>113</sup> M. Tosi, <sup>113</sup> D. Treille, <sup>113</sup> A. Tsirou, <sup>113</sup> V. Veckalns, <sup>113,xx</sup> M. Verweij, <sup>113</sup> W. D. Zeuner, <sup>113</sup> W. Bertl, <sup>114,a</sup> L. Caminada, <sup>114,yy</sup> K. Deiters, <sup>114</sup> W. Erdmann, <sup>114</sup> R. Horisberger, <sup>114</sup> Q. Ingram, <sup>114</sup> H. C. Kaestli, <sup>114</sup> D. Kotlinski, <sup>114</sup> U. Langenegger, <sup>114</sup> T. Rohe, <sup>114</sup> S. A. Wiederkehr, <sup>114</sup> M. Backhaus, <sup>115</sup> L. Bäni, <sup>115</sup> P. Berger, <sup>115</sup> B. Casal, <sup>115</sup> N. Chernyavskaya, <sup>115</sup> G. Dissertori, <sup>115</sup>

M. Dittmar,<sup>115</sup> M. Donegà,<sup>115</sup> C. Dorfer,<sup>115</sup> C. Grab,<sup>115</sup> C. Heidegger,<sup>115</sup> D. Hits,<sup>115</sup> J. Hoss,<sup>115</sup> T. Klijnsma,<sup>115</sup> W. Lustermann,<sup>115</sup> M. Marionneau,<sup>115</sup> M. T. Meinhard,<sup>115</sup> D. Meister,<sup>115</sup> F. Micheli,<sup>115</sup> P. Musella,<sup>115</sup> F. Nessi-Tedaldi,<sup>115</sup> W. Lustermann,<sup>115</sup> M. Marionneau,<sup>115</sup> M. T. Meinhard,<sup>115</sup> D. Meister,<sup>115</sup> F. Micheli,<sup>115</sup> P. Musella,<sup>115</sup> F. Nessi-Tedaldi,<sup>115</sup> J. Pata,<sup>115</sup> G. Perrin,<sup>115</sup> L. Perrozzi,<sup>115</sup> M. Quittnat,<sup>115</sup> M. Reichmann,<sup>115</sup> D. Ruini,<sup>115</sup> D. A. Sanz Becerra,<sup>115</sup> M. Schönenberger,<sup>115</sup> L. Shchutska,<sup>115</sup> V. R. Tavolaro,<sup>115</sup> K. Theofilatos,<sup>115</sup> M. L. Vesterbacka Olsson,<sup>115</sup> R. Wallny,<sup>115</sup> D. H. Zhu,<sup>115</sup> T. K. Aarrestad,<sup>116</sup> C. Amsler,<sup>116,zz</sup> D. Brzhechko,<sup>116</sup> M. F. Canelli,<sup>116</sup> A. De Cosa,<sup>116</sup> R. Del Burgo,<sup>116</sup> S. Donato,<sup>116</sup> C. Galloni,<sup>116</sup> T. Hreus,<sup>116</sup> B. Kilminster,<sup>116</sup> I. Neutelings,<sup>116</sup> D. Pinna,<sup>116</sup> G. Rauco,<sup>116</sup> P. Robmann,<sup>116</sup> D. Salerno,<sup>116</sup> K. Schweiger,<sup>116</sup> C. Seitz,<sup>116</sup> Y. Takahashi,<sup>116</sup> A. Zucchetta,<sup>116</sup> V. Candelise,<sup>117</sup> Y. H. Chang,<sup>117</sup> K. y. Cheng,<sup>117</sup> T. H. Doan,<sup>117</sup> Sh. Jain,<sup>117</sup> R. Khurana,<sup>117</sup> C. M. Kuo,<sup>117</sup> W. Lin,<sup>117</sup> A. Pozdnyakov,<sup>117</sup> S. S. Yu,<sup>117</sup> Arun Kumar,<sup>118</sup> P. Chang,<sup>118</sup> Y. Chao,<sup>118</sup> K. F. Chen,<sup>118</sup> P. H. Chen,<sup>118</sup> F. Fiori,<sup>118</sup> W.-S. Hou,<sup>118</sup> Y. Hsiung,<sup>118</sup> Y. F. Liu,<sup>118</sup> R.-S. Lu,<sup>118</sup> E. Paganis,<sup>118</sup> A. Psallidas,<sup>118</sup> A. Steen,<sup>118</sup> J. f. Tsai,<sup>118</sup> B. Asavapibhop,<sup>119</sup> K. Kovitanggoon,<sup>119</sup> G. Singh,<sup>119</sup> N. Srimanobhas,<sup>119</sup> A. Bat,<sup>120</sup> F. Boran,<sup>120</sup> S. Damarseckin,<sup>120</sup> Z. S. Demiroglu,<sup>120</sup> C. Dozen,<sup>120</sup> E. Eskut,<sup>120</sup> S. Girgis,<sup>120</sup> M. Oglakci,<sup>120</sup> G. Onengut,<sup>120</sup> K. Ozdemir,<sup>120,eee</sup> S. Ozturk,<sup>120,ddd</sup> A. Polatoz,<sup>120</sup> B. Tali,<sup>120,eee</sup> U. G. Tok,<sup>120</sup> S. Turk canar,<sup>120</sup> G. Gokoulut, T. Gulel, T. Hos, E. E. Kalgal, O. Kala, A. Kayls Topaksu, O. Killinsu,
M. Oglakci,<sup>120</sup> G. Onengut,<sup>120</sup> K. Ozdemir,<sup>120,ccc</sup> S. Ozturk,<sup>120,ddd</sup> A. Polatoz,<sup>120</sup> B. Tali,<sup>120,cee</sup> U. G. Tok,<sup>120</sup> S. Turkcapar,<sup>120</sup> I. S. Zorbakir,<sup>120</sup> C. Zorbilmez,<sup>120</sup> G. Karapinar,<sup>121,fff</sup> K. Ocalan,<sup>121,ggg</sup> M. Yalvac,<sup>121</sup> M. Zeyrek,<sup>121</sup> I. O. Atakisi,<sup>122</sup> E. Gülmez,<sup>122</sup> M. Kaya,<sup>122,ihh</sup> O. Kaya,<sup>122,iii</sup> S. Tekten,<sup>122</sup> E. A. Yetkin,<sup>122,ijj</sup> M. N. Agaras,<sup>123</sup> S. Atay,<sup>123</sup> A. Cakir,<sup>123</sup> K. Cankocak,<sup>123</sup> Y. Komurcu,<sup>123</sup> B. Grynyov,<sup>124</sup> L. Levchuk,<sup>125</sup> F. Ball,<sup>126</sup> L. Beck,<sup>126</sup> J. J. Brooke,<sup>126</sup> D. Burns,<sup>126</sup> E. Clement,<sup>126</sup> D. Cussans,<sup>126</sup> O. Davignon,<sup>126</sup> H. Flacher,<sup>126</sup> J. Goldstein,<sup>126</sup> G. P. Heath,<sup>126</sup> H. F. Heath,<sup>126</sup> L. Kreczko,<sup>126</sup> D. M. Newbold, <sup>126,kkk</sup> S. Paramesvaran, <sup>126</sup> T. Sakuma, <sup>126</sup> S. Seif El Nasr-storey, <sup>126</sup> D. Smith, <sup>126</sup> V. J. Smith, <sup>126</sup> K. W. Bell, <sup>127</sup> A. Belyaev, <sup>127,III</sup> C. Brew, <sup>127</sup> R. M. Brown, <sup>127</sup> D. Cieri, <sup>127</sup> D. J. A. Cockerill, <sup>127</sup> J. A. Coughlan, <sup>127</sup> K. Harder, <sup>127</sup> S. Harper, <sup>127</sup> A. Belyaev,<sup>127,III</sup> C. Brew,<sup>127</sup> R. M. Brown,<sup>127</sup> D. Cieri,<sup>127</sup> D. J. A. Cockerill,<sup>127</sup> J. A. Coughlan,<sup>127</sup> K. Harder,<sup>127</sup> S. Harper,<sup>127</sup> J. Linacre,<sup>127</sup> E. Olaiya,<sup>127</sup> D. Petyt,<sup>127</sup> C. H. Shepherd-Themistocleous,<sup>127</sup> A. Thea,<sup>127</sup> I. R. Tomalin,<sup>127</sup> T. Williams,<sup>127</sup> W. J. Womersley,<sup>127</sup> G. Auzinger,<sup>128</sup> R. Bainbridge,<sup>128</sup> P. Bloch,<sup>128</sup> J. Borg,<sup>128</sup> S. Breeze,<sup>128</sup> O. Buchmuller,<sup>128</sup> A. Bundock,<sup>128</sup> S. Casasso,<sup>128</sup> D. Colling,<sup>128</sup> L. Corpe,<sup>128</sup> P. Dauncey,<sup>128</sup> G. Davies,<sup>128</sup> M. Della Negra,<sup>128</sup> R. Di Maria,<sup>128</sup> Y. Haddad,<sup>128</sup> G. Hall,<sup>128</sup> G. Iles,<sup>128</sup> T. James,<sup>128</sup> M. Komm,<sup>128</sup> R. Lane,<sup>128</sup> C. Laner,<sup>128</sup> L. Lyons,<sup>128</sup> A.-M. Magnan,<sup>128</sup> S. Malik,<sup>128</sup> L. Mastrolorenzo,<sup>128</sup> T. Matsushita,<sup>128</sup> J. Nash,<sup>128,mmm</sup> A. Nikitenko,<sup>128,h</sup> V. Palladino,<sup>128</sup> M. Pesaresi,<sup>128</sup> A. Richards,<sup>128</sup> A. Rose,<sup>128</sup> E. Scott,<sup>128</sup> C. Seez,<sup>128</sup> A. Shtipliyski,<sup>128</sup> T. Strebler,<sup>128</sup> S. Summers,<sup>128</sup> A. Tapper,<sup>128</sup> K. Uchida,<sup>128</sup> M. Vazquez Acosta,<sup>128,nnn</sup> T. Virdee,<sup>128,q</sup> N. Wardle,<sup>128</sup> D. Winterbottom,<sup>128</sup> J. Wright,<sup>128</sup> S. C. Zenz,<sup>128</sup> J. E. Cole,<sup>129</sup> P. R. Hobson,<sup>129</sup> A. Khan,<sup>129</sup> P. Kyberd,<sup>129</sup> A. Morton,<sup>129</sup> I. D. Reid,<sup>129</sup> L. Teodorescu,<sup>129</sup> S. Zahid,<sup>129</sup> A. Borzou,<sup>130</sup> K. Call,<sup>130</sup> J. Dittmann,<sup>130</sup> K. Hatakeyama,<sup>130</sup> H. Liu,<sup>130</sup> N. Pastika,<sup>130</sup> C. Smith,<sup>130</sup> R. Bartek,<sup>131</sup> A. Dominguez,<sup>131</sup> A. Buccilli,<sup>132</sup> S. I. Cooper,<sup>132</sup> C. Henderson,<sup>133</sup> J. Rohlf<sup>133</sup> L. Sulak<sup>133</sup> D. Zou<sup>133</sup> G. Benelli<sup>134</sup> D. Cutts<sup>134</sup> A. Dominguez, <sup>137</sup> A. Buccilli, <sup>137</sup> S. I. Cooper, <sup>137</sup> C. Henderson, <sup>137</sup> P. Rumerio, <sup>137</sup> C. West, <sup>132</sup> D. Arcaro, <sup>133</sup> A. Avetisyan, <sup>135</sup> T. Bose, <sup>133</sup> D. Gastler, <sup>133</sup> D. Rankin, <sup>133</sup> C. Richardson, <sup>133</sup> J. Rohlf, <sup>133</sup> L. Sulak, <sup>133</sup> D. Zou, <sup>133</sup> G. Benelli, <sup>134</sup> D. Cutts, <sup>134</sup> M. Hadley, <sup>134</sup> J. Hakala, <sup>134</sup> U. Heintz, <sup>134</sup> J. M. Hogan, <sup>134,000</sup> K. H. M. Kwok, <sup>134</sup> E. Laird, <sup>134</sup> G. Landsberg, <sup>134</sup> J. Lee, <sup>134</sup> Z. Mao, <sup>134</sup> M. Narain, <sup>134</sup> J. Pazzini, <sup>134</sup> S. Piperov, <sup>134</sup> S. Sagir, <sup>134</sup> R. Syarif, <sup>134</sup> D. Yu, <sup>134</sup> R. Band, <sup>135</sup> C. Brainerd, <sup>135</sup> R. Breedon, <sup>135</sup> D. Burns, <sup>135</sup> M. Calderon De La Barca Sanchez, <sup>135</sup> M. Chertok, <sup>135</sup> J. Conway, <sup>135</sup> R. Conway, <sup>135</sup> P. T. Cox, <sup>135</sup> R. Erbacher, <sup>135</sup> C. Flores, <sup>135</sup> G. Funk, <sup>135</sup> W. Ko, <sup>135</sup> R. Lander, <sup>135</sup> C. Mclean, <sup>135</sup> M. Mulhearn, <sup>135</sup> D. Pellett, <sup>135</sup> J. Pilot, <sup>135</sup> S. Shalhout, <sup>135</sup> M. Shi, <sup>135</sup> J. Smith, <sup>135</sup> D. Stolp, <sup>135</sup> D. Taylor, <sup>135</sup> K. Tos, <sup>135</sup> M. Tripathi, <sup>135</sup> Z. Wang, <sup>135</sup> F. Zhang, <sup>135</sup> M. Bachtis, <sup>136</sup> C. Bravo, <sup>136</sup> R. Cousins, <sup>136</sup> A. Dasgupta, <sup>136</sup> A. Florent, <sup>137</sup> J. Hauser, <sup>137</sup> B. Clare <sup>137</sup> J. Ellison <sup>137</sup> M. Bachus, C. Bravo, R. Cousins, A. Dasgupta, A. Florent, J. Hauser, M. Ignatenko, N. Mccoll, S. Regnard, <sup>136</sup> D. Saltzberg, <sup>136</sup> C. Schnaible, <sup>136</sup> V. Valuev, <sup>136</sup> E. Bouvier, <sup>137</sup> K. Burt, <sup>137</sup> R. Clare, <sup>137</sup> J. Ellison, <sup>137</sup> J. W. Gary, <sup>137</sup> S. M. A. Ghiasi Shirazi, <sup>137</sup> G. Hanson, <sup>137</sup> G. Karapostoli, <sup>137</sup> E. Kennedy, <sup>137</sup> F. Lacroix, <sup>137</sup> O. R. Long, <sup>137</sup> M. Olmedo Negrete, <sup>137</sup> M. I. Paneva, <sup>137</sup> W. Si, <sup>137</sup> L. Wang, <sup>137</sup> H. Wei, <sup>137</sup> S. Wimpenny, <sup>137</sup> B. R. Yates, <sup>137</sup> J. G. Branson, <sup>138</sup> S. Cittolin, <sup>138</sup> M. Derdzinski, <sup>138</sup> R. Gerosa, <sup>138</sup> D. Gilbert, <sup>138</sup> B. Hashemi, <sup>138</sup> A. Holzner, <sup>138</sup> D. Klein, <sup>138</sup> G. Kole, <sup>138</sup> V. Krutelyov, <sup>138</sup> J. Letts, <sup>138</sup> M. Masciovecchio, <sup>138</sup> D. Olivito, <sup>138</sup> S. Padhi, <sup>138</sup> M. Pieri, <sup>138</sup> M. Sani, <sup>138</sup> V. Sharma, <sup>138</sup> J. Letts, <sup>138</sup> M. Masciovecchio, <sup>138</sup> D. Olivito, <sup>138</sup> S. Padhi, <sup>138</sup> M. Pieri, <sup>138</sup> M. Sani, <sup>138</sup> V. Sharma, <sup>138</sup> J. Letts, <sup>138</sup> M. 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Wasserbaech,<sup>138,ppp</sup> J. Wood,<sup>138</sup> F. Würthwein,<sup>138</sup> A. Yagil,<sup>138</sup> G. Zevi Della Porta,<sup>138</sup> N. Amin,<sup>139</sup> R. Bhandari,<sup>139</sup> J. Bradmiller-Feld,<sup>139</sup> C. Campagnari,<sup>139</sup> M. Citron,<sup>139</sup> A. Dishaw,<sup>139</sup> V. Dutta,<sup>139</sup> M. Franco Sevilla,<sup>139</sup> L. Gouskos,<sup>139</sup> R. Heller,<sup>139</sup> J. Incandela,<sup>139</sup> A. Ovcharova,<sup>139</sup> H. Qu,<sup>139</sup> J. Richman,<sup>139</sup> D. Stuart,<sup>139</sup> I. Suarez,<sup>139</sup> J. Yoo,<sup>139</sup> D. Anderson,<sup>140</sup> A. Bornheim,<sup>140</sup> J. Bunn,<sup>140</sup> J. M. Lawhorn,<sup>140</sup> H. B. Newman,<sup>140</sup> T. Q. Nguyen,<sup>140</sup> C. Pena,<sup>140</sup> M. Spiropulu,<sup>140</sup> J. R. Vlimant,<sup>140</sup> R. Wilkinson,<sup>140</sup> S. Xie,<sup>140</sup> Z. Zhang,<sup>140</sup> R. Y. Zhu,<sup>140</sup> M. B. Andrews, <sup>141</sup> T. Ferguson, <sup>141</sup> T. Mudholkar, <sup>141</sup> M. Paulini, <sup>141</sup> J. Russ, <sup>141</sup> M. Sun, <sup>141</sup> H. Vogel, <sup>141</sup> I. Vorobiev, <sup>141</sup> M. Weinberg, <sup>141</sup> J. P. Cumalat, <sup>142</sup> W. T. Ford, <sup>142</sup> F. Jensen, <sup>142</sup> A. Johnson, <sup>142</sup> M. Krohn, <sup>142</sup> S. Leontsinis, <sup>142</sup> E. MacDonald, <sup>142</sup> T. Mulholland, <sup>142</sup> K. Stenson, <sup>142</sup> K. A. Ulmer, <sup>142</sup> S. R. Wagner, <sup>142</sup> J. Alexander, <sup>143</sup> J. Chaves, <sup>143</sup>

Y. Cheng,<sup>143</sup> J. Chu,<sup>143</sup> A. Datta,<sup>143</sup> K. Mcdermott,<sup>143</sup> N. Mirman,<sup>143</sup> J. R. Patterson,<sup>143</sup> D. Quach,<sup>143</sup> A. Rinkevicius,<sup>143</sup> A. Ryd,<sup>143</sup> L. Skinnari,<sup>143</sup> L. Soffi,<sup>143</sup> S. M. Tan,<sup>143</sup> Z. Tao,<sup>143</sup> J. Thom,<sup>143</sup> J. Tucker,<sup>143</sup> P. Wittich,<sup>143</sup> M. Zientek,<sup>143</sup> S. Abdullin,<sup>144</sup> M. Albrow,<sup>144</sup> M. Alyari,<sup>144</sup> G. Apollinari,<sup>144</sup> A. Apresyan,<sup>144</sup> A. Apyan,<sup>144</sup> S. Banerjee,<sup>144</sup> L. A. T. Bauerdick,<sup>144</sup> A. Beretvas,<sup>144</sup> J. Berryhill,<sup>144</sup> P. C. Bhat,<sup>144</sup> G. Bolla,<sup>144,a</sup> K. Burkett,<sup>144</sup> J. N. Butler,<sup>144</sup> A. Canepa,<sup>144</sup> G. B. Cerati,<sup>144</sup> H. W. K. Cheung,<sup>144</sup> F. Chlebana,<sup>144</sup> M. Cremonesi,<sup>144</sup> J. Duarte,<sup>144</sup> V. D. Elvira,<sup>144</sup> J. Freeman,<sup>144</sup> Z. Gecse,<sup>144</sup> E. Gottschalk,<sup>144</sup> L. Gray,<sup>144</sup> D. Green,<sup>144</sup> S. Grünendahl,<sup>144</sup> O. Gutsche,<sup>144</sup> J. Hanlon,<sup>144</sup> R. M. Harris,<sup>144</sup> S. Hasegawa,<sup>144</sup> J. Hirschauer,<sup>144</sup> Z. Hu,<sup>144</sup> B. Jayatilaka,<sup>144</sup> S. Jindariani,<sup>144</sup> M. Johnson,<sup>144</sup> U. Joshi,<sup>144</sup> B. Klima,<sup>144</sup> M. J. Kortelainen,<sup>144</sup> B. Kreis,<sup>144</sup> S. Lammel,<sup>144</sup> D. Lincoln,<sup>144</sup> R. Lipton,<sup>144</sup> M. Liu,<sup>144</sup> T. Liu,<sup>144</sup> R. Lopes De Sá,<sup>144</sup> J. Lykken,<sup>144</sup> K. Maeshima,<sup>144</sup> N. Magini,<sup>144</sup> J. M. Marraffino,<sup>144</sup> D. Mason,<sup>144</sup> P. McBride,<sup>144</sup> P. Merkel,<sup>144</sup> S. Mrenna,<sup>144</sup> J. Lykken,<sup>144</sup> K. Maeshima,<sup>144</sup> M. O. Prokofvey,<sup>144</sup> G. Bakness,<sup>144</sup> L. Ristori,<sup>144</sup> A. Sayoy-Nayaro,<sup>144,qqq</sup> M. J. Kortelainen,<sup>144</sup> B. Kreis,<sup>144</sup> S. Lammel,<sup>144</sup> D. Lincoln,<sup>144</sup> R. Lipton,<sup>144</sup> M. Lu,<sup>144</sup> T. Liu,<sup>144</sup> R. Lopes De Sá,<sup>144</sup>
 J. Lykken,<sup>144</sup> K. Maeshima,<sup>144</sup> N. Magini,<sup>144</sup> J. M. Maraffino,<sup>144</sup> D. Mason,<sup>144</sup> P. McBride,<sup>144</sup> P. Merkel,<sup>144</sup> S. Narenn,<sup>144</sup> S. Snah,<sup>144</sup> K. Pedro,<sup>144</sup> O. Prokofyev,<sup>144</sup> G. Rakness,<sup>144</sup> L. Ristori,<sup>144</sup> A. Savoy-Navaro,<sup>144,094</sup>
 B. Schneider,<sup>144</sup> E. Sexton-Kennedy,<sup>144</sup> A. Soha,<sup>144</sup> W. J. Spalding,<sup>144</sup> L. Spiegel,<sup>144</sup> S. Tokoryev,<sup>141</sup> N. Strobbe,<sup>144</sup>
 L. Taylor,<sup>144</sup> S. Tkaczyk,<sup>144</sup> N. V. Tran,<sup>144</sup> L. Uplegger,<sup>144</sup> E. W. Vaandering,<sup>144</sup> C. Vernieri,<sup>144</sup> M. Verzocchi,<sup>144</sup> R. Vidal,<sup>144</sup>
 M. Wang,<sup>145</sup> A. Carnes,<sup>145</sup> M. Carrer,<sup>145</sup> D. Curry,<sup>145</sup> R. D. Field,<sup>145</sup> I. K. Furic,<sup>145</sup> S. V. Gleyzer,<sup>145</sup> B. M. Joshi,<sup>145</sup>
 J. Konigsberg,<sup>145</sup> A. Carnes,<sup>145</sup> M. Carrer,<sup>145</sup> D. Curry,<sup>145</sup> K. Matchev,<sup>145</sup> H. Mei,<sup>145</sup> G. Mitselmakher,<sup>145</sup> K. M. Joshi,<sup>145</sup>
 J. Sperka,<sup>145</sup> N. Terentyev,<sup>145</sup> L. Thomas,<sup>145</sup> J. Wang,<sup>145</sup> S. Wang,<sup>145</sup> J. Yelton,<sup>145</sup> Y. R. Joshi,<sup>146</sup> S. Linn,<sup>146</sup> P. Markowitz,<sup>146</sup>
 J. L. Rodriguez,<sup>146</sup> A. Ackert,<sup>147</sup> T. Adams,<sup>147</sup> A. Askew,<sup>147</sup> S. Hagopian,<sup>147</sup> V. Hagopian,<sup>147</sup> K. F. Johnson,<sup>147</sup> T. Kolberg,<sup>147</sup>
 G. Martinez,<sup>147</sup> T. Perry,<sup>147</sup> H. Prosper,<sup>147</sup> A. Saha,<sup>147</sup> A. Santra,<sup>147</sup> V. Sharma,<sup>147</sup> R. Yohay,<sup>148</sup> M. R. Adams,<sup>149</sup>
 V. Bhopatkar,<sup>148</sup> S. Colafranceschi,<sup>148</sup> M. Hohlmann,<sup>148</sup> D. Noonan,<sup>148</sup> T. Roy,<sup>148</sup> S. Yuniceva,<sup>148</sup> M. R. Adams,<sup>149</sup>
 C. E. Gerber,<sup>149</sup> D. A. Hangal,<sup>149</sup> D. J. Hofman,<sup>149</sup> K. Jung,<sup>149</sup> J. Kamin,<sup>149</sup> J. D. Sandoval Gonzalez,<sup>149</sup> M. B. Tonjes,<sup>149</sup> N. Varelas,<sup>149</sup> H. Wang,<sup>149</sup> Z. Wu,<sup>149</sup> J. Zhang,<sup>149</sup> B. Bilki,<sup>150,rr</sup> W. Clarida,<sup>150</sup> K. Dilsiz,<sup>150,sss</sup> S. Durgut,<sup>150</sup>
 R. P. Gandrajula,<sup>150</sup> M. Haytmyradov,<sup>150</sup> V. Khristenko,<sup>150</sup> J.-P. Merlo,<sup>150</sup> H. Mermerkaya,<sup>150,ut</sup> A. Mestvirishvili,<sup>150</sup>
 M. Moueller,<sup>151</sup> J Y. Iiyama, <sup>156</sup> G. M. Innocenti, <sup>156</sup> M. Klute, <sup>156</sup> D. Kovalskyi, <sup>156</sup> Y.-J. Lee, <sup>156</sup> A. Levin, <sup>156</sup> P. D. Luckey, <sup>156</sup> B. Maier, <sup>156</sup> A. C. Marini, <sup>156</sup> C. Mironov, <sup>156</sup> S. Narayanan, <sup>156</sup> X. Niu, <sup>156</sup> C. Paus, <sup>156</sup> C. Roland, <sup>156</sup> G. Roland, <sup>156</sup> G. Roland, <sup>156</sup> G. S. F. Stephans, <sup>156</sup> K. Sumorok, <sup>156</sup> K. Tatar, <sup>156</sup> D. Velicanu, <sup>156</sup> J. Wang, <sup>156</sup> T. W. Wang, <sup>156</sup> B. Wyslouch, <sup>156</sup> S. Zhaozhong,<sup>156</sup> A. C. Benvenuti,<sup>157</sup> R. M. Chatterjee,<sup>157</sup> A. Evans,<sup>157</sup> P. Hansen,<sup>157</sup> S. Kalafut,<sup>157</sup> Y. Kubota,<sup>157</sup> Z. Lesko,<sup>157</sup> J. Mans,<sup>157</sup> S. Nourbakhsh,<sup>157</sup> N. Ruckstuhl,<sup>157</sup> R. Rusack,<sup>157</sup> J. Turkewitz,<sup>157</sup> M. A. Wadud,<sup>157</sup> J. G. Acosta,<sup>158</sup> S. Oliveros,<sup>158</sup> E. Avdeeva,<sup>159</sup> K. Bloom,<sup>159</sup> D. R. Claes,<sup>159</sup> C. Fangmeier,<sup>159</sup> F. Golf,<sup>159</sup> R. Gonzalez Suarez,<sup>159</sup> R. Kamalieddin,<sup>159</sup> I. Kravchenko,<sup>159</sup> J. Monroy,<sup>159</sup> J. E. Siado,<sup>159</sup> G. R. Snow,<sup>159</sup> B. Stieger,<sup>159</sup> A. Godshalk,<sup>160</sup> C. Harrington,<sup>160</sup> I. Iashvili,<sup>160</sup> D. Nguyen,<sup>160</sup> A. Parker,<sup>160</sup> S. Rappoccio,<sup>160</sup> B. Roozbahani,<sup>160</sup> G. Alverson,<sup>161</sup> C. Harrington, M.I. Iashvili, M.D. Nguyen, M.A. Parker, M.S. Rappoccio, M.B. Roozbanani, M.G. Alverson, M. E. Barberis,<sup>161</sup> C. Freer,<sup>161</sup> A. Hortiangtham,<sup>161</sup> A. Massironi,<sup>161</sup> D. M. Morse,<sup>161</sup> T. Orimoto,<sup>161</sup> R. Teixeira De Lima,<sup>161</sup> T. Wamorkar,<sup>161</sup> B. Wang,<sup>161</sup> A. Wisecarver,<sup>161</sup> D. Wood,<sup>161</sup> S. Bhattacharya,<sup>162</sup> O. Charaf,<sup>162</sup> K. A. Hahn,<sup>162</sup> N. Mucia,<sup>162</sup> N. Odell,<sup>162</sup> M. H. Schmitt,<sup>162</sup> K. Sung,<sup>162</sup> M. Trovato,<sup>162</sup> M. Velasco,<sup>162</sup> R. Bucci,<sup>163</sup> N. Dev,<sup>163</sup> M. Hildreth,<sup>163</sup> K. Hurtado Anampa,<sup>163</sup> C. Jessop,<sup>163</sup> D. J. Karmgard,<sup>163</sup> N. Kellams,<sup>163</sup> K. Lannon,<sup>163</sup> W. Li,<sup>163</sup> N. Loukas,<sup>163</sup> N. Marinelli,<sup>163</sup> F. Meng,<sup>163</sup> C. Mueller,<sup>163</sup> Y. Musienko,<sup>163,II</sup> M. Planer,<sup>163</sup> A. Reinsvold,<sup>163</sup> R. Ruchti,<sup>163</sup> P. Siddireddy,<sup>163</sup> G. Smith,<sup>163</sup> S. Taroni,<sup>163</sup> M. Wayne,<sup>163</sup> A. Wightman,<sup>163</sup> M. Wolf,<sup>163</sup> A. Woodard,<sup>163</sup> J. Alimena,<sup>164</sup> L. Antonelli,<sup>164</sup> B. Bylsma,<sup>164</sup> L. S. Durkin,<sup>164</sup> S. Flowers,<sup>164</sup> B. Francis,<sup>164</sup> A. Hart,<sup>164</sup> C. Hill,<sup>164</sup> W. Ji,<sup>164</sup> T. Y. Ling,<sup>164</sup> W. Luo,<sup>164</sup> B. L. Winer, <sup>164</sup> H. W. Wulsin, <sup>164</sup> S. Cooperstein, <sup>165</sup> O. Driga, <sup>165</sup> P. Elmer, <sup>165</sup> J. Hardenbrook, <sup>165</sup> P. Hebda, <sup>165</sup>

S. Higginbotham,<sup>165</sup> A. Kalogeropoulos,<sup>165</sup> D. Lange,<sup>165</sup> J. Luo,<sup>165</sup> D. Marlow,<sup>165</sup> K. Mei,<sup>165</sup> I. Ojalvo,<sup>165</sup> J. Olsen,<sup>165</sup> C. Palmer,<sup>165</sup> P. Piroué,<sup>165</sup> J. Salfeld-Nebgen,<sup>165</sup> D. Stickland,<sup>165</sup> C. Tully,<sup>165</sup> S. Malik,<sup>166</sup> S. Norberg,<sup>166</sup> A. Barker,<sup>167</sup> V. E. Barnes,<sup>167</sup> S. Das,<sup>167</sup> L. Gutay,<sup>167</sup> M. Jones,<sup>167</sup> A. W. Jung,<sup>167</sup> A. Khatiwada,<sup>167</sup> D. H. Miller,<sup>167</sup> N. Neumeister,<sup>167</sup> C. C. Peng,<sup>167</sup> H. Qiu,<sup>167</sup> J. F. Schulte,<sup>167</sup> J. Sun,<sup>167</sup> F. Wang,<sup>167</sup> R. Xiao,<sup>167</sup> W. Xie,<sup>167</sup> T. Cheng,<sup>168</sup> J. Dolen,<sup>168</sup> N. Parashar,<sup>168</sup> Z. Chen,<sup>169</sup> K. M. Ecklund,<sup>169</sup> S. Freed,<sup>169</sup> F. J. M. Geurts,<sup>169</sup> M. Guilbaud,<sup>169</sup> M. Kilpatrick,<sup>169</sup> W. Li,<sup>169</sup> B. Michlin,<sup>169</sup> B. P. Padley,<sup>169</sup> J. Roberts,<sup>169</sup> J. Rorie,<sup>169</sup> W. Shi,<sup>169</sup> Z. Tu,<sup>169</sup> J. Zabel,<sup>169</sup> A. Zhang,<sup>169</sup> A. Bodek,<sup>170</sup> P. B. Michlin,<sup>170</sup> R. Demina,<sup>170</sup> V. t. Duh,<sup>170</sup> T. Ferbel,<sup>170</sup> M. Galanti,<sup>170</sup> A. Garcia-Bellido,<sup>170</sup> J. Han,<sup>170</sup> O. Hindrichs,<sup>170</sup> A. Agapitos,<sup>172</sup> J. P. Chou,<sup>172</sup> Y. Gershtein,<sup>172</sup> T. A. Gómez Espinosa,<sup>172</sup> E. Halkiadakis,<sup>172</sup> M. Heindl,<sup>172</sup> E. Hughes,<sup>172</sup> S. Kaplan,<sup>172</sup> S. Salur,<sup>172</sup> S. Schnetzer,<sup>172</sup> D. Sheffield,<sup>173</sup> S. Sanalwar,<sup>174</sup> R. Stone,<sup>172</sup> S. Thomas,<sup>174</sup> P. Thomassen,<sup>172</sup> H. Saka,<sup>172</sup> A. G. Delannoy,<sup>173</sup> J. Heideman,<sup>173</sup> G. Riley,<sup>173</sup> K. Rose,<sup>173</sup> S. Spanier,<sup>173</sup> K. Thapa,<sup>174</sup> O. Bouhali,<sup>174</sup>,<sup>174</sup> W. Walker,<sup>174</sup> A. Gellannoy,<sup>174</sup> M. Dalchenko,<sup>174</sup> M. De Mattia,<sup>174</sup> A. Delgado,<sup>174</sup> S. Dildick,<sup>174</sup> R. Eusebi,<sup>174</sup> J. Gilmore,<sup>174</sup> T. Huang,<sup>174</sup> T. Kamon,<sup>174</sup> N. Akchurin,<sup>175</sup> J. Damgov,<sup>175</sup> F. De Guio,<sup>175</sup> S. R. Dudero,<sup>175</sup> J. Faulkner,<sup>175</sup> S. Undleeb,<sup>175</sup> S. W. Lee,<sup>175</sup> T. Mengke,<sup>175</sup> S. Muthumuni,<sup>175</sup> T. Peltola,<sup>175</sup> S. Undleeb,<sup>175</sup> I. Gurpina,<sup>175</sup> S. Kunori,<sup>175</sup> K. Lamichhane,<sup>176</sup> S. W. Lee,<sup>175</sup> T. Mengke,<sup>175</sup> S. Muthumuni,<sup>175</sup> T. Peltola,<sup>176</sup> H. Ni,<sup>176</sup> K. Padeken,<sup>176</sup> J. D. Ruiz Alvarez,<sup>176</sup> P. Sheldon,<sup>176</sup> K. Janjam,<sup>176</sup> W. Johns,<sup>176</sup> C. Maguire,<sup>176</sup> A. Melo,<sup>176</sup> H. Ni,<sup>176</sup> C. Cullol,<sup>179</sup> S. Kunori,<sup>175</sup> K. Lam

(CMS Collaboration)

<sup>1</sup>Yerevan Physics Institute, Yerevan, Armenia

<sup>2</sup>Institut für Hochenergiephysik, Wien, Austria

<sup>3</sup>Institute for Nuclear Problems, Minsk, Belarus

<sup>4</sup>Universiteit Antwerpen, Antwerpen, Belgium <sup>5</sup>Vrije Universiteit Brussel, Brussel, Belgium

<sup>6</sup>Université Libre de Bruxelles, Bruxelles, Belgium

<sup>7</sup>Ghent University, Ghent, Belgium

<sup>8</sup>Université Catholique de Louvain, Louvain-la-Neuve, Belgium

<sup>9</sup>Centro Brasileiro de Pesquisas Fisicas, Rio de Janeiro, Brazil

<sup>10</sup>Universidade do Estado do Rio de Janeiro, Rio de Janeiro, Brazil

<sup>11a</sup>Universidade Estadual Paulista, Universidade Federal do ABC, São Paulo, Brazil

<sup>11b</sup>Universidade Estadual Paulista

<sup>11c</sup>Universidade Federal do ABC

<sup>12</sup>Institute for Nuclear Research and Nuclear Energy, Bulgarian Academy of Sciences, Sofia, Bulgaria

<sup>13</sup>University of Sofia, Sofia, Bulgaria

<sup>14</sup>Beihang University, Beijing, China

<sup>15</sup>Institute of High Energy Physics, Beijing, China

<sup>16</sup>State Key Laboratory of Nuclear Physics and Technology, Peking University, Beijing, China

<sup>17</sup>Tsinghua University, Beijing, China

<sup>18</sup>Universidad de Los Andes, Bogota, Colombia

<sup>19</sup>University of Split, Faculty of Electrical Engineering, Mechanical Engineering and Naval Architecture,

Split, Croatia

<sup>20</sup>University of Split, Faculty of Science, Split, Croatia

<sup>21</sup>Institute Rudjer Boskovic, Zagreb, Croatia

<sup>22</sup>University of Cyprus, Nicosia, Cyprus

<sup>23</sup>Charles University, Prague, Czech Republic

<sup>24</sup>Universidad San Francisco de Quito, Quito, Ecuador

<sup>25</sup>Academy of Scientific Research and Technology of the Arab Republic of Egypt, Egyptian Network of High Energy Physics, Cairo, Egypt <sup>26</sup>National Institute of Chemical Physics and Biophysics, Tallinn, Estonia <sup>7</sup>Department of Physics, University of Helsinki, Helsinki, Finland <sup>28</sup>Helsinki Institute of Physics, Helsinki, Finland <sup>29</sup>Lappeenranta University of Technology, Lappeenranta, Finland <sup>30</sup>IRFU, CEA, Université Paris-Saclay, Gif-sur-Yvette, France <sup>31</sup>Laboratoire Leprince-Ringuet, Ecole polytechnique, CNRS/IN2P3, Université Paris-Saclay, Palaiseau, France <sup>32</sup>Université de Strasbourg, CNRS, IPHC UMR 7178, F-67000 Strasbourg, France <sup>33</sup>Centre de Calcul de l'Institut National de Physique Nucleaire et de Physique des Particules, CNRS/IN2P3, Villeurbanne, France <sup>34</sup>Université de Lyon, Université Claude Bernard Lyon 1, CNRS-IN2P3, Institut de Physique Nucléaire de Lyon, Villeurbanne, France <sup>35</sup>Georgian Technical University, Tbilisi, Georgia <sup>36</sup>Tbilisi State University, Tbilisi, Georgia <sup>37</sup>RWTH Aachen University, I. Physikalisches Institut, Aachen, Germany <sup>38</sup>RWTH Aachen University, III. Physikalisches Institut A, Aachen, Germany <sup>39</sup>RWTH Aachen University, III. Physikalisches Institut B, Aachen, Germany <sup>40</sup>Deutsches Elektronen-Synchrotron, Hamburg, Germany <sup>41</sup>University of Hamburg, Hamburg, Germany <sup>42</sup>Institut für Experimentelle Teilchenphysik, Karlsruhe, Germany <sup>43</sup>Institute of Nuclear and Particle Physics (INPP), NCSR Demokritos, Aghia Paraskevi, Greece <sup>4</sup>National and Kapodistrian University of Athens, Athens, Greece <sup>5</sup>National Technical University of Athens, Athens, Greece <sup>46</sup>University of Ioánnina, Ioánnina, Greece <sup>47</sup>MTA-ELTE Lendület CMS Particle and Nuclear Physics Group, Eötvös Loránd University, Budapest, Hungary <sup>48</sup>Wigner Research Centre for Physics, Budapest, Hungary <sup>49</sup>Institute of Nuclear Research ATOMKI, Debrecen, Hungary <sup>50</sup>Institute of Physics, University of Debrecen, Debrecen, Hungary <sup>51</sup>Indian Institute of Science (IISc), Bangalore, India <sup>52</sup>National Institute of Science Education and Research, Bhubaneswar, India <sup>53</sup>Panjab University, Chandigarh, India <sup>54</sup>University of Delhi, Delhi, India <sup>55</sup>Saha Institute of Nuclear Physics, HBNI, Kolkata,India <sup>6</sup>Indian Institute of Technology Madras, Madras, India <sup>7</sup>Bhabha Atomic Research Centre, Mumbai, India <sup>58</sup>Tata Institute of Fundamental Research-A, Mumbai, India <sup>59</sup>Tata Institute of Fundamental Research-B, Mumbai, India <sup>60</sup>Indian Institute of Science Education and Research (IISER), Pune, India <sup>51</sup>Institute for Research in Fundamental Sciences (IPM), Tehran, Iran <sup>62</sup>University College Dublin, Dublin, Ireland <sup>63a</sup>INFN Sezione di Bari, Università di Bari, Politecnico di Bari, Bari, Italy <sup>63b</sup>INFN Sezione di Bari <sup>63c</sup>Università di Bari <sup>63d</sup>Politecnico di Bari <sup>64a</sup>INFN Sezione di Bologna, Università di Bologna, Bologna, Italy <sup>64b</sup>INFN Sezione di Bologna <sup>64</sup>cUniversità di Bologna <sup>65a</sup>INFN Sezione di Catania, Università di Catania, Catania, Italy <sup>65b</sup>INFN Sezione di Catania <sup>65</sup>*c*Università di Catania <sup>66a</sup>INFN Sezione di Firenze, Università di Firenze, Firenze, Italy 666 INFN Sezione di Firenze 66c Università di Firenze <sup>67</sup>INFN Laboratori Nazionali di Frascati, Frascati, Italy <sup>68a</sup>INFN Sezione di Genova, Università di Genova, Genova, Italy <sup>68b</sup>INFN Sezione di Genova <sup>68c</sup>Università di Genova

<sup>69a</sup>INFN Sezione di Milano-Bicocca <sup>69b</sup>Università di Milano-Bicocca <sup>70a</sup>INFN Sezione di Napoli, Università di Napoli 'Federico II', Napoli, Italy, Università della Basilicata, Potenza, Italy, Università G. Marconi, Roma, Italy <sup>70b</sup>INFN Sezione di Napoli <sup>70</sup>cUniversità di Napoli 'Federico II' <sup>70d</sup>Università della Basilicata <sup>70e</sup>Università G. Marconi <sup>71a</sup>INFN Sezione di Padova, Università di Padova, Padova, Italy, Università di Trento, Trento, Italy <sup>1b</sup>INFN Sezione di Padova <sup>71</sup><sup>c</sup>Università di Padova <sup>71d</sup>Università di Trento <sup>72a</sup>INFN Sezione di Pavia <sup>72b</sup>Università di Pavia <sup>73a</sup>INFN Sezione di Perugia, Università di Perugia, Perugia, Italy <sup>73b</sup>INFN Sezione di Perugia <sup>73c</sup>Università di Perugia <sup>74a</sup>INFN Sezione di Pisa, Università di Pisa, Scuola Normale Superiore di Pisa, Pisa, Italy <sup>4b</sup>INFN Sezione di Pisa <sup>74c</sup>Università di Pisa <sup>74d</sup>Scuola Normale Superiore di Pisa <sup>75a</sup>INFN Sezione di Roma, Sapienza Università di Roma, Rome, Italy <sup>75b</sup>INFN Sezione di Roma <sup>75</sup>cSapienza Università di Roma <sup>76a</sup>INFN Sezione di Torino, Università di Torino, Torino, Italy, Università del Piemonte Orientale, Novara, Italy <sup>76b</sup>INFN Sezione di Torino <sup>76c</sup>Università di Torino <sup>76d</sup>Università del Piemonte Orientale <sup>77a</sup>INFN Sezione di Trieste, Università di Trieste, Trieste, Italy <sup>7b</sup>INFN Sezione di Trieste <sup>77</sup><sup>c</sup>Università di Trieste <sup>78</sup>Kyungpook National University <sup>79</sup>Chonnam National University, Institute for Universe and Elementary Particles, Kwangju, Korea <sup>80</sup>Hanyang University, Seoul, Korea <sup>81</sup>Korea University, Seoul, Korea <sup>82</sup>Seoul National University, Seoul, Korea <sup>83</sup>University of Seoul, Seoul, Korea <sup>84</sup>Sungkyunkwan University, Suwon, Korea <sup>85</sup>Vilnius University, Vilnius, Lithuania <sup>86</sup>National Centre for Particle Physics, Universiti Malaya, Kuala Lumpur, Malaysia <sup>87</sup>Centro de Investigacion y de Estudios Avanzados del IPN, Mexico City, Mexico <sup>88</sup>Universidad Iberoamericana, Mexico City, Mexico <sup>89</sup>Benemerita Universidad Autonoma de Puebla, Puebla, Mexico <sup>90</sup>Universidad Autónoma de San Luis Potosí, San Luis Potosí, Mexico <sup>1</sup>University of Auckland, Auckland, New Zealand <sup>92</sup>University of Canterbury, Christchurch, New Zealand <sup>93</sup>National Centre for Physics, Quaid-I-Azam University, Islamabad, Pakistan <sup>94</sup>National Centre for Nuclear Research, Swierk, Poland <sup>95</sup>Institute of Experimental Physics, Faculty of Physics, University of Warsaw, Warsaw, Poland <sup>96</sup>Laboratório de Instrumentação e Física Experimental de Partículas, Lisboa, Portugal <sup>97</sup>Joint Institute for Nuclear Research, Dubna, Russia <sup>98</sup>Petersburg Nuclear Physics Institute, Gatchina (St. Petersburg), Russia <sup>99</sup>Institute for Nuclear Research, Moscow, Russia <sup>100</sup>Institute for Theoretical and Experimental Physics, Moscow, Russia <sup>101</sup>Moscow Institute of Physics and Technology, Moscow, Russia <sup>102</sup>National Research Nuclear University 'Moscow Engineering Physics Institute' (MEPhI), Moscow, Russia <sup>103</sup>P.N. Lebedev Physical Institute, Moscow, Russia

<sup>104</sup>Skobeltsyn Institute of Nuclear Physics, Lomonosov Moscow State University, Moscow, Russia <sup>05</sup>Novosibirsk State University (NSU), Novosibirsk, Russia <sup>106</sup>State Research Center of Russian Federation, Institute for High Energy Physics of NRC "Kurchatov Institute", Protvino, Russia <sup>107</sup>National Research Tomsk Polytechnic University, Tomsk, Russia <sup>108</sup>University of Belgrade, Faculty of Physics and Vinca Institute of Nuclear Sciences, Belgrade, Serbia <sup>109</sup>Centro de Investigaciones Energéticas Medioambientales y Tecnológicas (CIEMAT), Madrid, Spain <sup>110</sup>Universidad Autónoma de Madrid, Madrid, Spain <sup>111</sup>Universidad de Oviedo, Oviedo, Spain <sup>112</sup>Instituto de Física de Cantabria (IFCA), CSIC-Universidad de Cantabria, Santander, Spain <sup>13</sup>CERN, European Organization for Nuclear Research, Geneva, Switzerland <sup>114</sup>Paul Scherrer Institut, Villigen, Switzerland <sup>115</sup>ETH Zurich - Institute for Particle Physics and Astrophysics (IPA), Zurich, Switzerland <sup>116</sup>Universität Zürich, Zurich, Switzerland <sup>117</sup>National Central University, Chung-Li, Taiwan <sup>118</sup>National Taiwan University (NTU), Taipei, Taiwan <sup>119</sup>Chulalongkorn University, Faculty of Science, Department of Physics, Bangkok, Thailand <sup>120</sup>Cukurova University, Physics Department, Science and Art Faculty, Adana, Turkey <sup>121</sup>Middle East Technical University, Physics Department, Ankara, Turkey <sup>122</sup>Bogazici University, Istanbul, Turkey <sup>123</sup>Istanbul Technical University, Istanbul, Turkey <sup>124</sup>Institute for Scintillation Materials of National Academy of Science of Ukraine, Kharkov, Ukraine <sup>5</sup>National Scientific Center, Kharkov Institute of Physics and Technology, Kharkov, Ukraine <sup>126</sup>University of Bristol, Bristol, United Kingdom <sup>127</sup>Rutherford Appleton Laboratory, Didcot, United Kingdom <sup>28</sup>Imperial College, London, United Kingdom <sup>129</sup>Brunel University, Uxbridge, United Kingdom <sup>130</sup>Baylor University, Waco, USA <sup>131</sup>Catholic University of America, Washington DC, USA <sup>132</sup>The University of Alabama, Tuscaloosa, USA <sup>133</sup>Boston University, Boston, USA <sup>134</sup>Brown University, Providence, USA <sup>135</sup>University of California, Davis, Davis, USA <sup>136</sup>University of California, Los Angeles, USA <sup>137</sup>University of California, Riverside, Riverside, USA <sup>138</sup>University of California, San Diego, La Jolla, USA <sup>139</sup>University of California, Santa Barbara - Department of Physics, Santa Barbara, USA <sup>9</sup>California Institute of Technology, Pasadena, USA <sup>141</sup>Carnegie Mellon University, Pittsburgh, USA <sup>142</sup>University of Colorado Boulder, Boulder, USA <sup>143</sup>Cornell University, Ithaca, USA <sup>144</sup>Fermi National Accelerator Laboratory, Batavia, USA <sup>145</sup>University of Florida, Gainesville, USA <sup>146</sup>Florida International University, Miami, USA <sup>147</sup>Florida State University, Tallahassee, USA <sup>148</sup>Florida Institute of Technology, Melbourne, USA <sup>149</sup>University of Illinois at Chicago (UIC), Chicago, USA <sup>150</sup>The University of Iowa, Iowa City, USA <sup>151</sup>Johns Hopkins University, Baltimore, USA <sup>152</sup>The University of Kansas, Lawrence, USA <sup>153</sup>Kansas State University, Manhattan, USA <sup>154</sup>Lawrence Livermore National Laboratory, Livermore, USA <sup>155</sup>University of Maryland, College Park, USA <sup>156</sup>Massachusetts Institute of Technology, Cambridge, USA <sup>157</sup>University of Minnesota, Minneapolis, USA <sup>158</sup>University of Mississippi, Oxford, USA <sup>159</sup>University of Nebraska-Lincoln, Lincoln, USA <sup>160</sup>State University of New York at Buffalo, Buffalo, USA <sup>161</sup>Northeastern University, Boston, USA <sup>162</sup>Northwestern University, Evanston, USA

<sup>163</sup>University of Notre Dame, Notre Dame, USA <sup>164</sup>The Ohio State University, Columbus, USA <sup>165</sup>Princeton University, Princeton, USA <sup>166</sup>University of Puerto Rico, Mayaguez, USA <sup>167</sup>Purdue University, West Lafayette, USA <sup>168</sup>Purdue University Northwest, Hammond, USA <sup>169</sup>Rice University, Houston, USA <sup>170</sup>University of Rochester, Rochester, USA <sup>171</sup>The Rockefeller University, New York, USA <sup>172</sup>Rutgers, The State University of New Jersey, Piscataway, USA <sup>173</sup>University of Tennessee, Knoxville, USA <sup>174</sup>Texas A&M University, College Station, USA <sup>175</sup>Texas Tech University, Lubbock, USA <sup>176</sup>Vanderbilt University, Nashville, USA <sup>177</sup>University of Virginia, Charlottesville, USA <sup>178</sup>Wayne State University, Detroit, USA <sup>179</sup>University of Wisconsin - Madison, Madison, WI, USA

<sup>a</sup>Deceased.

- <sup>b</sup>Also at Vienna University of Technology, Vienna, Austria.
- <sup>c</sup>Also at IRFU, CEA, Université Paris-Saclay, Gif-sur-Yvette, France.
- <sup>d</sup>Also at Universidade Estadual de Campinas, Campinas, Brazil.
- <sup>e</sup>Also at Federal University of Rio Grande do Sul, Porto Alegre, Brazil.
- <sup>f</sup>Also at Universidade Federal de Pelotas, Pelotas, Brazil.
- <sup>g</sup>Also at Université Libre de Bruxelles, Bruxelles, Belgium.
- <sup>h</sup>Also at Institute for Theoretical and Experimental Physics, Moscow, Russia.
- <sup>i</sup>Also at Joint Institute for Nuclear Research, Dubna, Russia.
- <sup>j</sup>Also at Cairo University, Cairo, Egypt.
- <sup>k</sup>Also at Zewail City of Science and Technology, Zewail, Egypt.
- <sup>1</sup>Also at Fayoum University, El-Fayoum, Egypt.
- <sup>m</sup>Also at Department of Physics, King Abdulaziz University, Jeddah, Saudi Arabia.
- <sup>n</sup>Also at Université de Haute Alsace, Mulhouse, France.
- <sup>o</sup>Also at Skobeltsyn Institute of Nuclear Physics, Lomonosov Moscow State University, Moscow, Russia.
- <sup>p</sup>Also at Tbilisi State University, Tbilisi, Georgia.
- <sup>q</sup>Also at CERN, European Organization for Nuclear Research, Geneva, Switzerland.
- <sup>r</sup>Also at RWTH Aachen University, III. Physikalisches Institut A, Aachen, Germany.
- <sup>s</sup>Also at University of Hamburg, Hamburg, Germany.
- <sup>t</sup>Also at Brandenburg University of Technology, Cottbus, Germany.
- <sup>u</sup>Also at Institute of Nuclear Research ATOMKI, Debrecen, Hungary.
- <sup>v</sup>Also at Institute of Physics, University of Debrecen, Debrecen, Hungary.
- <sup>w</sup>Also at MTA-ELTE Lendület CMS Particle and Nuclear Physics Group, Eötvös Loránd University, Budapest, Hungary.
- <sup>x</sup>Also at IIT Bhubaneswar, Bhubaneswar, India.
- <sup>y</sup>Also at Institute of Physics, Bhubaneswar, India.
- <sup>z</sup>Also at Shoolini University, Solan, India.
- <sup>aa</sup>Also at University of Visva-Bharati, Santiniketan, India.
- <sup>bb</sup>Also at University of Ruhuna, Matara, Sri Lanka.
- <sup>cc</sup>Also at Isfahan University of Technology, Isfahan, Iran.
- <sup>dd</sup>Also at Yazd University, Yazd, Iran.
- <sup>ee</sup>Also at Plasma Physics Research Center, Science and Research Branch, Islamic Azad University, Tehran, Iran.
- <sup>ff</sup>Also at Università degli Studi di Siena, Siena, Italy.
- <sup>gg</sup>Also at INFN Sezione di Milano-Bicocca, Università di Milano-Bicocca, Milano, Italy.
- <sup>hh</sup>Also at International Islamic University of Malaysia, Kuala Lumpur, Malaysia.
- <sup>ii</sup>Also at Malaysian Nuclear Agency, MOSTI, Kajang, Malaysia.
- <sup>ij</sup>Also at Consejo Nacional de Ciencia y Tecnología, Mexico city, Mexico.
- <sup>kk</sup>Also at Warsaw University of Technology, Institute of Electronic Systems, Warsaw, Poland.
- <sup>11</sup>Also at Institute for Nuclear Research, Moscow, Russia.
- mm Also at National Research Nuclear University 'Moscow Engineering Physics Institute' (MEPhI), Moscow, Russia.
- <sup>nn</sup>Also at St. Petersburg State Polytechnical University, St. Petersburg, Russia.
- <sup>oo</sup>Also at University of Florida, Gainesville, USA.
- <sup>pp</sup>Also at P.N. Lebedev Physical Institute, Moscow, Russia.

- <sup>qq</sup>Also at California Institute of Technology, Pasadena, USA.
- <sup>rr</sup>Also at Budker Institute of Nuclear Physics, Novosibirsk, Russia.
- <sup>ss</sup>Also at Faculty of Physics, University of Belgrade, Belgrade, Serbia.
- <sup>tt</sup>Also at INFN Sezione di Pavia, Università di Pavia, Pavia, Italy.
- <sup>uu</sup>Also at University of Belgrade, Faculty of Physics and Vinca Institute of Nuclear Sciences, Belgrade, Serbia.
- <sup>vv</sup>Also at Scuola Normale e Sezione dell'INFN, Pisa, Italy.
- <sup>ww</sup>Also at National and Kapodistrian University of Athens, Athens, Greece.
- <sup>xx</sup>Also at Riga Technical University, Riga, Latvia.
- <sup>yy</sup>Also at Universität Zürich, Zurich, Switzerland.
- <sup>zz</sup>Also at Stefan Meyer Institute for Subatomic Physics.
- <sup>aaa</sup>Also at Istanbul Aydin University, Istanbul, Turkey.
- bbb Also at Mersin University, Mersin, Turkey.
- <sup>ccc</sup>Also at Piri Reis University, Istanbul, Turkey.
- <sup>ddd</sup>Also at Gaziosmanpasa University, Tokat, Turkey.
- eee Also at Adiyaman University, Adiyaman, Turkey.
- fff Also at Izmir Institute of Technology, Izmir, Turkey.
- <sup>ggg</sup>Also at Necmettin Erbakan University, Konya, Turkey.
- hhh Also at Marmara University, Istanbul, Turkey.
- <sup>iii</sup>Also at Kafkas University, Kars, Turkey.
- <sup>iii</sup>Also at Istanbul Bilgi University, Istanbul, Turkey.
- <sup>kkk</sup>Also at Rutherford Appleton Laboratory, Didcot, United Kingdom.
- <sup>111</sup>Also at School of Physics and Astronomy, University of Southampton, Southampton, United Kingdom.
- mmm Also at Monash University, Faculty of Science, Clayton, Australia.
- <sup>nnn</sup>Also at Instituto de Astrofísica de Canarias, La Laguna, Spain.
- <sup>000</sup>Also at Bethel University.
- <sup>ppp</sup>Also at Utah Valley University, Orem, USA.
- <sup>qqq</sup>Also at Purdue University, West Lafayette, USA.
- <sup>rrr</sup>Also at Beykent University.
- <sup>sss</sup>Also at Bingol University, Bingol, Turkey.
- <sup>ttt</sup>Also at Erzincan University, Erzincan, Turkey.
- <sup>uuu</sup>Also at Sinop University, Sinop, Turkey.
- <sup>vvv</sup>Also at Mimar Sinan University, Istanbul, Istanbul, Turkey.
- <sup>www</sup>Also at Texas A&M University at Qatar, Doha, Qatar.
- <sup>xxx</sup>Also at Kyungpook National University.