Advanced THz MIMO Sparse Imaging Scheme Using Multi-pass Synthetic Aperture Focusing and Low Rank Matrix Completion Techniques

Shaoqing Hu Member, IEEE, Chao Shu, Yasir Alfadhl, Senior Member, IEEE, and Xiaodong Chen, Fellow, IEEE

Abstract—This paper proposes an advanced THz multiple-input-multiple-output (MIMO) near-field sparse imaging scheme for target detection that uses single-pass synthetic aperture focusing and multi-pass interferometric synthetic aperture focusing techniques to improve imaging effectiveness and efficiency. It benefits from the MIMO of linear sparse periodic array (SPA) and random sparse imaging to reduce sampling data as well as system cost. Both simulated and proof-of-concept experimental results have verified the scheme, revealing that the single-pass synthetic aperture imaging approach is sufficient to identify pure metallic targets with 3.87% of $\lambda/2$ sampling data. And multi-pass interferometric synthetic aperture imaging approach is capable of improving image quality on image signal to noise ratio and contrast, which is ideal for detecting more challenging targets. The random sparse imaging with help of low rank matrix completion (LRMC) technique has shown promising potential of achieving equivalent image quality when further reducing 43.75% data in the experiment of 5-pass imaging on a complex target, this corresponds to 82.51% data reduction compared to $\lambda/2$ sampling.

Index Terms—Interferometric synthetic aperture radar (InSAR), low rank matrix completion (LRMC), multiple-input-multiple-output (MIMO), personnel screening, security detection, sparse periodic array (SPA), under-sampled sparse imaging.

I. INTRODUCTION

MICROWAVE and sub-millimeter wave imaging for target detection has been developed in last two decades, it faces low spatial resolution due to low operation frequency [1]–[6]. THz wave, referring to the frequency band between 100 GHz and 10 THz, has a short wavelength, non-ionizing characteristic and strong penetrating ability which is promising to applications for target detection or personnel screening [7]–[9]. This kind of imaging systems whatever frequency band is used can be categorized into passive, active imaging systems and their combination. The passive imaging system utilizes emissivity or temperature differences of objects to form the target images [10]–[15]. It is capable of achieving a fast imaging rate due to exempting from transmitting signal but challenging in achieving a sufficient sensitivity to detect a small noise equivalent temperature difference (NETD or NEAT) below 1K, which is desirable to detect items warmed up by body contact. On the contrary, the active imaging system is capable of achieving a superior imaging performance because of power source illumination and collecting the stronger reflections from target. The fast electronic scanning of a linear array integrated with mechanical scanning of array movement provides a possible solution to balancing the high frame rate and low system cost. The state-of-the-art MIMO array are used for electronic scanning [16]–[20] including multi-static linear sparse periodic array (SPA) [21]–[24], which has an advantage in reducing the array elements but maintaining high image quality. However, most MIMO imaging systems use sampling spacing on the order of $\lambda/2$ by Nyquist sampling criterion to avoid aliasing [22]. This will cause the increase of data acquisition time and system cost due to a large number of sampling points and channels at high frequency band. For example, there are 384 antenna elements in each of transmitter and receiver linear array imaging system working at 24.25-30 GHz [18] while a total of 736 Tx antennas and 736 Rx antennas are used in a planar imaging system working at 72-80 GHz [19]. We have investigated the feasibility of large sampling spacing in SPA for THz imaging. The maximum Tx or Rx element spacing is preferred to be determined by the interested field of view without incurring ghost images [25]. Large sampling spacing is applicable but it will cause image quality of signal to noise ratio (SNR) and contrast deteriorate, which is ideal for detecting pure metallic targets as demonstrated in this paper. This imaging approach is termed single-pass synthetic aperture focusing imaging. In addition, we investigated multi-pass interferometric synthetic aperture focusing technique to improve image quality [26]. Interferometric technique has been widely used in airborne synthetic aperture radar (SAR) and inverse synthetic aperture radar (ISAR) to form a 3D image [27]–[32]. It uses phase correlation resulting from either multiple receivers (usually 3) or different passes (usually 2) to gain the third dimensional information compared to traditional 2D SAR/ISAR image. It utilizes mono-static transceivers compared to the imaging distance with single or a few receivers [30]–[32]. However, we firstly apply multi-pass interferometric technique into near field THz sparse imaging system with multi-static MIMO array for potential application of security/personnel screening. It improves imaging performance without deploying more channels so as to maintain low system cost. We propose two detection working simultaneously called dual-mode operation that allows to cease the detection earlier, this will increase the detection efficiency compared to directly using $\lambda/2$ Nyquist sampling in one pass.
The other significant novelty of proposed work is integrating random sparse imaging into the multi-pass synthetic aperture focusing technique to reduce the sampling data, time and associated system cost. Sparse imaging with a linear sparse array and specific algorithm has been proposed [20]. However, the center frequency in operation is low as 35 GHz. In addition, the targets are three simplified metallic cylinders at a short distance of 0.5 m and the proposed algorithm would suffer from the heavy computational complexity for large or complex scenario. Another two most popular reconstruction algorithms for random sparse imaging are compressive sensing (CS) and low rank matrix completion (LRMC) [33], [34]. However, the performance of CS-based method depends on the design of measurement matrix [35] and it is sensitive to noise [36]. Besides, it will cost much PC resource and time to reconstruct images due to sparse representation (a round transformations between two domains). By contrast, LRMC technique is an alternative but superior technique to reconstruct the missing samples exempting from the sparse representation [37], [38]. With the advantages of high reconstruction accuracy, LRMC has gained interests in various applications, such as radar changing imaging [36], remote SAR imaging [39], [40] and the latest W-band 0.4m-SAR imaging for target detection [34]. However, there is very little discussion about THz sparse imaging with LRMC technique and multi-pass synthetic aperture focusing technique for target detection, far target distances in particular. Thus it has been proposed and investigated in this paper, achieving successful imaging at 220 GHz for detecting finer, more challenging targets at a far distance of 1.4 m (< 54.10 m of far field distance) in both simulation and proof-of-concept experiments. The results have demonstrated its capability of reducing sampling points as well as array elements but maintaining a high-quality image at THz band, which is particularly vital in reducing system cost of planar imaging systems.

In addition, another contribution of this paper is that a systematic approach of computational imaging simulation has been proposed that involves the theoretical analysis in MATLAB and computational electromagnetic imaging simulation with FEKO™. Computational imaging simulation is challenging due to a long distance of free space involved, especially at THz band of tiny mesh size. Thus, targets are usually simplified models like simple points, small scatters or metallic plates [2], [17], [34], [41], [42]. The proposed approach is capable of modelling various imaging scenarios.

The rest of paper is organized as follows. Section II introduces the fundamental theoretical analysis and computational electromagnetic (EM) simulation of an imaging scheme. Section III introduces the LRMC technique and corresponding simplified single value thresholding (SVT) algorithm for the proposed sparse random imaging. Section IV uses simulation examples to show the effectiveness of the proposed computational imaging simulation and LRMC-SVT-based image reconstruction. Section V gives proof-of-concept experiments and measured imaging results including single-pass synthetic aperture imaging and multi-pass interferometric synthetic aperture imaging of two kinds of targets: a pure metallic target and a complex target with dielectric substrate. Section VI and VII give discussions and conclusions.

II. SYSTEMATIC COMPUTATIONAL SIMULATION ON SYNTHETIC APERTURE IMAGING

Theoretical analysis using self-programmed codes leads to initial imaging system design while modeling and simulation using computational electromagnetic (CEM) software provides an effective way to optimize and validate the imaging performance prior to practical implementation. Therefore, a complete systematic simulation study approach including preliminary theoretical analysis in MATLAB and CEM imaging in FEKO™ has been proposed.

A. Theoretical Analysis in MATLAB

The MIMO array used also known as SPA consists of $N_t$ transmitter (Tx) elements with a spacing of $d_t$, half placed at two ends of the $N_r$ receiver (Rx) elements with a spacing of $d_r$ that equals to $0.5 \cdot N_t \cdot d_t$, as shown in Fig.1 [25]. The electronic scanning along one direction such as the horizontal direction shown in Fig.2 is achieved by sequentially switched on and off transmitter elements, when each transmitter is on, all receiver elements are used to record the echo data. The sequence number of SPA and corresponding Tx-Rx pairs for recorded data in each row is shown in Table I. Afterwards, the SPA moves to next position along the other direction, which is called mechanical scanning, and previous recording is repeated. This process is repeated until full aperture data are sampled [25]. This one (the number $N = 1$) planar scanning leads to single(one)-pass synthetic aperture imaging.

In order to improve imaging performance, an additional degree of freedom of SPA position along the electronic scanning direction with a step of $d_s$ is introduced. It can be either constant for simplicity or variable to achieve flexible sampling configuration. The total number is $N (> 1)$, donating $N$-pass. These muti-pass datsets are phase correlated so they can be mathematically focused with multi-pass interferometric synthetic focusing technique.

![Fig. 1. Linear Sparse Periodic Array.](image)

Therefore, we can gain a planar PSF of this SPA imaging system-the product of planar PSFs of transmitter and receiver

<table>
<thead>
<tr>
<th>Sequence</th>
<th>1st half</th>
<th>2nd half</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tx $^1$</td>
<td>Rx $^{N_r}$, Rx $^{N_r}$, Tx $^{N_t}$</td>
<td>Rx $^{N_r}$, Rx $^{N_r}$, Tx $^{N_t}$</td>
</tr>
<tr>
<td>$Rx^1$</td>
<td>$Tx^{N_t}$</td>
<td>$Rx^{N_r}$, $Tx^{N_t}$</td>
</tr>
<tr>
<td>$Rx^{N_r}$</td>
<td>$Tx^{N_t}$</td>
<td>$Rx^{N_r}$, $Tx^{N_t}$</td>
</tr>
</tbody>
</table>

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arrays, using Generalized Synthetic Aperture Focusing Technique (GSAFT) in

\[ PSF(SPA) = \sum_{n=1}^{N} \sum_{w=1}^{W} \sum_{p=1}^{Nt} \sum_{q=1}^{Nr} e^{jk(|\vec{R}_{to,n}^p,w| + |\vec{R}_{ro,n}^q,w|)}. \]  

which is also the imaging system response. The \( \vec{R}_{to,n}^p,w \) and \( \vec{R}_{ro,n}^q,w \) are the vectors in the \( n \)-th pass between the position of \( p \)-th transmitting antenna at \( w \)-th mechanical scanning position and the position of \( q \)-th receiving antenna at \( w \)-th mechanical scanning position to the target point \( o \).

Equation (1) depicts the 2D point spread functions whose slice cuts are the corresponding 1D point spread functions. PSFs provide a method to assess the imaging performance of cross range spatial resolution and artifacts. For example, Fig.3 shows the perspective view and top view of a PSF derived from (1). The first null implies the cross range spatial resolution while the side lobe level predicts how likely the artifacts arise.

In addition, the theoretical cross range resolution for an imaging or radar system can be predicted by

\[ \delta_{\text{cross-range}} \approx \frac{\lambda_c}{4 \sin(\theta/2) |\theta=\min(\theta_{HPBW},2\arctan(\frac{D}{L})|}, \]  

where \( \lambda_c \) is wavelength of center frequency, \( L \) is the scanning length along either direction, \( \theta \) is the minimum angle between Half Power Beam Width (HPBW) of receiver antenna and subtended angle by scanning aperture. For an aperture-limited imaging system in which target distance \( D \) is much larger than scanning aperture length or the receiver antenna has about 180° beam width, equation (2) can be approximated by

\[ \delta_{\text{limited-aperture}} \approx \frac{\lambda_c}{2 \cdot L} \cdot D, \]  

where \( 2 \cdot L \) replaced by the effective aperture length of \( L_d = L_t + L_r \) is widely used in SPA electronic scanning [25].

The theoretical range resolution can be predicted by

\[ \delta_{\text{range}} = \frac{c}{2B}, \]  

where \( c \) is light speed constant and \( B \) is operation bandwidth of imaging system.

Equation (1) \sim (4) give the theoretical analysis of resolutions and contrast (side lobe level) on an imaging system in MATLAB. Following on the design guideline we proposed in [25], it leads to the configuration of SPA and scanning intervals according to the desired imaging performance. The design will then be verified by computational electromagnetic simulation in FEKO™.

**B. Computational EM Imaging Simulation in FEKO™**

After the echo datasets (or S parameters) are collected, the corresponding multi-pass interferometric synthetic aperture focusing image can be reconstructed by multiplying S parameters and system response (PSF in (1)) as

\[ g(r_o) = \sum_{n=1}^{N} \sum_{w=1}^{W} \sum_{p=1}^{Nt} \sum_{q=1}^{Nr} S(\vec{R}_{to,n}^p,w, \vec{R}_{ro,n}^q,w) \cdot e^{jk(|\vec{R}_{to,n}^p,w| + |\vec{R}_{ro,n}^q,w|)}. \]

If \( N = 1 \), it is simplified as single-pass synthetic aperture focusing image. In addition to resolutions, image signal to noise ratio (SNR) defined by

\[ SNR_{image} = \frac{B_{\text{bright}} - B_{\text{dark}}}{\sigma(B_{\text{dark}})}, \]

can be used to quantitatively assess the image contrast (quality), where \( B_{\text{bright}} \) and \( B_{\text{dark}} \) are the mean brightness of the target area and non-target (dark) area. \( \sigma(B_{\text{dark}}) \) is the standard deviation of the non-target (dark) area brightness [43].

S parameters can be gained by computational electromagnetic (CEM) simulation that provides an effective way to evaluate imaging system prior to the practical implementation. Full wave solutions in CEM simulation provide reliable results but require fine mesh size and more PC resources. One of full wave solutions-multilevel fast multipole method (MLFMM)
in FEKO™ is much more efficient to reduce the memory complexity and solving complexity. Asymptotic solutions in CEM simulation including physical optics (PO) and ray-launching geometrical optics (RL-GO) provide reasonably accurate results by solving Maxwell Equations with appropriate assumptions and approximations. They save much PC resources and computational time when applied to electrically large targets [44], [45]. Therefore, FEKO™ is suitable for the imaging simulation that involves a long free space of target distance and large, complex targets. The featured hybrid solutions in FEKO™ that combines full wave and asymptotic solutions can facilitate simulation on challenging scenarios with less computational resources but providing required accuracy at the same time. For the simplest imaging scenario that only involves a small array and a pure small metallic target, it is suitable to use either the default method of moments (MOM) or hybrid solution of MLFMM/MOM. For the intermediate imaging scenario that involves a larger array, long target distance or large pure metallic target, the MOM/PO or MLFMM/PO hybrid solution can be adopted in which the MOM or MLFMM are used as the global solver while the PO is used as the local solver for the target. Besides, the large element physical optics (LE-PO) can be used instead of PO, which allows for much larger mesh size to save PC random-access memory and computational time. However, if the target includes the dielectric, the PO-based hybrid simulation method is not applicable. Thus, the RL-GO method can be applied in this imaging scenario. Geometrical optics (GO) leads to the mesh storage reduced remarkably, so it is very suitable for electrically large targets of perfect electric conductor and dielectric objects with multiple reflections. Taking mesh element size of triangular element as an example, the side length in MOM, MLFMM and PO should be shorter than approximately $\lambda/2$ and an edge length of $\lambda/10$ is preferred. The allowed edge length in LE-PO for when near field requests are present should be $2\lambda$. If only far field requests are present, the triangles only need to represent the geometry accurately, regardless of frequency or wavelength. For dielectric surfaces to be solved using the GO method, the mesh size is independent of the solution frequency so the maximum triangular mesh element size should be chosen such that the geometry of the surface is well represented. It is worth mentioning that the RL-GO in hybrid simulation can only be coupled with the MOM rather than MLFMM. It is indicated that the computational cost including PC resources and simulation time will reduce with later approaches but accuracy reduces because of assumptions and approximations used. Therefore, a simulation approach that properly meets demands should be chosen. Beside, if the array elements are uniform, we can use the equivalent source of element’s far field placed at the elements’ positions instead of the geometric model of array to further significantly save the computational time, this method is effective to deal with imaging scenario deploying a large array and its interaction with large targets [46].

In summary, the systematic work flow of this computational electromagnetic imaging simulation study has been concluded in Fig. 4. Based on the desired imaging specifications, the configurations of MIMO array (SPA) and mechanical scanning are firstly designed according to the analysis according to (1) $\sim$ (4) and design guideline we proposed in [25]. Then, the computational simulation is conducted in FEKO™ in which equivalent source simulation method might be adopted to save computational time and PC resources for complex imaging scenarios. However, the echo data (amplitudes and phases) need to be extracted by self-programmed lua scripts in Post-FEKO if equivalent source simulation is used. Thereafter, the simulated data are input to reconstruct the target image based on algorithm like GSAFT in (5).

**III. LOW RANK MATRIX COMPLETION TECHNIQUE FOR UNDER-SAMPLED SPARSE IMAGING**

Due to multi-pass phase correlated datasets, the sampling time and data processing load both increase. We aim to explore random sparse sampling and reconstruction approach to alleviate these issues. It is vital in implementing the planar imaging system which will remove part of the TR channels. The full $S$ parameters in (5) for reconstruction is $S_{full} = \{S_{Nr,Nr}\}_{n=1}^N$. They can be either fully sampled or approximated with few observations-random under-sampled data $S_{sparse}$ denoted in black and corresponding completed data by LRMC denoted in white, as shown in Fig. 5.

$$S_{sparse}(i,j) = P \cdot S_{full} = \begin{cases} S_{full}(i,j), & (i,j) \text{ sampled} \\ 0, & \text{otherwise} \end{cases}$$

where $P$ is a sparse sampling matrix consisting of 0 (black) and 1 (white) to deploy different sampling rate and pattern for study. In practical product, only active samples and associated channels can be implemented. According to related theory [37], [47], the missing echo can be completed by solving the following nuclear norm minimization optimization problem:

$$\text{minimize} \quad \|\hat{S}_{full}\|_*$$

subject to $\|\hat{S}_{full} - S_{sparse}\|_F \leq \delta$

where $\|\cdot\|_*$ is the nuclear norm of recovery matrix $\hat{S}_{full}$, which is the sum of its singular values [47], and $\|\cdot\|_F$ refers to
the Frobenius norm, which is the square root of the sum of the absolute squares of its elements. There are many algorithms to solve (8) such as Principal Component Pursuit by Alternating Directions and Single Value Thresholding (SVT) [37], [38], [48], which is not the focus of this paper. Thus we do not address details and have proposed to simplify the traditional SVT algorithm by removing specifying the number of singular values in computation [37], [47], as introduced in Table II

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Config.1</th>
<th>Config.2</th>
</tr>
</thead>
<tbody>
<tr>
<td>TR Separation (mm)</td>
<td>S&lt;sub&gt;TR&lt;/sub&gt; = 181</td>
<td>S&lt;sub&gt;TR&lt;/sub&gt; = 181</td>
</tr>
<tr>
<td>Element Pattern</td>
<td>Wide</td>
<td>Narrow</td>
</tr>
<tr>
<td>Target Distance</td>
<td>1.1 m</td>
<td>1.4 m</td>
</tr>
<tr>
<td>Resolution by (3) (mm x mm)</td>
<td>3.91 x 2.50</td>
<td>4.97 x 3.18</td>
</tr>
<tr>
<td>Subtended angle (x, y)</td>
<td>(9.98&lt;sup&gt;°&lt;/sup&gt;, 15.53&lt;sup&gt;°&lt;/sup&gt;)</td>
<td>(7.85&lt;sup&gt;°&lt;/sup&gt;, 12.23&lt;sup&gt;°&lt;/sup&gt;)</td>
</tr>
<tr>
<td>Resolution by (2) (mm x mm)</td>
<td>3.92 x 2.52</td>
<td>4.98 x 3.36</td>
</tr>
<tr>
<td>Image SNR (ISNR)</td>
<td>15.85 dB</td>
<td>23.11 dB</td>
</tr>
</tbody>
</table>

Wide: HPBW of about 42<sup>°</sup> with a peak gain of 12.95 dB at 220 GHz; Narrow: HPBW of about 12<sup>°</sup> with a peak gain of 23.68 dB at 220 GHz.

SNRs are calculated in Table III. The MIMO array in simulation consists of 8 Tx elements and 8 Rx elements in which the Tx element spacing <i>dt</i> is 6 mm. The mechanical scanning length is 0.3 m and the interval <i>dv</i> between sampling points is 4 mm. This sampling setting provides a FOV (field of view) of 0.192 m x 0.3 m. Two kinds of array elements with a wide beam (42<sup>°</sup> HPBW and peak gain of 12.95 dB) or narrow beam (12<sup>°</sup> HPBW and peak gain of 23.68 dB modelling the standard WR3 horn used in experiments) are compared in simulation. The theoretical resolutions along two directions can be roughly estimated by (3) or by equation (2) for a non-aperture limited imaging system. Tx array and Rx array are separated by 181 mm to imitate the experimental set-up, which causes more artifacts in background and deterioration on image SNR [25]. When the array element with narrow beam width of high gain is used, the image SNR is improved. More analyses and simulation of various scenarios can be referred to our previous work [25].

Fig. 6. Reconstructed single-pass synthetic aperture focusing images based on full simulated data (a) configuration 1 (ISNR=15.85 dB) (b) configuration 2 (ISNR=23.11 dB) and LRMC data of configuration 2 with (c) 40% (ISNR=17.38 dB) (d) 45% (ISNR=21.44 dB) sampled simulated data.

The theoretical resolutions along two directions can be roughly estimated by (3) or by equation (2) for a non-aperture limited imaging system. Tx array and Rx array are separated by 181 mm to imitate the experimental set-up, which causes more artifacts in background and deterioration on image SNR [25]. When the array element with narrow beam width of high gain is used, the image SNR is improved. More analyses and simulation of various scenarios can be referred to our previous work [25].

Fig. 5. Illustration of \( \hat{S}_{full} \) data.

**IV. COMPUTATIONAL IMAGING SIMULATION AND RESULTS**

Using above proposed method, we carried out computational imaging simulation study prior to the practical implementation. For example, there are two configurations listed in Table III. The corresponding reconstructed single-pass synthetic aperture focusing images are shown in Fig.6 and image

TABLE II

SIMPLIFIED SVT LRMC SPARSE IMAGING ALGORITHM.

| Input: | Sparse sampling matrix \( P \), under sampled matrix \( \hat{S}_{sparse} \), step size \( \delta \), tolerance \( \epsilon \), threshold \( \tau \), maximum iteration count \( k_{max} \) |
| Output: | Approximation full sampling matrix \( \hat{S}_{full} \) |
| Description: | Recover full sampling matrix \( \hat{S}_{full} \) from a under sampled subset \( \hat{S}_{sparse} \) |

1. Set \( Y^0 = \delta \hat{S}_{sparse} \)
2. for \( k = 1 \) to \( k_{max} \)
   - Compute \( [\Sigma^{k-1}, \Sigma^{k-1}, \Sigma^{k-1}] = \text{SVD}(Y^{k-1}) \)
   - Set \( r_k = \max \left\{ j : \sigma_j^{k-1} > \tau \right\} \)
   - Set \( X^k = \Sigma^{k-1} \delta P \cdot (\Sigma^{k-1} - \tau) \eta_{k-1}^{k-1} \)
   - if \( \| P \cdot (X^k - \hat{S}_{sparse}) \|_F / \| \hat{S}_{sparse} \|_F \leq \epsilon \) then break
   - Set \( Y^k = Y^{k-1} + \delta P \cdot (\hat{S}_{sparse} - X^k) \)
   - Set \( Y^k = P \cdot Y^k \)
3. end
4. Set \( \hat{S}_{full} = X^k \)
5. Reconstruct image with replacing \( S \) in (5) by \( \hat{S}_{full} \)

SVD represents Singular Value Decomposition, \( \Sigma^2 \) is a diagonal matrix with singular values \( \sigma_1, \sigma_2, \sigma_3, \ldots \).
studies [25], [46]. It is demonstrated that the computational analysis in MATLAB provides an effective approach to design the imaging scheme including array configuration, scanning aperture and mechanical sampling interval according to the desired practical imaging performance.

Furthermore, we tested the proposed LRMC sparse imaging algorithm only based on the simulated data of configuration 2, which is applied in proof-of-concept experiments. 40% and 45% sparse sampled data are used to retrieve the approximation of full sampling matrix and then reconstruct the target images, as shown in Fig.6(c) and Fig.6(d), respectively. It is worth mentioning that all these percentages (without referring to Nyquist λ/2 sampling) in this paper are calculated based on their corresponding reference data that is already a significant data reduction compared to Nyquist sampling data with half-wavelength-λ/2 interval. For example, the intervals along two directions in simulation are 3 mm and 4 mm. The generated full data as reference is only 3.87% of Nyquist sampling scheme with λ/2 sample interval. The results show that 40% data almost reconstruct the target image perfect except for more artifacts in background and little deformation on edges. When 45% data is used, the target image shows no visible difference from the reference and the image SNR achieves 21.44 dB, which is higher than the 17.38 dB of 40% data used and comparable to the 23.11 dB in reference. Thus, the proposed SVT LRMC sparse imaging algorithm has been preliminary verified feasible in simulation.

V. PROOF-OF-CONCEPT EXPERIMENTS AND RESULTS

The proof-of-concept experimental set-up is shown in Fig.7. Two THz mixer heads highlighted in blue are mounted on two linear horizontal scanning stages moving to each Tx and Rx element’s positions, imitating the Tx and Rx array of SPA respectively. Since the scanning stages are fixed, the target mounted on the head of PNF-XYV-0.9m × 0.9m scanning system moves vertically to inversely imitate a relatively mechanical scanning of the SPA to a fixed target. Besides, it changes N positions along horizontal (electronic scanning) direction to realize the N-pass movements of SPA inversely. Fig.8 shows the set-up of the whole system and the target under test mounted on the scanning system. The system under test uses a SPA consisting of Nt = 8 Tx elements and Nr = 8 Rx elements, the Tx element spacing dt is 6 mm so the electronic sampling interval is 3 mm. The horns utilized in the experiment are WR3 (220 ∼ 325 GHz) standard pyramidal horns with a peak gain of about 23.81 dB at 220 GHz and the typical output power from the THz mixer at 220 GHz is -13 dBm (0.05 mW) [25].

A. Pure Metallic Target with Smooth Surface

The target is a rectangular metallic plate (140 mm × 120 mm × 5 mm) having 10 holes with diameters ranging from 5 mm to 8 mm and the scanning length (width of field of view) is 192 mm. The mechanical scanning length is 0.3 m with an interval dv of 4 mm, and two experiments of target at 1.10 m and 1.40 m from the scanning plane are carried out. The number of different passes N is 4 and the step along x-axis is 20 mm. The current sampling configuration makes even total 4 passes data only occupies 15.50% of 1-pass Nyquist λ/2 sampling data. Fig.9 and Fig.10 show the reconstructed single-pass synthetic focusing images of two experiments. The corresponding multi-pass interferometric synthetic aperture images have been shown in Fig.11. There are 10 holes that can be identified in Fig.11 that is more than any image in Fig.9 and Fig.10. In addition, the artifacts in background (blue area) are less while the target image (red area) is more uniform, so the...
image SNR is obviously improved, as indicated in Fig.12. It is worth noting that the image SNRs in the second experiment of target placed at 1.4 m are higher due to targets within FOV defined as \(0.5 \cdot N_t \cdot N_r \cdot dt\) and widened beam-width with propagation [25].

![Fig. 9. Reconstructed single-pass synthetic aperture focusing images of target at (a) position x1 (b) position x2 (x1-20 mm) (c) position x3 (x1-40 mm) (d) position x4 (x1-60 mm).](image)

![Fig. 10. Reconstructed single-pass synthetic aperture focusing images of target at (a) position x1 (b) position x2 (x1-20 mm) (c) position x3 (x1-40 mm) (d) position x4 (x1-60 mm).](image)

![Fig. 11. Reconstructed 4-pass interferometric synthetic aperture focusing images of pure metallic target at (a) 1.1 m (b) 1.4 m.](image)

![Fig. 12. Image SNRs of pure metallic target in two experiments.](image)

### B. Complex Target including Metallic Pattern and Dielectric Substrate

In addition to the pure metallic target, the more challenging target of metallic patches etched on the dielectric substrate (260 mm × 180 mm × 1.6 mm) imitating the mannequin as shown Fig.13 have been tested. The target distance is 1.40 m and mechanical scanning length is 0.4 m with an interval of 2.5 mm, so the theoretical resolutions are 4.98 mm and 3.26 mm along horizontal and vertical directions according to (2). There are \(N = 5\) different passes with a step of 10 mm along x-axis. The current sampling configuration makes even total 5 passes data only occupies 31.00% of 1-pass Nyquist \(\lambda/2\) sampling data. The reconstructed single-pass images of the target have been shown in Fig.14(a) to Fig.14(e). The corresponding image SNRs as shown in Fig.15 range from 10.69 dB to 11.01 dB. The artifacts in the background are high while high power (red area) spreads on the non-metallic surface, which degrades image contrast indicated by low SNRs. It results from two factors. One is lower reflectively difference between metal and dielectric substrate. The other one is deteriorating focusing caused by much more scattering from the uneven surface of dielectric substrate. Thus, the proposed multi-pass interferometric synthetic aperture focusing technique is more desired to significantly improve the image quality and target identification. It has been verified in Fig.14(f) and the image SNR improves by about 4.06 dB.

### C. Image Reconstruction of Random Under-sampled Sparse Data with LRMC

Although the proposed multi-pass interferometric synthetic aperture focusing imaging helps to improve the image quality, it increases the sampling data/time. In addition, if we implement full planar electronic scanning system, the number of transceivers and hardware associated to samples are increased too. This will increase the system cost. Thus, we proposed to use random sparse under-sampling to reduce the number and LRMC technique to complete the missing samples, reconstructing the image on the basis of the simplified SVT algorithm in this paper. We only use the experimental data of more challenging target as a study case for brevity, 50% and
Fig. 13. The photographs of the experimental complex target including metallic pattern and dielectric substrate.

66.6% data of each single-pass scanning are investigated, this leads to 84.5% and 79.3% reduction compared to Nyquist $\lambda/2$ sampling data.

The reconstructed images are shown in Fig.16(a)∼16(b), respectively. And the image SNRs are listed in Table IV. As implied from the results, it is reasonable that more data will improve the image SNR, that is why the references have the highest image SNR. However, reconstructed images based on 66.6% data already show no visible difference from the references.

In order to demonstrate reducing the number of transceivers and related system cost, some of Tx/Rx elements in the SPA in each mechanical scanning position are randomly removed thus random sparse sampling is achieved. There must be more approaches to designing optimal “sparse” sampling patterns or aperiodic sparse arrays, which is not the focus of this paper so it will not be discussed due to limited pages. According to Table I, the number of $M_t$ Tx elements removed will cause samples missed one following one with an interval of $N_t/2$ samples while the number of $M_r$ Rx elements removed will cause samples missed one block, each block consist of $N_t/2$ samples, following one block with an interval of $N_r$ blocks. If both Tx and Rx elements are removed, there will be $N_t \cdot N_r$ Tx-Rx pairs overlapped so total of $M_t \cdot N_r + M_r \cdot N_t - N_t \cdot N_r$ samples are missed. For example, 17(a) shows a sparse sampling pattern with 1 Tx and 1 Rx elements removed in each row. Fig.17(b)∼17(d) show the reconstructed multi-pass images with 3 Tx & 3 Rx, 2 Tx & 2 Rx and 1 Tx & 1 Rx removed. The images SNRs are compared in Table IV. The results have shown that the scenario of 5 Tx & 5 Rx left (3 Tx & 3 Rx removed) is capable of providing an improvement than single-pass image. This improvement increases with more transceivers/data used so the scenario of 2 Tx & 2 Rx removed (56.25% and above data) is promising to achieve equivalent image quality to reference, this corresponds to 82.51% more data reduction compared to $\lambda/2$ sampling. The scenario of 1 Tx & 1 Rx removed provides 0.125 dB higher image SNR that, in addition to deviation, possibly benefits from random sampling pattern that is helpful to suppress the artifacts.

Fig. 14. Reconstructed single-pass synthetic aperture focusing images in experiment D2 of target at (a) position x1 (b) position x2(x1-10 mm) (c) position x3(x1-20 mm) (d) position x4(x1-30 mm) (e) position x5(x1-40 mm) and (f) corresponding 5-pass interferometric synthetic aperture focusing image.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Sampling Scheme</th>
<th>Image SNR / dB</th>
</tr>
</thead>
<tbody>
<tr>
<td>Samples removed</td>
<td>50% sampled data</td>
<td>12.538 (Fig.16(a))</td>
</tr>
<tr>
<td></td>
<td>66.6% sampled data</td>
<td>13.689 (Fig.16(b))</td>
</tr>
<tr>
<td>Tx &amp; Rx removed</td>
<td>3 Tx &amp; 3 Rx / 39.06% data</td>
<td>11.849 (Fig.17(b))</td>
</tr>
<tr>
<td></td>
<td>2 Tx &amp; 2 Rx / 56.25% data</td>
<td>13.315 (Fig.17(c))</td>
</tr>
<tr>
<td></td>
<td>1 Tx &amp; 1 Rx / 76.56% data</td>
<td>14.195 (Fig.17(d))</td>
</tr>
<tr>
<td>Reference-$S_{full}$</td>
<td>5-pass 100% data w/o LRMC</td>
<td>14.07 (Fig.14(f))</td>
</tr>
</tbody>
</table>

The percentages are calculated on the basis of Reference-$S_{full}$ data that is only 31.10% of 1-pass Nyquist $\lambda/2$ sampling data.

VI. DISCUSSION

In proof-of-concept experiments, it is demonstrated that the single-pass synthetic aperture imaging with large element spacing (such as 4.40$\lambda$ in this paper that leads to significant data reduction of $\lambda/2$ sampling ) is capable of identifying pure metallic targets, which saves the data acquisition time and system cost. The proposed multi-pass interferometric synthetic aperture sparse imaging technique improves the image quality
Fig. 15. Image SNRs of complex targets consisting of metallic pattern and dielectric substrate.

Fig. 16. Reconstructed multi-pass synthetic aperture focusing images with LRMC-SVT retrieved data based on (a) 50% (b) 66.6% sampled data.

but maintain the low sampling data ratio, which works as a complementary mode for more challenging targets. The reconstruction based on LRMC technique has demonstrated acceptable image quality in both single-pass synthetic aperture focusing image and multi-pass interferometric synthetic aperture focusing image. Therefore, the simplified operating procedures with a constant $d_s$ using such an advance imaging system for target detection can be summarized as follows:

1) Start, initialise $n = 1$, step value $d_s$ and pass number $N$ generated accordingly;
2) Scan and record $n$th-pass under sampled dataset;
3) Reconstruct $n$th single-pass synthetic aperture focusing image and if $n > 1$, reconstruct $n$-pass interferometric synthetic aperture focusing image simultaneously;
4) If target is identified, go to step 5) so cease the detection earlier, else if $n <= N$, $n = n + 1$, go to step 2);
5) End (successful target detection).

We admit that more effort might be demanded to make full use of the proposed imaging system, such as designing optimal pass step $d_s$, other potential 1D/2D sparse MIMO arrays or sampling patterns. Therefore, we hope more research and improvements will be followed up by either the authors or readers in the future.

**VII. CONCLUSION**

A systematic method of computational imaging simulation for target detection has been proposed. It not only leads to designing the sampling scheme for an imaging system but also provides an effective evaluation on the practical imaging performance.

The proposed THz MIMO sparse imaging scheme using multi-pass interferometric synthetic aperture focusing technique and LRMC technique has been verified in both simulation and proof-of-concept experiments. The multi-pass interferometric synthetic aperture focusing technique allows to improve the imaging performance without adding additional transceivers/channels. The LRMC technique enables to reduce the sampling time and system cost associated to transceivers but without compromising on the high image quality.

An novel dual-mode operation has also been proposed so they can operate simultaneously with help of real-time imaging algorithm. The image quality is increasing as new pass interferometric dataset is added. Also, the scanning and image reconstruction will cease earlier once the target is identified in either of two kinds of results, which is effective than directly using traditional $\lambda/2$ sampling scheme.

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**REFERENCES**


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