

## Article

# Numerical Study on Hydrogen–Gasoline Dual-Fuel Spark Ignition Engine

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**Abstract:** Hydrogen, as a suitable and clean energy carrier, has been long considered a primary fuel or in combination with other conventional fuels such as gasoline and diesel. Since the density of hydrogen is very low, in port fuel-injection configuration, the engine's volumetric efficiency reduces due to the replacement of hydrogen by intake air. Therefore, hydrogen direct in-cylinder injection (injection after the intake valve closes) can be a suitable solution for hydrogen utilization in spark ignition (SI) engines. In this study, the effects of hydrogen direct injection with different hydrogen energy shares (HES) on the performance and emissions characteristics of a gasoline port-injection SI engine are investigated based on reactive computational fluid dynamics. Three different injection timings of hydrogen together with five different HES are applied at low and full load on a hydrogen–gasoline dual-fuel SI engine. The results show that retarded hydrogen injection timing increases the concentration of hydrogen near the spark plug, resulting in areas with higher average temperatures, which led to NO<sub>x</sub> emission deterioration at –120 Crank angle degree After Top Dead Center (CAD aTDC) start of injection (SOI) compared to the other modes. At –120 CAD aTDC SOI for 50% HES, the amount of NO<sub>x</sub> was 26% higher than –140 CAD aTDC SOI. In the meanwhile, an advanced hydrogen injection timing formed a homogeneous mixture of hydrogen, which decreased the HC and soot concentration, so that –140 CAD aTDC SOI implied the lowest amount of HC and soot. Moreover, with the increase in the amount of HES, the concentrations of CO, CO<sub>2</sub> and soot were reduced. Having the HES by 50% at –140 CAD aTDC SOI, the concentrations of particulate matter (PM), CO and CO<sub>2</sub> were reduced by 96.3%, 90% and 46%, respectively. However, due to more complete combustion and an elevated combustion average temperature, the amount of NO<sub>x</sub> emission increased drastically.

**Keywords:** hydrogen direct injection; dual fuel; emission; CFD; spark ignition engine

## 1. Introduction

Fluid dynamics, thermodynamics and chemical reactions are three physical processes governing the reactive flow in computational fluid dynamic CFD. The process of fluid dynamics translates the balance of spatial convection and temporal evolution of the flow properties because of mass, momentum and energy conservation. Reactive fluid thermodynamics comprises microscopic heat transfer concerning work done by pressure, gas

molecules and corresponding changes in volume. Chemical reactions define chemical species generation/destruction considering mass conservation [1].

In automotive powertrain research and development, efficiency and engine tailpipe emission have been always two major parameters that should be addressed [2–4]. Renewable energy can be a source of hydrogen production with no negative effects on the environment and carbon footprint. The Laminar burning velocity of hydrogen is 207 cm/s, which is much higher than gasoline (41.5 cm/s). As can be seen in Table 1 [5], the unique properties of hydrogen make it very suitable for use in combustion engines.

Hydrogen is considered one of the most important and suitable energy carriers for engines in the future [6]. However, some technical problems such as low energy density and storage limitations have prevented its further development. Hydrogen is very suitable for use in combination with other fuels. Using hydrogen in combination with other fuels improves efficiency and reduces pollution, and also does not have storage problems. The dual mode can be the best alternative for hydrogen utilization in internal combustion engines (ICEs) owing to low energy density and storage difficulties [7,8]. Due to the high velocity of the hydrogen flame, the combustion process is accelerated, which leads to improved engine efficiency [9–11]. In addition, the high flammability range of hydrogen can make the combustion complete and stable. Even though hydrogen reduces the amount of PM and CO emissions, it increases NO<sub>x</sub> emissions [12]. There are two types of working principles in hydrogen/gasoline engines. In the first type, gasoline and hydrogen enter the cylinder as port fuel injection (PFI). In the second type, gasoline is a PFI, and hydrogen is injected directly into the cylinder. Compared to the second type, in the first type, hydrogen port injection causes air to be replaced by the hydrogen introduction, thus reducing the volumetric efficiency [13–17]. Several studies have been performed on SI engines with hydrogen and gasoline in a PFI strategy [18–24]. The result showed hydrogen addition can improve combustion efficiency and engine performance together with exhaust emission reduction, especially under lean burn conditions. Niu et al. [25] presented experimental research with hydrogen enrichment in gasoline SI engines with a remarkable excess air ratio of  $\lambda = 2.65$ . The results showed the addition of hydrogen reduced unburned hydrocarbons (HC) by up to 48.9%. Moreover, by adding 2% hydrogen, the thermal efficiency of the engine improved by 4.15%, and power output enhancement improved by 6.21% together with reductions in specific fuel consumption by 17% and NO<sub>x</sub> emissions by 26% [26].

**Table 1.** Fuel properties. Reproduced with permission from Li, G., etc., Int. J. Hydrog. Energy; published by Elsevier, 2019 [27,28].

Fuel Properties	Hydrogen (H <sub>2</sub> )	Gasoline
Diffusion coefficient (cm <sup>2</sup> /s)	0.61	0.16
Lower heating value (MJ/kg)	120	44
Laminar burning velocity (cm/s) (298 K, excess air ratio = 1, 0.1 MPa)	207	41.5
Flammability limit (excess air ratio)	0.14–10.08	0.6–2.4
Adiabatic flame temperature (K) (Excess air ratio = 1)	2318	2148

Many researchers have studied the hydrogen direct-injection strategy in SI gasoline engines [29,30] compared with gasoline PFI and have concluded that the former has better combustion efficiency and reduced emissions. Furthermore, hydrogen addition can reduce the coefficient of variation (COV) by stabilizing the ignition [8,24,31–36].

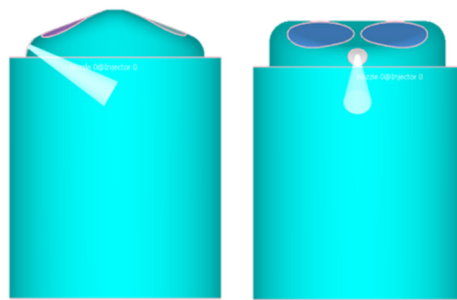
In the PFI strategy of hydrogen, since hydrogen replaces the intake air, it decreases engine volumetric efficiency. Moreover, due to the low energy density of hydrogen, individual hydrogen application as fuel requires a large fuel tank volume. Therefore, the best tradeoff can be the utilization of gasoline and hydrogen at the same time, where hydrogen is sprayed directly into the cylinder after the inlet valve is closed. In this paper, a numerical

investigation on the effect of injection timing and HES on combustion and emission characteristics of hydrogen/gasoline spark ignition engines is presented. Three different injection times of hydrogen along with five different HES were investigated to evaluate the effect of hydrogen addition on combustion efficiency and engine-out emissions.

## 2. Modeling Methodology

### 2.1. Engine Model

The experimental model of this study includes a single-cylinder research engine manufactured by Ford [37]. In the model under consideration, the engine speed is 1500 rpm and full load. The engine is equipped with two dedicated fuel systems. This system enables engine operation for both port injection of gasoline and direct injection of hydrogen at the same time. The arrangement of the injectors is illustrated in Figure 1. The direct-injection injector is placed between the inlet valves at an angle of 60 degrees to the cylinder axis. The study includes a comparison of gasoline port injection and different HES including 10%, 20%, 30%, 40%, and 50% hydrogen. The start of injection (SOI) has been selected for hydrogen direct injection at  $-120$ ,  $-130$  and  $-140$  Crank angle degree After Top Dead Center (CAD aTDC). The technical specifications of this engine are presented in Table 2. The compression ratio of this engine is 10.5. Combustion is stoichiometric in all functional states (equivalence ratio equal to 1).



**Figure 1.** Geometry of cylinder used in computational fluid dynamic (CFD) simulation. Reproduced with permission from Aghahasani, M., etc., Energy Convers Manag.; published by Elsevier, 2022 [38].

**Table 2.** Engine specifications and operational conditions. Reproduced with permission from Aghahasani, M., etc., Energy Convers Manag.; published by Elsevier, 2022 [38].

Parameters	Specification
Displacement (cm <sup>3</sup> )	626.4
Stroke (mm)	100.6
Bore (mm)	89.04
Compression Ratio (Geometric)	10.5:1
Number of Intake and Exhaust Valve	2/2
EVO/EVC (CAD aTDC fired)	150/−350
IVO/IVC (CAD aTDC fired)	350/−140

### 2.2. Solution Point

Turbulence modeling was performed with the RANS model (RNG k-epsilon). All settings of this modeling were done in CONVERGE software solution (Table 3). The engine speed is kept constant at 1500 rpm; the cylinder wall temperature is set at 450 K. The surface temperature of the piston and the temperature of the cylinder head are 450 K. hydrogen and gasoline were considered with the chemical formulas H<sub>2</sub> and IC<sub>8</sub>H<sub>18</sub>, respectively. Various combustion mechanisms were used for IC<sub>8</sub>H<sub>18</sub> and hydrogen, and a set of 152 reactions and 48 species in the CONVERGE solver was used to model combustion in a hydrogen/gasoline

engine [39]. Diagnostic modeling of NO<sub>x</sub> and soot was performed with the CONVERGE software solver. The extended Zeldovich thermal NO<sub>x</sub> model with mass scaling factor converting NO to NO<sub>x</sub> equal to 1.533 and the Hiroyasu-NSC soot model were used for modeling NO<sub>x</sub> and soot. In all cases, the total input energy is considered constant. The equivalence ratio for all cases is assumed to be 1.0. In addition to Table 2, which shows the performance and operation of the engine during tests, Table 4 also shows more of the operating performance of the test engine, which is also used to adjust the numerical solver.

**Table 3.** Sub-model group used in CFD simulation. Reproduced with permission from Li, G., etc., Int. J. Hydrog. Energy; published by Elsevier, 2019 [28,30].

Model of Parameters	Characteristics
Turbulence	RNG k-Model
Wall heat transfer	O'Rourke and Amsden Model
Combustion	SAGE
Ignition	Spark-energy Deposition Model

**Table 4.** Operational performance of engine. Reproduced with permission from Aghahasani, M., etc., Energy Convers Manag.; published by Elsevier, 2022 [38].

Parameter	Characteristics
Engine speed	1500 rpm
Equivalence ratio	1.0
Gasoline (E10) LHV(MJ/kg)	42.02
Hydrogen (H <sub>2</sub> ) LHV(MJ/kg)	120
Inlet pressure	1.06 bar

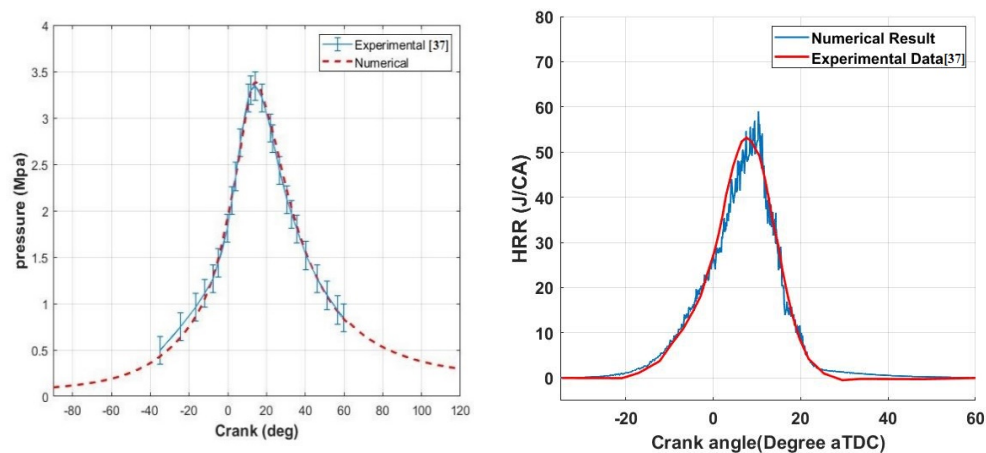
The hydrogen injector has been simulated using constant pressure (14 bar) boundary conditions. The diameter of the hydrogen inlet is 2.376 mm, and it is sprayed at an angle of 60 degrees to the vertical axis. In the case of 50% hydrogen, the duration of injection is equal to 20 CA, and for other percentages, injection duration is reduced so that the injection pressure is constant in all cases. In order to increase the accuracy of the simulation, two embeddings with scale 5 and also, in all stages of combustion, hydrogen-sensitive AMR (adaptive mesh refinement), have been applied in order to better simulate hydrogen combustion.

### 2.3. Numerical Model Validation

The simulation is implemented considering the engine operating at a low load (1500 rpm) with 0.55 bar of initial pressure and an initial temperature of 340 K (IVC). In this study, the boundary conditions of a constant pressure of 14 bar were applied for hydrogen fuel injection, so that for 50% hydrogen, the duration of fuel injection was about 20 CA. The instrumentation apparatus of the test setup is explained in Table 5. The simulation and experimental results presented [37] in the reference are compared to confirm the numerical results obtained from the CFD code of CONVERGE software. Figure 2 demonstrates the variation of pressure and heat release rate (HRR) with the crank angle for Gasoline PFI for a low load. The trends of simulation are similar to that of the experiment. For almost all points, the difference between the simulation and experimental pressure is less than 1.5 bar, and this difference is less than 1% for the maximum pressure point. As mentioned in reference [39], LFS (laminar flame speeds) data can be used to verify the results of hydrogen combustion. Validation has been done for 100% hydrogen and an equivalence ratio of 1 at WOT. As can be seen in Table 6, the simulation shows an acceptable accuracy in predicting the combustion details.

**Table 5.** Instrumentation apparatus for measurement. Reproduced with permission from Aghahasani, M., et al., *Energy Convers Manag.*; published by Elsevier, 2022 [38].

Apparatus	Production Type
Ignition timing	Motec M800
Injection timing (SOI)	Motec M800
Throttling Regulators	Parker Pilot
Fuel flow meter	Coriolis fuel meter CMF010
Crank angle position encoder	AVL 365X
In-cylinder pressure transducer	AVL GU21C



**Figure 2.** Validation of model by cylinder pressure and Heat Release Rate (HRR) for 100% gasoline port fuel injection. Reproduced with permission from Pamninger, M., et al., *Proceedings of the ASME 2016 Internal Combustion Engine Division Fall Technical Conference*; published by ASME, 2016 [37].

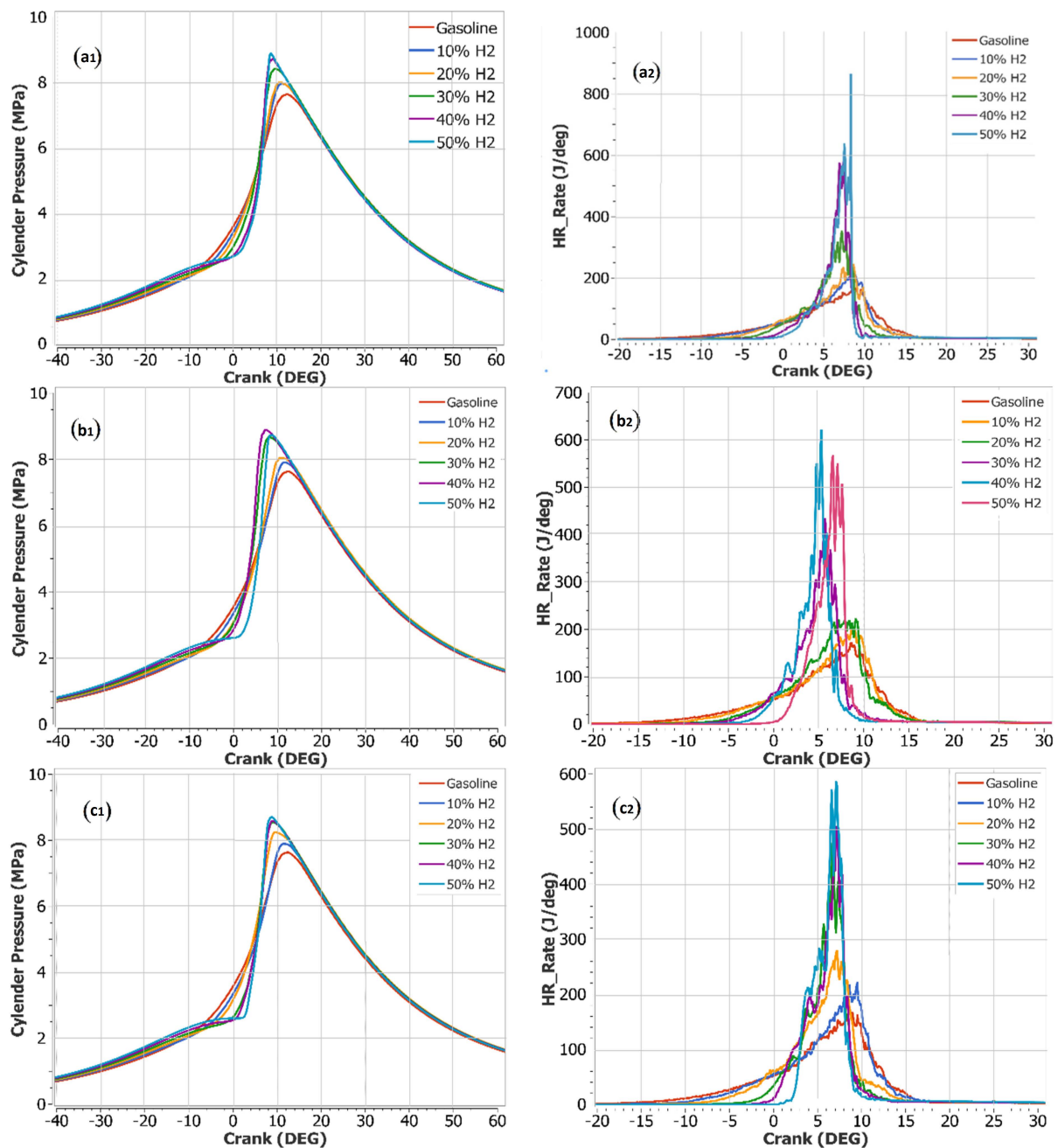
**Table 6.** Validation of LFS against measured data for  $R_{CNG} = 100\%$ .

LFS Measured Data (cm/s)	LFS Experimental (cm/s)	Error
201	198 [40]	1.5%
201	205 [41]	1.9%
201	197 [42]	2%

### 3. Results and Discussion

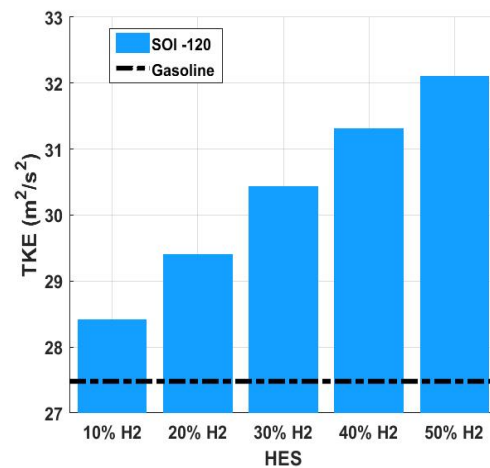
#### 3.1. Influences of Direct Injection of Hydrogen on Combustion

Figure 3 explains the effects of the direct hydrogen injection timing and HES on the cylinder pressure at full load. Both maximum pressure and combustion rate increase with increasing hydrogen. Two main reasons are given to explain this observation. The first one, since hydrogen has a higher flame propagation speed compared to gasoline, the combustion process behaves in a constant volume mode leading to increased maximum pressure. Second, hydrogen has a wider combustion limit that makes combustion more complete.



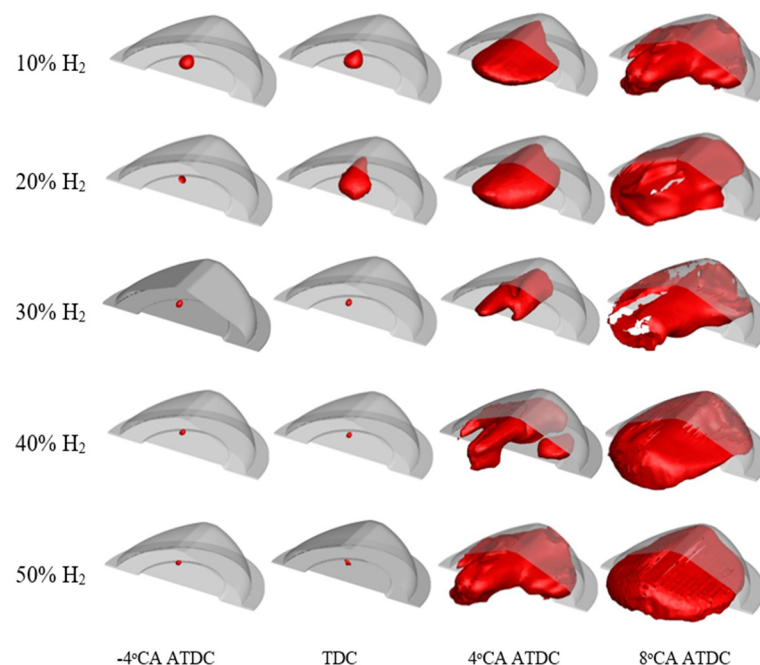
**Figure 3.** Effects of direct hydrogen injection timing and hydrogen energy share (HES) on the in-cylinder pressure and HRR for SOI (a1,a2) –120 crank angle degree after top dead center (CAD aTDC) (b1,b2) –130 CAD aTDC (c1,c2) –140 CAD aTDC.

Since the hydrogen is sprayed directly into the cylinder at high pressure, the hydrogen jet causes a better mixture which increases the turbulence. Therefore, fuel distribution in the mixture is higher and the combustion process is more efficient. As illustrated in Figure 4 with the addition of hydrogen, the amount of turbulent kinetic energy (TKE) increases, leading to faster and more complete combustion. This reduces the emissions and turns the combustion towards a constant volume process offering improved engine cycle efficiency.



**Figure 4.** Effects of HES on turbulent kinetic energy (TKE) for SOI –120 CA aTDC.

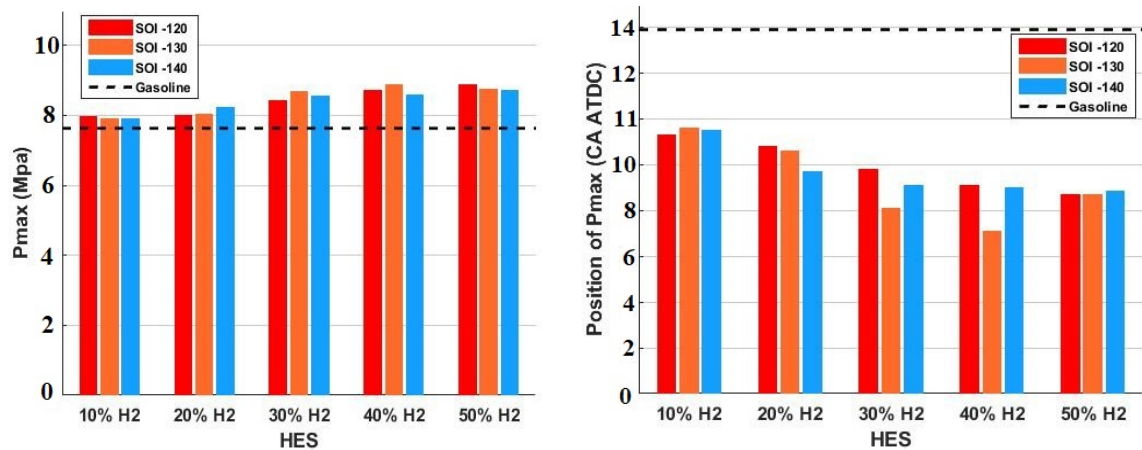
In order to reach the maximum output torque, the ignition timing in all cases is set in such a way that CA50 is in the range of 7–9 CA aTDC. Therefore, with the addition of hydrogen, the ignition time is delayed due to the higher combustion speed of hydrogen. As a result, for 10% and 20%, the hydrogen combustion rate is observed to be higher in the range of –4 CA aTDC to TDC. However, as can be seen in Figure 5, with the addition of hydrogen, the combustion rate has increased from TDC to 4 CA aTDC. As can be seen in Figure 5, by adding hydrogen, the speed of combustion has increased significantly. The main reason for this observation is the higher combustion speed of hydrogen compared to gasoline. A higher combustion speed causes a constant volume combustion process, which results in higher maximum pressure and improves thermal efficiency.



**Figure 5.** Flame propagation contours for different HES. Reproduced with permission from Agha-  
hasani, M., etc., *Energy Convers Manag.*; published by Elsevier, 2022 [43].

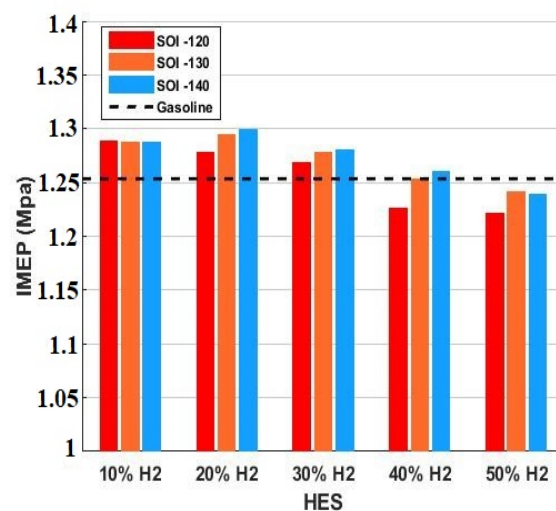
Figure 6 illustrates the maximum pressure and position of the maximum pressure to better illustrate the effect of the direct hydrogen injection timing and HES. Compared to gasoline, the maximum pressure of HES from 10% to 50% increases by an average of 3.8%, 6.1%, 12%, 14.4% and 15%, respectively, and the maximum pressure position advances by

27.9%, 34.8%, 43.4%, 47.2% and 45.1%, respectively. As shown in Figures 3 and 6, the faster the combustion rate, the higher the maximum pressure. Figure 3 illustrates the influence of the hydrogen direct-injection timing and HES on HRR. As the percentage of hydrogen increases, the HRR becomes more concentrated and more shifted in advance compared to the gasoline mode.



**Figure 6.** Effects of hydrogen direct-injection timing and HES on  $P_{MAX}$  and position of  $P_{MAX}$ .

Indicated mean effective pressure (IMEP) is employed as a factor for investigations on engine efficiency. Figure 7 describes the effect of the hydrogen direct-injection timing and HES on IMEP. Since engine IMEP is influenced by fuel-mixture homogeneity, there is better performance at SOI  $-140$  CAD aTDC, where hydrogen has more time to create a better mixture in the engine. With the increase of HES up to 30%, IMEP is more than pure gasoline, but when increasing the HES to 40% and 50%, because of hydrogen's low energy density, IMEP is reduced. The maximum amount of IMEP is related to the state of 20% HES [44,45].



**Figure 7.** Influences of hydrogen direct-injection timing and HES on indicated mean effective pressure (IMEP).

In all studied cases, the ignition timing is adjusted so that the CA50 is almost the same. By adding hydrogen, as seen in Figure 5, the combustion speed increases. Therefore, for higher hydrogen percentages, the ignition time is retarded, and this issue, as can be seen in Figure 8, causes the start of combustion (SOC) to be retarded. For hydrogen percentages higher than 20%, the SOC is after the top dead center. Therefore, the IMEP



decreases significantly for hydrogen percentages higher than 20%. Hydroxide is one of the most important parameters to understand and detect the SOC. As illustrated in Figure 9, in the TDC, with hydrogen addition, the OH decreased, which is a confirmation of the observations in Figure 8. The main reason for this issue is the retardation in the ignition timing to achieve the same CA50 for different cases.

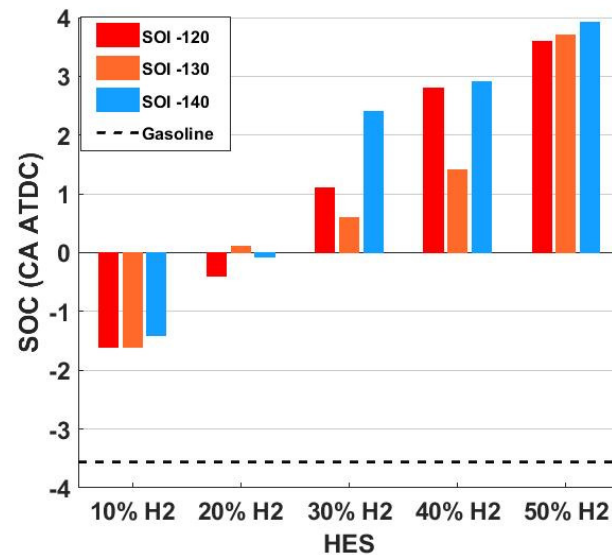


Figure 8. Start of combustion (SOC) for different case studies.

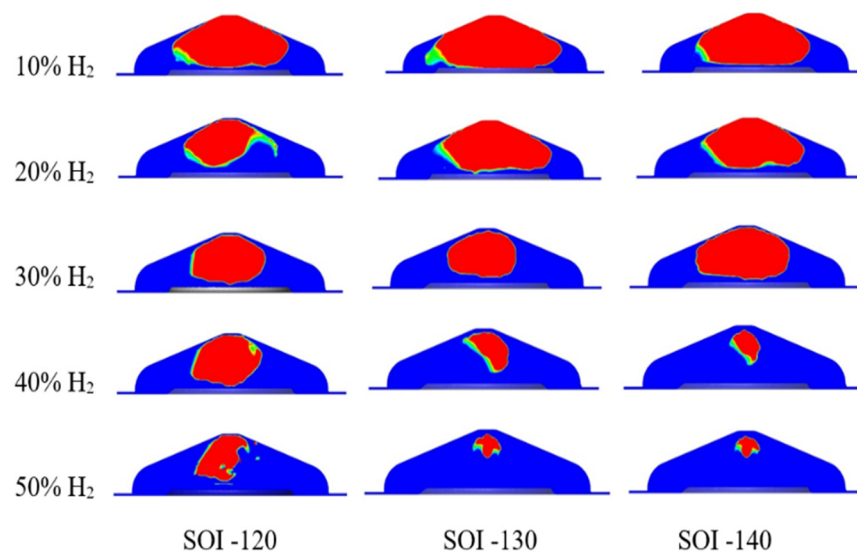
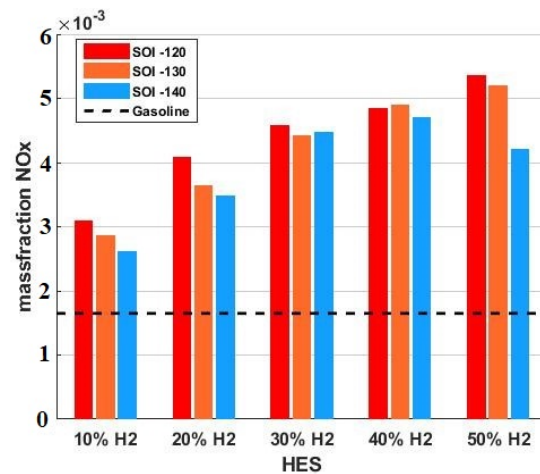


Figure 9. Contours of OH for different case studies at Top Dead Center (TDC).

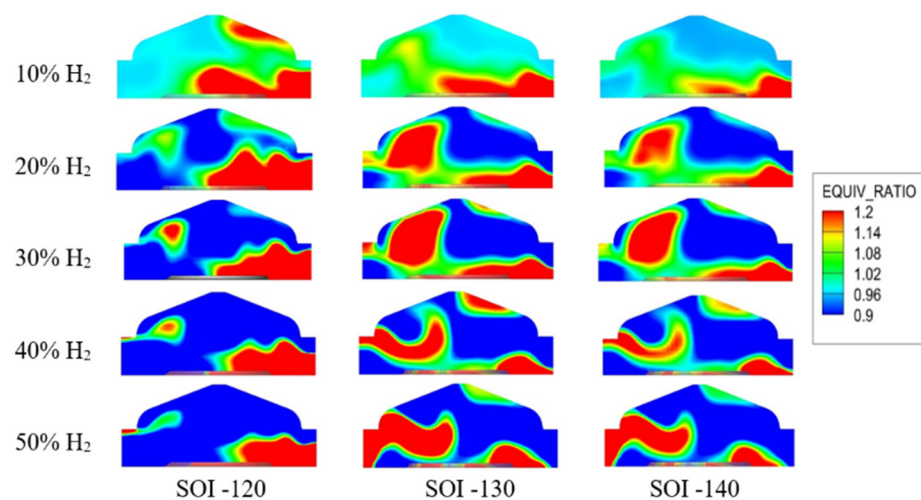
### 3.2. Influences of Hydrogen Direct Injection on Emissions

Figure 10 indicates the effect of the direct hydrogen injection timing and HES on  $\text{NO}_x$  emissions.  $\text{NO}_x$  emission behaves similarly to pressure and HRR. In this study, since the equivalence ratio is 1 and is considered uniform for all cases, the most important factor affecting  $\text{NO}_x$  emission is temperature. The hydrogen addition clearly raises the temperature inside the cylinder, so the  $\text{NO}_x$  also increases with increasing hydrogen.  $\text{NO}_x$  emissions for various HES from 10% to 50% increase by an average of 73.2%, 126.2%, 172.4%, 191.8% and 198.3%, respectively.

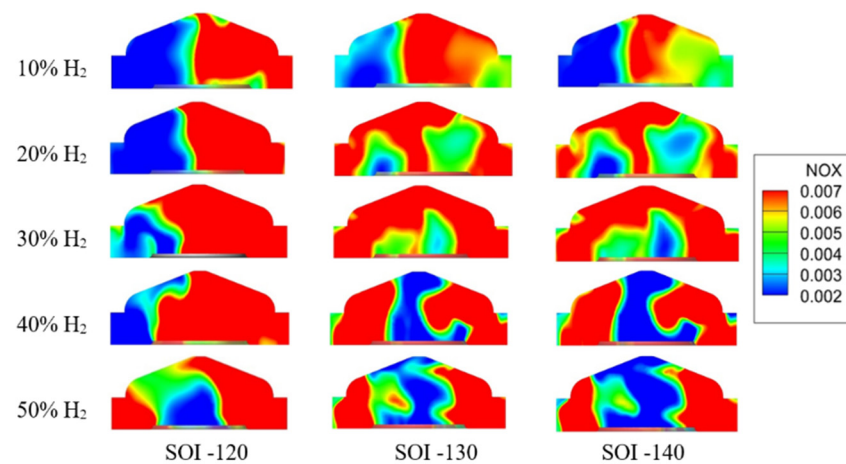


**Figure 10.** Influences of hydrogen direct-injection timing and HES on NO<sub>x</sub> emissions.

As shown in Figure 10, at the same HES, the SOI of  $-120$  CAD aTDC has the highest NO<sub>x</sub> emission. The main reason is that in this mode there is less time to create a homogeneous mixture, so some areas have a higher concentration of hydrogen than other areas, so the combustion temperature in these areas is higher than in other areas and more NO<sub>x</sub> is produced. In order to better understand this issue, the contours of the equivalence ratio and NO<sub>x</sub> are illustrated in Figures 11 and 12. Figure 11 shows that in the case of SOI  $-120$  CAD aTDC, due to retarded injection, there was less opportunity for homogeneous distribution of hydrogen, and therefore, most of the hydrogen was concentrated in only one area with high condensation. However, for SOI  $-130$  and  $-140$  CAD aTDC, due to more time to create a homogeneous mixture of hydrogen and air, the concentration of hydrogen in one area is reduced and different areas containing hydrogen are observed. As can be seen in Figure 12, in the areas where the concentration of hydrogen was higher, owing to the higher temperature of hydrogen combustion, more NO<sub>x</sub> emission is observed, and as the distribution of hydrogen becomes more homogeneous, NO<sub>x</sub> emission reduced, so for SOI  $-120$  CAD aTDC the most NO<sub>x</sub> emission has been observed. The more homogeneous distribution of hydrogen has an effect on other pollutants such as CO and PM and has led to a further reduction in these pollutants, which will be discussed further.

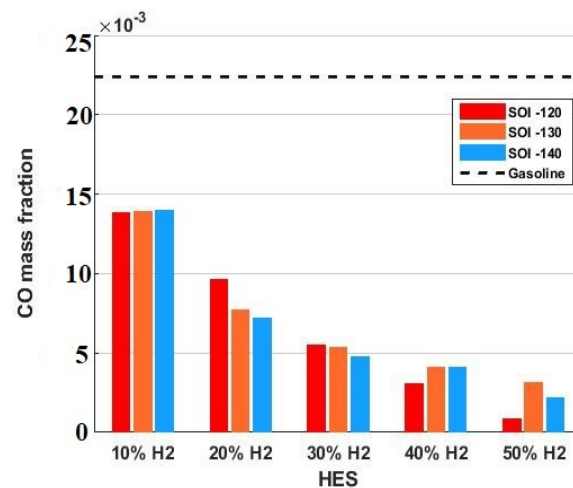


**Figure 11.** Contours of equivalence ratio for different case studies at  $-40$  CAD aTDC.



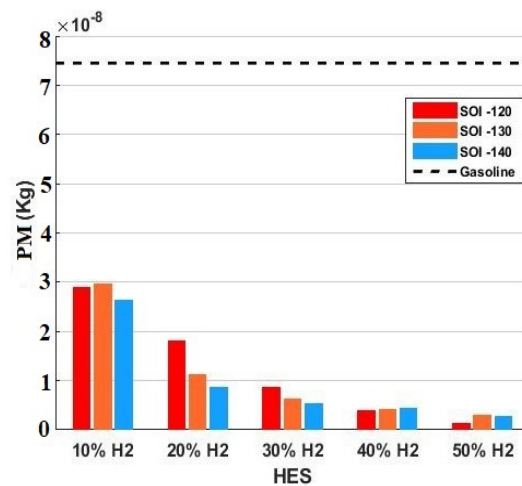
**Figure 12.** Contours of  $\text{NO}_x$  emissions for different case studies at 40 CAD aTDC.

Figure 13 shows the effect of the direct hydrogen injection timing and HES on CO emissions. Since hydrogen can make combustion more complete, CO emission is significantly reduced. Compared to gasoline, CO emissions for HES from 10% to 50% decrease by an average of 37.9%, 63.6%, 76.8%, 83.3% and 90.9%, respectively.



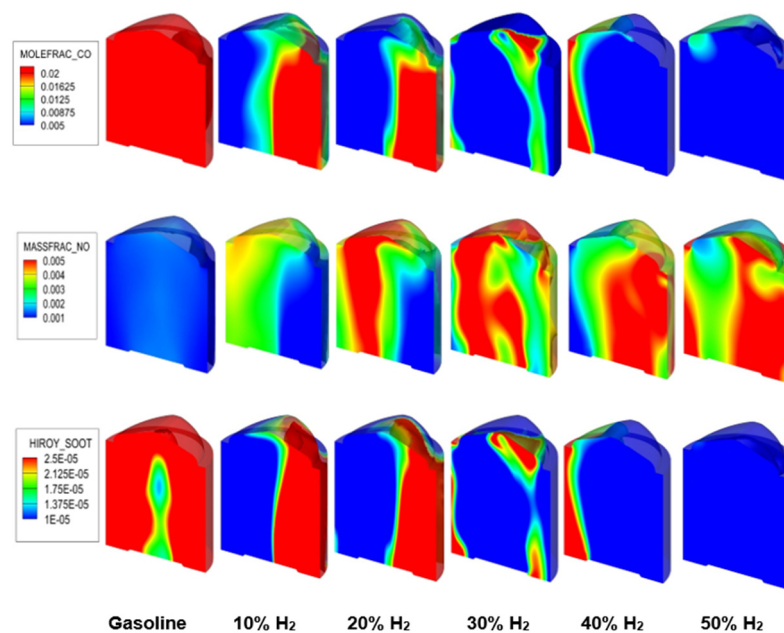
**Figure 13.** Effects of direct hydrogen injection timing and HES on the CO emissions.

Figure 14 presents the effect of the hydrogen direct-injection timing and HES on PM emissions. Since hydrogen combustion is more complete, it reduces the distance of wall quenching resulting in reduced PM emissions. PM emissions for HES from 10% to 50% decrease by an average of 62.1%, 83.1%, 90.9%, 94.4% and 96.9%, respectively, compared to gasoline. At the SOI of  $-140$  CAD aTDC, due to the longer time for more complete mixing, the homogeneous mixture is composed of hydrogen and more complete combustion takes place, so PM emissions show a greater reduction than in other cases.



**Figure 14.** Effects of direct hydrogen injection timing and HES on particulate matter (PM) emissions.

The contour of the changes for CO, NO<sub>x</sub> and PM emissions with an increase in HES at EVO and SOI – 120 aTDC are shown in Figure 15. As can be seen, with an increase in the percentage of hydrogen, CO and PM emissions decreased, which indicates more complete and clean combustion, but the NO<sub>x</sub> increased due to the higher combustion temperature of hydrogen.



**Figure 15.** Effects of HES on CO, NO<sub>x</sub> and PM emissions for start of injection (SOI) – 120 CAD aTDC at exhaust valve open (EVO).

#### 4. Conclusions

A numerical study was conducted to investigate the effect of direct-injected hydrogen in a port-fueled gasoline SI engine. The influence of hydrogen injection-timing variation and HES on combustion and emissions characteristics were evaluated. In general, direct injection of hydrogen enhanced IMEP and sped up the combustion process along with engine efficiency improvement. For HES 20%, IMEP increased by 3.52% compared to pure gasoline PFI. Compared to gasoline PFI direct injection of hydrogen for HES 10, 20, 30, 40 and 50%, CO emissions reduced by 37.9%, 63.6%, 76.8%, 83.3% and 91%, respectively. In the same manner, for HES 10% to 50%, PM emissions reduced by 62.1%, 83.1%, 90.9%,

94.4% and 96.9%, respectively. Hydrogen direct injection increased the combustion average temperature as well which led to a higher concentration of NO<sub>x</sub> emissions, especially in the case with SOI –120 CAD aTDC due to a more heterogeneous mixture than in the other cases. In contrast, NO<sub>x</sub> emissions for the case with SOI –140 CAD aTDC were lower than the other cases due to the more homogeneous mixture wherein NO<sub>x</sub> reduced by an average of 15.8%, 14.4%, 2.4%, 2.8% and 21.2%, for HES from 10% to 50%, respectively, compared to SOI –120 CAD aTDC.

**Author Contributions:** The authors confirm contribution to the paper as follows: Study conception and design, A.G. and A.M.A.; Simulation and data collection, M.A.; Analysis and interpretation of results: A.G. and A.M.A.; Draft manuscript preparation: M.A. and A.G.; Verification of the methods: A.M.A., M.M., J.K.; Supervision and investigation of findings: M.M., J.K., A.P. and T.M. All authors have read and agreed to the published version of the manuscript.

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**Conflicts of Interest:** The authors declare no conflict of interest.

## Abbreviations

aTDC	After Top Dead Center
bTDC	Before Top Dead Center
CAD	Crank angle degree
DI	Direct injection
CO	Carbon monoxide
CO <sub>2</sub>	Carbon dioxide
COV	Coefficient of variation
EVO	Exhaust valve open
EVC	Exhaust valve close
HES	Hydrogen energy share
HRR	Heat release rate
IMEP	Indicated mean effective pressure
IVO	Intake valve open
IVC	Intake valve close
ICE	Internal combustion engine
TKE	Turbulent kinetic energy
PFI	Port fuel injection
PM	Particle Matter
RI	Ringling intensity
SI	Spark Ignition
SOI	Start of injection
SOC	Start of combustion

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