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# State-of-Health Estimation of Lithium-Ion Battery Based on Constant Voltage Charging Duration

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Abstract: It is imperative to determine the State of Health (SOH) of lithium-ion batteries precisely to guarantee the secure functioning of energy storage systems including those in electric vehicles. Nevertheless, predicting the SOH of lithium-ion batteries by analyzing full charge–discharge patterns in everyday situations can be a daunting task. Moreover, to conduct this by analyzing relaxation phase traits necessitates a more extended idle waiting period. In order to confront these challenges, this study offers a SOH prediction method based on the features observed during the constant voltage charging stage, delving into the rich information about battery health contained in the duration of constant voltage charging. Innovatively, this study suggests using statistics of the time of constant voltage (CV) charging as health features for the SOH estimation model. Specifically, new features, including the duration of constant voltage charging, the Shannon entropy of the time of the CVcharging sequence, and the Shannon entropy of the duration increment sequence, are extracted from the CV charging phase data. A battery's State-of-Health estimation is then performed via an elastic net regression model. The experimentally derived results validate the efficacy of the approach as it attains an average mean absolute error (MAE) of only 0.64%, a maximum root mean square error (RMSE) of 0.81%, and an average coefficient of determination (R2) of 0.98. The above statement serves as proof that the suggested technique presents a substantial level of precision and feasibility for the estimation of SOH.

**Keywords:** lithium-ion batteries; health state estimation; constant voltage charging phase; machine learning

## 1. Introduction

In order to address the environmental issues stemming from traditional vehicle greenhouse gas emissions, the electrification of automobiles has emerged as a primary direction for the global automotive industry's transformation and upgrading, with a focus on energy conservation and emission reduction [1–3]. Against this backdrop, fuel cell electric vehicles, pure electric vehicles, and hybrid energy electric vehicles composed of lithium-ion batteries and fuel cells have come into existence. Fuel cell electric vehicles have garnered attention for their long-range and fast hydrogen refueling advantages [4,5]. Electric vehicles primarily utilize lithium-ion batteries as energy storage systems, offering the advantages of high overall energy efficiency and low operational costs [6–8]. Hybrid energy electric vehicles combine the strengths of fuel cells and lithium-ion batteries, achieving higher energy efficiency.

In order to ensure the efficient and safe operation of lithium-ion battery energy storage systems, the Battery Management System (*BMS*) is an indispensable component [3,9–12]. Furthermore, accurately estimating the *SOH* holds significant importance in *BMS* to diagnose the



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**Copyright:** © 2023 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). degree of battery life decay. These data play a vital role in guaranteeing the secure functioning of energy storage systems, as well as ensuring the reliability and range performance of electric vehicles [13–16].

Current studies have divided the techniques for evaluating the *SOH* into two categories: model-based and data-driven methodologies [17,18]. To perform model-based *SOH* estimation, researchers usually build models of lithium-ion batteries utilizing electrochemical models [19,20], equivalent circuit models [21–23], or empirical models [24,25]. This estimation identifies and estimates battery characteristic parameters by constructing physicochemical models through the computational processing of experimental data, thereby achieving a practical *SOH* estimation [17]. However, building battery models requires many multidimensional parameters, making parameter identification difficult. Choosing the right model that finds a middle ground between the precision of *SOH* estimation and computational sophistication is no easy task, leading to limitations in the practical application of model-based approaches.

Unlike model-based approaches, data-driven techniques obviate the need of prior knowledge on intricate battery deterioration mechanisms. Rather, they attain superior estimation precision via the analysis and processing of copious amounts of battery data [17]. As of late, data-driven techniques have garnered considerable interest. In particular, the estimation of *SOH* is deemed a customary regression quandary in data-driven methodologies. Among these methods, Support Vector Machine (*SVM*) [26–28], Relevance Vector Machine (*RVM*) [29], Long Short-Term Memory (*LSTM*) [30–32], Gaussian Process Regression (*GPR*) [33,34], and other techniques have been widely used. In order to precisely acquire the non-linear correlation between *SOH* and the external health attributes of batteries, prompt measures are required [35,36], and there is an increasing trend toward utilizing complex algorithms for model construction, increasing model complexity significantly. Therefore, it is imperative to streamline the model and enhance its computational efficiency while upholding its precision [17]. In addition to building efficient and well-performing algorithmic models, high-quality feature engineering directly enhances the criticality of *SOH* estimation methods.

Most existing research on feature engineering relies primarily on extracting health features for the *SOH* estimation from complete constant current and constant voltage (*CCCV*) charge–discharge curves. Ref. [37] has demonstrated that *CCCV* charging and discharging cycles can gather the majority of information required for battery health estimation. Ref. [38] incorporated the energy employed in the *CC* charging phase and equal discharge voltage intervals as input features. Ref. [39] proposed 14 features from the complete *CCCV* charge–discharge curve and selected eight features, including *CC* charge curve area, *CC* charge duration, *CV* charge duration, and their ratios, as health indicators. These methods achieved good estimation accuracy by extracting different features. However, these methods require collecting relatively complete *CCCV* charge–discharge systems greatly relies on the extent of battery charge and discharge, which is primarily determined by the operational demands of the load, which leads to some randomness in the starting point of charging. Therefore, applying *CCCV* charge–discharge curves to estimate the *SOH* of batteries in energy storage systems is challenging.

For achieving practicality in an *SOH* estimation, extracting health features based on relaxation voltage data is an effective solution. These methods extract features from the relaxation voltage data after battery charge and discharge, avoiding the randomness of the starting point of charging. In [40], relaxation time deviation voltage was extracted as a health feature. Ref. [41] employs a 30 s rest voltage to estimate the health status of the battery. Ref. [42] removed features from the 30 min relaxation voltage curve after the battery was fully charged, including the variance, maximum value, and skewness of the relaxation voltage. Although these methods do not require specific conditions and set voltage ranges, they still require the battery to be placed for an extended period to

extract features. Achieving an accurate *SOH* estimation with shorter sluggish times remains a challenge.

In the CCCV charging mode, the initial charging state does not have any impact on the process of charging the CV, which exhibits robustness to the previous discharge process. This has been observed in a recent study that emphasized on extracting health features using data from the CV charging phase [43]. CV charging refers to the battery continuing to charge at a constant voltage after the CC charging is completed. Based on the analysis above, using the CV charging phase data for feature extraction is unaffected by the starting point of charging and the waiting time required compared to the relaxation phase. Ref. [44] proposed using a CV to assess aging factors as health features. Ref. [45] utilized the time constant of the decoupled CV current as a metric for ascertaining health, which has proven to be effective. However, this approach entails a complex identification process for determining the appropriate parameters. To extract features directly from the CV charging phase, Ref. [46] suggested that the duration of CV charging may serve as a simple yet potent measure to gauge the SOH. Additionally, Ref. [43] developed a model for estimating the SOH focused on the duration of constant voltage charging while also accounting for the impact of the cutoff current on the length of said charging period, effectively improving the accuracy of SOH estimation. Ref. [47] extracted multiple time intervals of constant voltage current differences in the CV charging phase as features and demonstrated a strong correlation between time intervals and SOH. These methods have achieved an SOH estimation by extracting health features from the CV charging phase. However, a further improvement in the SOH estimation accuracy is constrained due to the insufficient exploration of the battery health information contained in the CV charging phase data.

To address the shortcomings identified in the existing literature mentioned above, this study utilizes statistical methods to extract battery health information from CV charging time data. It proposes a new set of feature combinations to enhance the SOH estimation accuracy. Initially, CV charging durations are extracted, and the charging durations are divided based on the intervals of CV currents. This results in CV charging duration sequences and CV charging duration variation sequences. Shannon entropy processing [48] is applied to both sequences, resulting in a feature combination composed of CV charging durations, the Shannon entropy of the CV charging duration sequence, and the Shannon entropy of the CV charging duration variation sequence. The Pearson correlation coefficient was wielded to validate the correlation of the three extracted features with the battery's SOH. A model for estimating the SOH was established using the Elastic Net Regression [49]. The estimation accuracy of the model was quantitatively analyzed using RMSE, MAE, and R2. T The effectiveness and superiority of the proposed method were confirmed by evaluating the feature combination's performance in estimating the SOH under various experimental conditions. The main contributions of this study can be summarized as follows:

- (1) Thoroughly delving into the abundant data about battery health found in the durations of *CV* charging and suggesting the implementation of *CV* charging duration statistics as indicators of battery health. A new health feature combination consists of *CV* charging durations, the Shannon entropy of the *CV* charging duration sequence, and the Shannon entropy of the *CV* charging duration sequence. The empirical evidence confirms that the suggested combination of features brings about an elevation in the accuracy of *SOH* estimation, enabling a more accurate estimation of the battery health status.
- (2) This study is completely dependent on the *CV* charging phase to extract features without being influenced by the initial charging point, adapting it for a wider array of application scenarios. In addition, when compared to relaxation phase feature combinations that necessitate lengthy idle periods, the precision of an *SOH* estimation is notably enhanced with the employment of the feature combination postulated in this paper.

## 2. Experimental Data Processing

## 2.1. Introduction to the Dataset

This paper compares and analyzes algorithms and models using the publicly available large-scale battery dataset from the Clean Energy Vehicle Engineering Center at Tongji University [42]. The batteries in the dataset undergo aging cycles in the laboratory. The dataset consists of three sets of data, all utilizing individual cylindrical 18,650 lithium-ion battery cells with repeatable charge–discharge cycles. Table 1 displays an overview of the dataset.

Dataset	Charge Voltage—Discharge Voltage (V)	Capacity in Ampere-Hours (Ah)	Cycle Temperature (°C)	Charge Current/Discharge Current Multiplier
			25	0.25/1
NCA	4 2-2 65	35	25	1/1
i vezri	1.2 2.00	0.0	35	0.5/1
			45	0.5/1
			25	0.5/1
NCM	4.2–2.5	3.5	35	0.5/1
			45	0.5/1
				0.5/1
NCM + NCA	4.2–2.5	2.5	25	0.5/2
				0.5/4

Table 1. Introduction to dataset loop conditions.

Dataset 1 battery cathode material is an NCA battery, and battery aging experiments were undertaken at 25 °C, 35 °C, and 45 °C, with charging current of 0.25 C, 0.5 C, and 1 C, and discharging current of 1 C, respectively. Dataset 2 battery cathode material is an NCM battery, and the battery aging experiment was performed under the conditions of 25 °C, 35 °C, and 45 °C, with a charging current of 0.25 C, and a discharging current of 1 C. Dataset 3 battery cathode material is NCM + NCA, and battery aging experiments were executed at 25 °C, with a charging current of 0.5 C, and discharge current of 1 C, 2 C, and 4 C, respectively. The battery cycling temperature cell dataset contains five processes of the complete cycle, i.e., *CC* charging, *CV* charging, post-charging relaxation, *CC* discharging, and post-discharge relaxation. In this paper, the battery cathode materials NCA, NCM, and NCM + NCA are used as the nomenclature of datasets 1, 2, and 3, respectively, and they serve the purposes of feature extraction, model training and testing, appraisal, and the enhancement of the overall effectiveness of the suggested approach.

#### 2.2. Feature Extraction

## 2.2.1. Data Preprocessing

All experiments are conducted on Python 3.11.4 version. To exclude the wrong values in the battery dataset due to experimental errors, measurement errors, recording errors, etc., the dataset is firstly rejected for outliers according to the lousy value range given by [42], i.e., the exclusion of battery data, exhibiting discharging capacities falling between 1650 mA·h and 2510 mA·h and bearing the highest values, guarantees the precision of the model's predictive results.

In view of the fact that the dataset encompasses the entire battery cycle process, it is imperative that the segment of the *CV* charging data needs to be localized. By finding all the constant voltage charging data segments in it and distinguishing them from the data segments of other stages, the change curve of battery voltage is utilized to determine the location of the *CV* charging stage.

Since the *CV* charging data segment has the characteristics of stable charging voltage and gradually decreasing charging current, the battery voltage will be stabilized at a fixed

value. By screening the voltage value, we can identify the precise placement of the *CV* charging phase. Once the location is confirmed, we can dissect and assess this stage so as to gain an in-depth insight into the battery's performance.

## 2.2.2. Feature Analysis

There is a robust correlation between the charging duration and the lithium-ion battery's maximum available capacity, defining the *SOH*. As the internal active materials and the electrolyte progressively degrade, the capacity of the battery decreases, its battery performance becomes less stable, and the charging duration may become more irregular and random. Therefore, this paper focuses on extracting constant voltage charging durations and their related statistical features, analyzing their correlation with the *SOH* estimation.

Shannon entropy is typically used to measure a sequence's uncertainty or randomness, as shown in Equation (1). Based on the above analysis, as the battery capacity decreases, the charging duration sequence exhibits randomness, and the Shannon entropy of the charging duration sequence may change. This can signify the declining pattern of battery capacity and act as a gauge in approximating the condition of battery health.

$$H(t) = \sum_{t}^{n} p(t_i) \log \frac{1}{p(t_i)}$$
(1)

where H(t) denotes the Shannon entropy of the continuous constant voltage charging time series signal *t*, and  $p(t_i)$  denotes the constant voltage charging time series, i = 1, 2, 3, ..., N.

Before calculating the Shannon entropy, it is necessary to segment the constant voltage charging curve. Figure 1 illustrates a schematic diagram of the division of constant voltage charging intervals. This paper adopts equal current intervals as the basis for segmenting constant voltage charging durations. The curve of constant voltage charging durations is divided into four intervals based on the values of the current, with the corresponding current values of boundary points as follows:

$$\begin{array}{c} 1400 \\ l_{1} \\ l_{2} \\ l_{3} \\ l_{4} \\ l_{5} \\ l_{5} \\ l_{4} \\ l_{5} \\ l_{4} \\ l_{5} \\ l_{4} \\ l_{5} \\ l_{4} \\ l_{4} \\ l_{2} \\ l_{4} \\$$

 $I' = [I_{41}, I_{42}, I_{43}, I_{44}, I_{45}]$ (2)

Figure 1. Schematic diagram of constant voltage charging interval duration division.

Recording the timestamp corresponding to each current value, where the timestamp corresponding to  $I_{41}$  is marked as  $t_1$ , the resulting time series is as follows:

$$t' = [t_1, t_2, t_3, t_4, t_5] \tag{3}$$

The constant voltage charging duration for each interval is calculated as follows:

$$t_{4,i} = t_{i+1} - t_i \tag{4}$$

where i = 1, 2, 3, 4.

The charging durations of each interval are combined to create a constant voltage charging duration sequence as follows:

$$t = [t_{4,1}, t_{4,2}, t_{4,3}, t_{4,4}] \tag{5}$$

On the basis of the constant voltage charging duration sequence given in (5), the difference between adjacent intervals' charging durations is calculated as follows:

$$\Delta t_j = t_{4,(j+1)} - t_{4,j} \tag{6}$$

where j = 1, 2, 3.

A constant voltage charging duration increment sequence is formed as follows:

$$t_{div} = [\Delta t_1, \Delta t_2, \Delta t_3] \tag{7}$$

The Shannon entropy of Equations (5) and (7) is calculated based on Equation (1), the Shannon entropy of the constant voltage charging duration sequence is obtained, defined as  $T_{sha}$ , and the Shannon entropy of the constant voltage charging duration increment sequence is obtained, defined as  $T_{sha2}$ . In the following section, we will explore the correlation between  $T_{cv}$ ,  $T_{sha}$ , and  $T_{sha2}$  as features and the *SOH*, in which  $T_{cv}$  represents the constant voltage charging duration.

## 2.2.3. Feature Correlation Analysis

To discern how the features and the *SOH* relate to one another, we treat them as two distinct variables and employ a correlation analysis methodology to ascertain the connection between their respective patterns and the intensity of correlation. In the correlation analysis, the Pearson correlation coefficient is customarily utilized to determine the extent of linear correlation between the two variables [50], as well as to assess the similarity between features and categories.

Here, the Pearson coefficient is utilized to scrutinize the correlation that exists among  $T_{cv}$ ,  $T_{sha}$ , and  $T_{sha2}$ , and the *SOH*. Correlation analysis experiments are conducted using batteries from the NCM + NCA dataset with a cycling temperature of 25 °C, a charging rate of 0.5 C, and a discharge rate of 4 C.

The Pearson coefficient represents the covariance ratio between two elements equal to the product of their respective standard deviations, as derived in Equations (8) and (9).

$$Cov(X, SOH) = E[(X - \mu_X)(SOH - \mu_{SOH})]$$
(8)

where *X* is the corresponding characteristic element,  $\mu_X$  is the standard deviation of the *X* element,  $\mu_{SOH}$  is the standard deviation of *SOH*, and *Cov*(*X*, *SOH*) is the covariance between *X* and *SOH*.

$$\rho = \frac{Cov(X, SOH)}{\sigma_X \sigma_{SOH}}$$
(9)

where  $\rho$  is the Pearson coefficient.

As per the evaluative metrics of the Pearson correlation coefficient, a higher absolute  $\rho$  value points towards a stronger correlation. Table 2 illustrates that the basic values of the

Pearson coefficients are higher than 0.95 for all three independent variables and the *SOH*, which unequivocally denotes a robust correlation.

Table 2. Pearson correlation degree of the characteristic.

Feature	Pearson's Correlation
$T_{cv}$	-0.99
T <sub>sha</sub>	0.96
T <sub>sha2</sub>	0.97

Figure 2a–c represent the Pearson correlation plots for the three features and the *SOH*. From the figures, it is evident that the feature  $T_{cv}$  has a pronounced negative correlation with *SOH*, while  $T_{sha}$  and  $T_{sha2}$  exhibit positive correlations with *SOH*.



**Figure 2.** Relationship plots between each feature and the *SOH*: (a)  $T_{cv}$ , (b)  $T_{sha}$ , and (c)  $T_{sha2}$ .

#### 3. Methodology

# 3.1. Mathematical Model of Elastic Net Regression

The Elastic Net Regression model is a form of linear regression that incorporates both *L*1 and *L*2 norms as regularization terms while undergoing training. Through the amalgamation of *L*1 and *L*2 regularization, the model becomes more stable, capable of better generalizing new data, and less susceptible to the influence of outliers or extreme values. Additionally, when dealing with a large amount of battery information, using Elastic Net Regression can control model complexity and prevent overfitting, which significantly aids in simplifying *SOH* estimation models.

In (10), the penalty term for Elastic Net Regression is illustrated to consist of a fusion of *L*1 and *L*2 regularization.

$$F(\omega) = \alpha(\mu \sum_{i=1}^{n} |\omega_i| + (1-\mu) \sum_{i=1}^{n} \omega_i^2)$$
(10)

Here,  $F(\omega)$  represents the penalty term for Elastic Net Regression,  $\alpha$  represents the regularization coefficient for Elastic Net Regression,  $\mu$  represents the mixing parameter that controls the weighting of *L*1 and *L*2 regularization in the combination, n signifies the number of features, and  $\omega_i$  stands for the coefficient for the *i*th feature.

The loss function for Elastic Net Regression is represented by Equation (11).

$$L(\omega) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\omega}(x^{(i)}) - y^{(i)})^2$$
(11)

Here, *m* is a data sample, and the '*i*th' sample's estimated *SOH* by the model is represented by  $h_{\omega}(x^{(i)})$ , while the actual *SOH* label for the '*i*th' sample is represented by  $y^{(i)}$ .

Due to the effective control of computational complexity, Elastic Net Regression can efficiently handle a large amount of battery data. When estimating the battery health status, Elastic Net Regression can rapidly extract critical information from a plethora of feature data, reducing data dimensionality. Therefore, using Elastic Net Regression simplifies data processing and modeling complexity, effectively conserving computational resources. It enhances the *SOH* estimation efficiency while maintaining the estimation accuracy.

## 3.2. SOH Estimation Method Based on Elastic Net Regression Model

Figure 3 depicts the overall framework for estimating battery health status using the Elastic Net Regression model. After thoroughly examining the tenets of the Elastic Net Regression model and taking into account the current circumstances surrounding lithium-ion batteries, we have crafted a model to estimate the *SOH* in accordance with the Elastic Net Regression.



Figure 3. Holistic framework for estimating battery health status based on Elastic Net Regression.

The following are the steps for constructing the model.

- (1) Data preprocessing: remove outliers, convert capacity to the *SOH* defined by capacity, and standardize the dataset.
- (2) Dataset construction: allocate the estimation dataset as a training set and a test set on a per-battery basis, with a 1:1 ratio of training batteries to test batteries.
- (3) Define input and output: use  $T_{cv}$ ,  $T_{sha}$ , and  $T_{sha2}$  as model inputs, with the corresponding *SOH* data as model output.
- (4) Set model hyperparameters: set the Elastic Net regression model parameters with the best regularization coefficient as 0.00001, and the Elastic Net mixing parameter as 0.1, representing a combination of *L*1 and *L*2 regularization penalties.
- (5) Train and test the SOH estimation model, and reverse standardize the output results.

## 4. Analysis of Experimental Results

# 4.1. Evaluation Metrics

This study employs three evaluation metrics, namely, *MAE*, *RMSE*, and *R*2, to gauge estimation accuracy. These metrics serve as vital benchmarks for assessing model performance in machine learning. Here is an introduction to these three evaluation metrics:

*MAE* is represented as the average of absolute errors, which is, in fact, a more general form of the average error. A smaller *MAE* value indicates a higher model accuracy. Its expression is as shown in (12).

$$MAE = \frac{1}{m} \sum_{i=1}^{m} \left| (SOH_i - \widehat{SOH_i}) \right|$$
(12)

where *m* denotes the quantity of samples,  $SOH_i$  stands for the factual maximum battery capacity, while  $\widehat{SOH_i}$  corresponds to the anticipated maximum battery capacity.

*RMSE* measures the average magnitude of errors in the measurements. A smaller value indicates a higher model accuracy. Its expression is as shown in (13).

$$RMSE = \sqrt{\frac{1}{m} \sum_{i=1}^{m} \left(SOH_i - \widehat{SOH_i}\right)^2}$$
(13)

The *R*2, referred to as the coefficient of determination, denotes the proportion of the entire data variance that a model is capable of accounting for. It serves as a performance metric for models and is commonly used for comparative analysis of different model performances. Its value ranges from [0, 1]. A higher *R*2 indicates a better model fit. Its expression is as shown in (14).

$$R^{2} = 1 - \frac{\sum_{i=1}^{m} (\widehat{SOH_{i}} - SOH_{i})^{2}}{\sum_{i=1}^{m} (\overline{SOH_{i}} - SOH_{i})^{2}}$$
(14)

#### 4.2. Comparison with Other Similar Features

For the purpose of validating the eminence of the proposed health attribute, constant voltage charging duration, this section contrasts the outcomes of experiments performed solely with it against the combined results of constant voltage charging duration and the remaining two statistical features. We investigate the performance of the feature combination, i.e.,  $T_{cv}$ ,  $T_{sha}$ , and  $T_{sha2}$ , proposed in this study, including the duration of CV charging, the Shannon entropy of the CV charging duration sequence, and the Shannon entropy of the CV charging the SOH.

#### 4.2.1. Comparison Experiment with Other Similar Features under the Same Condition

Three different conditions were randomly selected from the three datasets for analysis in the experiments conducted under the same conditions. In dataset NCA, conditions 1 and 2 were selected, where condition 1 represents batteries cycled at 25 °C, utilizing a charge current rate of 0.25 C alongside a discharge rate of 1 C. Condition 2 represents batteries cycled at 25 °C, with a charge current rate of 1 C, and a discharge rate of 1 C. In dataset NCM, condition 3 was selected, representing batteries cycled at 35 °C, with a charge current rate of 0.5 C, and a discharge rate of 1 C. In the dataset, NCM + NCA, conditions 4 and 5 were selected, where condition 4 represents batteries cycled at 25 °C, with a charge current rate of 0.5 C, and discharge rates of 1 C and 4 C. Condition 5 represents batteries cycled at 25 °C, with a charge current rate of 0.5 C, with a charge current rate of 0.5 C, and discharge rates of 1 C and 4 C. Condition 5 represents batteries cycled at 25 °C, with a charge current rate of 0.5 C, with a charge current rate of 0.5 C, and a discharge rates of 1 C and 4 C. Condition 5 represents batteries cycled at 25 °C, with a charge current rate of 0.5 C, with a charge current rate of 0.5 C, and a discharge rates of 1 C and 4 C. Condition 5 represents batteries cycled at 25 °C, with a charge current rate of 0.5 C, and a discharge current rate of 0.5 C, and a discharge rates of 1 C and 4 C. Condition 5 represents batteries cycled at 25 °C, with a charge current rate of 0.5 C, and a discharge rate of 1 C.

Tables 3 and 4 present the *SOH* estimation errors for different combinations of constant voltage features. As shown in the tables, when using only one constant voltage charging feature or combining them pairwise as health features, the *SOH* estimation errors are relatively large, and the estimation performance is not very stable. When using the feature combination proposed in this study to build the *SOH* estimation model, the average *MAE* and *RMSE* are the lowest, and the estimation accuracy is the highest. It can be observed that combining constant voltage charging duration with its statistical parameters under different operating conditions can achieve better estimation results, demonstrating that

using statistical parameters of constant voltage charging duration as features effectively complements the missing battery health information in constant voltage charging duration.

Condition	$T_{cv}, T_{sha}, T_{sha2}$			Only T <sub>cv</sub>		Only T <sub>sha</sub>			Only T <sub>sha2</sub>			
	MAE/%	RMSE/%	R2	MAE/%	RMSE/%	R2	MAE/%	RMSE/%	R2	MAE/%	RMSE/%	R2
Condition 1	0.38	0.53	0.97	1.14	1.69	0.72	0.45	0.60	0.96	3.07	3.38	-0.14
Condition 2	1.08	1.19	0.96	2.31	2.42	0.84	3.82	4.19	0.53	1.68	2.47	0.84
Condition 3	0.33	0.50	0.99	0.50	0.71	0.98	0.63	1.00	0.96	1.54	2.35	0.78
Condition 4	0.45	0.63	1.00	0.70	0.84	0.99	2.28	2.67	0.92	1.99	2.33	0.94
Condition 5	0.62	0.82	0.99	1.06	1.25	0.98	2.46	3.06	0.89	1.63	2.00	0.96
Cross Condition	0.98	1.20	0.98	1.09	1.35	0.98	2.52	3.04	0.89	2.03	2.48	0.93
<b>Overall Mean</b>	0.64	0.81	0.98	1.13	1.38	0.92	2.03	2.43	0.86	1.99	2.50	0.72

**Table 3.** *SOH* estimation error under the proposed feature combination and individual *CV* features.

The bolded numbers in the table indicate the average values of *MAE*, *RMSE*, and *R*2 for the proposed feature combination and individual *CV* features under different conditions.

Table 4. SOH estimation error under the proposed feature combination and its pairwise combinations.

Condition	$T_{cv}, T_{sha}, T_{sha2}$			$T_{cv}$ , $T_{sha}$		$T_{cv}, T_{sha2}$			$T_{sha}, T_{sha2}$			
	MAE/%	RMSE/%	R2	MAE/%	RMSE/%	R2	MAE/%	RMSE/%	R2	MAE/%	RMSE/%	R2
Condition 1	0.38	0.53	0.97	0.68	0.92	0.92	0.56	0.79	0.94	0.45	0.60	0.96
Condition 2	1.08	1.19	0.96	1.18	1.29	0.96	2.46	2.55	0.82	1.51	2.32	0.85
Condition 3	0.33	0.50	0.99	0.40	0.53	0.99	0.33	0.52	0.99	0.51	0.71	0.98
Condition 4	0.45	0.63	1.00	0.45	0.63	1.00	0.55	0.73	0.99	2.01	2.42	0.93
Condition 5	0.62	0.82	0.99	0.62	0.82	0.99	1.01	1.24	0.98	1.46	1.76	0.97
Cross Condition	0.98	1.20	0.98	1.00	1.22	0.98	1.12	1.37	0.98	2.03	2.52	0.93
<b>Overall Mean</b>	0.64	0.81	0.98	0.72	0.90	0.97	1.01	1.20	0.95	1.33	1.72	0.94

The bolded numbers in the table indicate the average values of *MAE*, *RMSE*, and *R*2 for the proposed feature combination and its pairwise combinations under different conditions.

Figure 4a–e displays the *SOH* fitting curves using the Elastic Net Regression model with different feature combinations under the same conditions. From the curves, it can be observed that the fitting effect of *SOH* using the feature combination proposed in this study is better, and it closely follows the real *SOH* curve compared to other feature combinations. The present study has effectively demonstrated that utilizing statistics related to the constant voltage charge duration as health indicators can duly enhance the precision of *SOH* estimation. This proved the superiority of the feature combination stated in the study.

#### 4.2.2. Comparison Experiment with Other Similar Features under the Cross Condition

An analysis was conducted using the NCM + NCA dataset as an example of crosscondition evaluation. The training and testing sets included batteries from three different conditions within the NCM + NCA dataset. Batteries underwent numerous cycles at an operating temperature of 25 °C, during which the charge rate was set at 0.5 C and the discharge rates were set at 1 C, 2 C, and 4 C.

Figure 5a–g shows scatter plots of the *SOH* estimates for different feature combinations under cross-condition conditions. In the illustration, the arrows indicate the direction of increasing density. It is evident from the figures that when using this specific feature combination for the *SOH* estimation, the estimation yields the best results, with the estimation points exhibiting the highest density along the actual *SOH* curve. Tables 3 and 4 display the *MAE*, *RMSE*, and *R*2 values for the *SOH* estimation under cross-condition conditions using these different feature combinations. Among them, the *SOH* estimation error is the smallest, and the fitting performance is the best when employing the proposed feature combination.



**Figure 4.** *SOH* estimation results for different feature combinations using the Elastic Net Regression Model under identical conditions: (**a**) condition 1, (**b**) condition 2, (**c**) condition 3, (**d**) condition 4, and (**e**) condition 5.

# 4.3. Comparison with Relaxation Features

In addition, this section conducts comparative experiments between the proposed feature combination and the relaxation stage feature combination. A comparison analysis is performed with the feature combination proposed in [42], which consists of relaxation voltage variance (*Var*), relaxation voltage skewness (*Ske*), and relaxation voltage maximum value (*Max*). This feature combination will be labeled as (*Var*, *Ske*, *Max*) in the following text.

# 4.3.1. Comparison Experiment with Relaxation Features under the Same Condition

This section uses the same experimental batteries as in Section 4.2.1 for five identical functional condition experiments. Figure 4a–e, respectively, display the *SOH* estimation results under identical conditions using the feature combination proposed in this study and the relaxation feature combination. The figures clearly show that the proposed combination of features yields superior fitting outcomes and bears a greater resemblance to the authentic *SOH* curve when juxtaposed with the relaxation feature.

The estimation error results for the *SOH* using the Elastic Net Regression model with two feature combinations under the same operating conditions are presented in Table 5, with *MAE*, *RMSE*, and *R*2 as evaluation metrics. As shown in the table, utilizing the feature combination proposed in this paper for the *SOH* estimation demonstrates a significant superiority, with an average *MAE* of 0.64%, an average *RMSE* of 0.81%, and an average *R*2 of 0.98. The estimation errors for each operating condition using the proposed feature combination are consistently lower than those with the relaxation segment feature combination, indicating a better fitting performance.



**Figure 5.** The scatter plots of *SOH* estimation points using different feature combinations with Elastic Net Regression under cross conditions: (a) proposed, (b)  $T_{cv}$ , (c)  $T_{cv}$  and  $T_{sha}$ , (d)  $T_{cv}$  and  $T_{sha2}$ , (e)  $T_{sha}$  and  $T_{sha2}$ , (f)  $T_{sha2}$ , (g)  $T_{sha2}$ , and (h) relaxation.

<b>Fable 5.</b> So	OH estima	ation error	based o	on Elastic	Net F	Regression	under	two f	eatures	combinatior	۱.

Condition		$(T_{cv},T_{sha},T_{sha2})$		(Var, Ske, Max)				
Condition	MAE/%	RMSE/%	R2	MAE/%	RMSE/%	R2		
Condition 1	0.38	0.53	0.97	0.63	0.87	0.93		
Condition 2	1.08	1.19	0.96	1.82	2.45	0.84		
Condition 3	0.33	0.50	0.99	0.79	0.93	0.97		
Condition 4	0.45	0.63	1.00	0.72	0.87	0.99		
Condition 5	0.62	0.82	0.99	1.17	1.28	0.98		
Cross Condition	0.98	1.20	0.98	1.38	1.83	0.96		
<b>Overall Mean Value</b>	0.64	0.81	0.98	1.09	1.37	0.94		

The bolded numbers in the table indicate the average values of *MAE*, *RMSE*, and *R*2 for two features combination under different conditions.

# 4.3.2. Comparison Experiment with Relaxation Features under the Cross Condition

This section utilizes the same cross-condition experimental conditions as in Section 4.2.2. Under these cross conditions, the *SOH* estimation errors using the feature

combination proposed in this study and the relaxation feature combination are presented in Table 5. Additionally, the scatter plots for the *SOH* estimation are illustrated in Figure 5a,h. The experimental outcomes clearly demonstrate that utilizing the suggested features in cross-condition experiments leads to considerably lower *SOH* estimation errors, signifying an overall improved fitting performance.

# 5. Conclusions

Based on the preceding discussion, we can summarize the main contributions and innovations of this study. Firstly, this study extensively explores the constant voltage charging duration, which contains rich information about the battery health status. We propose using *CV* charging duration statistics as a health feature, extracting feature combinations highly correlated with the health status of lithium-ion batteries during the constant voltage charging stage. Secondly, this study only relies on the *CV* charging phase for feature extraction, unaffected by the charging initiation point, making it applicable to a broader range of scenarios. It provides a practical and highly accurate battery health estimation solution for battery manufacturers, *BMS* manufacturers, and electric vehicle charger manufacturers. This contributes to improving the safety of lithium-ion battery energy storage systems. Additionally, it enables electric vehicle users to obtain more accurate information about the battery's health status, thereby advancing the safety of electric vehicles.

The experimental results indicate that the feature combination proposed in this paper achieves a high accuracy in the *SOH* estimation, with both the average *MAE* and *RMSE* less than 0.81%. The *R*2 is above 0.98, demonstrating a significant superiority. However, this study should be improved in the following directions. Firstly, considering that battery performance is influenced by other factors such as temperature and humidity, we will further explore the impact of environmental factors on the *SOH* estimation based on the above methods. Additionally, this study utilizes a laboratory battery dataset, lacking real-world application data, which may not fully account for battery performance in complex environmental conditions. Therefore, in the future work, to better align with real-world usage scenarios, we plan to collect real vehicle data to train and test the proposed method, making it more comprehensive in adapting to the complexity and variability of the real world.

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