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Abstract

Elemental segregation driven by the reduction of the total Gibbs energy of the system has been widely observed at the melt/substrate interfaces in various Al- and Mg alloys containing different inoculant

particles. This study provides experimental observations, analyses, and identifications of the formation of Y-segregation 2DCs at the Mg/MgO interfaces in a solidified Mg–0.5Y (w%) sample. From an extended Gibbs adsorption isotherm, the interfacial segregation of solute Y in a dilute Mg alloy melt is quantitatively described. The thermodynamics of the elemental interactions, conditions for the formation of MgO and  $Y_2O_3$  particles, and the contributions to the interfacial energy difference are detailed. A reasonable atomic segregation factor at the liquid/MgO interface from the bulk Mg–0.5Y melt is estimated. This changes the structural and chemical configuration at the interface, thus the nucleation potency of native MgO particles as well as the as-cast grain size.

Thermodynamics - Nucleation potency - Grain refinement - ICME

Keywords (separated by '-')



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## Thermodynamics of Mg–Y–O Alloys and Segregation at the Mg/MgO Interface

Rainer Schmid-Fetzer, Shihao Wang, and Zhongyun Fan

## Abstract

Elemental segregation driven by the reduction of the total 9 Gibbs energy of the system has been widely observed at 10 the melt/substrate interfaces in various Al- and Mg alloys 11 containing different inoculant particles. This study pro-12 vides experimental observations, analyses, and identifi-13 cations of the formation of Y-segregation 2DCs at the 14 Mg/MgO interfaces in a solidified Mg-0.5Y (w%) 15 sample. From an extended Gibbs adsorption isotherm, 16 the interfacial segregation of solute Y in a dilute Mg alloy 17 melt is quantitatively described. The thermodynamics of 18 the elemental interactions, conditions for the formation of 19 MgO and  $Y_2O_3$  particles, and the contributions to the 20 interfacial energy difference are detailed. A reasonable 21 atomic segregation factor at the liquid/MgO interface 22 from the bulk Mg-0.5Y melt is estimated. This changes 23 the structural and chemical configuration at the interface, 24 thus the nucleation potency of native MgO particles as 25 well as the as-cast grain size. 26

### Keywords

Thermodynamics • Nucleation potency • Grain refinement • ICME

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This study on elemental segregation driven by the reduction of the total Gibbs energy provides experimental observations, analyses, and identifications of the formation of Y-segregation two-dimensional-compounds (2DCs) at the Mg/MgO interfaces in a solidified Mg–0.5Y (wt.%) sample. It is shown that the segregation of Y occurs in the Mg–0.5Y melt, forming specifically Y<sub>2</sub>O<sub>3</sub> 2DC at the liquid-Mg/ {111}<sub>MgO</sub> interface and Mg(Y)–O 2DC monolayer at the liquid-Mg/{100}<sub>MgO</sub> interface. That is proven by dedicated electron microscopy, and a summary is depicted in Fig. 1 [1].

This changes the nucleation potency of native MgO particles as well as the as-cast grain size. That is demonstrated by grain refinement of commercially pure Mg treated by high shear melt conditioning, HSMC, before casting (CP Mg-HSMC), shown as a basis in Fig. 2, left-hand micrographs. Segregation of Y towards the highly dispersed native MgO particles in the melt after addition of 0.5 wt.% Y is suggested to improve the observed grain refinement in Mg– 0.5Y–HSMC, Fig. 2, right-hand micrographs. The average as-cast grain size is reduced from  $235 \pm 18 \,\mu\text{m}$  to  $106 \pm 4 \,\mu\text{m}$  [1]. The grain refining mechanism is attributed to the enhanced potency of {111} MgO particles (the predominant oxide in terms of population) modified by Y<sub>2</sub>O<sub>3</sub> 2DC, their dispersity and abundant number density, and the necessary growth restriction provided by 0.5 wt.% Y.

## Thermodynamics and Interfacial Energy

The thermodynamics of the elemental interactions, conditions for the formation of MgO and  $Y_2O_3$  particles, and the contributions to the interfacial energy difference are detailed below. From an extended Gibbs adsorption isotherm, the interfacial segregation of solute Y in a dilute Mg alloy melt is quantitatively described [1, 2]. It is suggested that

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Fig. 1 Graphical sketch of the electron microscopic methods and results to determine and distinguish the  $Y_2O_3$  2DC at the liquid-Mg/{111}<sub>MoO</sub> interface and Mg(Y)-O 2DC monolayer at the liquid-Mg/{100}<sub>MgO</sub> interface [1]

interfacial segregation is favored by (1) a negative difference 69 in interfacial energies approximated by  $\Delta \gamma = \gamma^i_{\rm Y(L)/MgO}$  -70  $\gamma^i_{Mg(L)/MgO}$  in this case, (2) a positive interaction term  $\Omega$  of a 71 regular solution between solvent and solute atoms related to 72 a positive enthalpy of mixing  $\Delta_{mix} H_{Mg-Y}^{Liquid}$ , and (3) a positive 73 difference in entropies of fusion between pure solvent and 74 solute  $\Delta S^i = \Delta_{\text{fus}} S_{\text{Mg}} - \Delta_{\text{fus}} S_{\text{Y}}$ . The three contributions are 75 considered separately below. 76

#### **Enthalpy and Entropy Contributions** 77

A strong attractive interaction among Mg and Y in the melt 78 is proven to exist from a comprehensive CALHAD assess-79 ment of that binary system [3] and the following data is 80 calculated from these thermodynamic parameters using the 81 Pandat software [4, 5]. A large negative value of the mixing 82 enthalpy with the minimum value of  $\Delta_{mix}H_{Mg-Y}^{Liquid} =$ 83 -10.6 kJ/mol at 41 at.% Y is obtained from the subregular 84 solution [3]. The approximation by a regular solution 85 equation to fit the dilute, Mg-rich range results in 86  $\Delta_{mix} H_{Mg-Y}^{Liquid,reg} = -14 \text{ kJ/mol at 50 at.\% Y, corresponding to}$ 87 the interaction term  $\Omega = -56$  kJ/mol. This strong negative 88 term impedes the interfacial segregation of Y. The 89

coordination numbers  $Z_{I} = 9$ ,  $Z_{V} = 12$ , Z = 13, in the nota-90 tion of Ref. [2], are used for the numerical calculations. 91 Although the value of the entropy difference,  $\Delta S^i =$ 92 2.837 J/mol/K calculated from Ref. [3], is positive it only 93 accounts for a small promotional contribution to the inter-94 facial segregation of Y. At 700 °C its contribution is about 18 times smaller compared to the impeding  $\Omega$  term.

## **Interfacial Energy Contributions**

The remaining impeding effect can be canceled if the value 98 of  $\Delta \gamma$  is negatively large enough. The interfacial energies of 99 pure liquid elements/MgO are not known. However, the difference  $\Delta \gamma$  can be predicted by solving Eq. (25) in Ref. [2] with the data given above. At 700 °C the limit is  $\Delta \gamma < -1.05 \text{ J/m}^2$  to result in enrichment of Y. The value of  $\Delta \gamma = -1.39 \text{ J/m}^2$  is obtained for reasonable atomic segregation of factor 10 with 1.37 at.% Y (4.8 wt.% Y) at the Liquid/{111} $_{MgO}$  interface from the bulk 0.137 at.% Y (0.5 wt.% Y) melt.

The sign of  $\Delta \gamma$  may be estimated to check the plausibility 108 of assuming  $\Delta \gamma < -1.05 \text{ J/m}^2$ . Clearly, the interface Mg(L)/ 109 MgO is non-reactive, whereas strong reactions are expected 110 at the Y(L)/MgO interface as shown later by inspection of 111

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Thermodynamics of Mg-Y-O Alloys and Segregation at the Mg/MgO Interface



**Fig. 2** Grain size of commercially pure Mg with highly dispersed native MgO particles, CP Mg–HSMC, left-hand micrographs (a, b), is significantly reduced by the addition of 0.5 wt.% Y enabling

the Mg–Y–O phase diagram. If interfacial reactions occur in metal/oxide systems, the interfacial energies and wetting are difficult to analyze [6] but, in general, the wetting tendency and work of adhesion are increased significantly compared to the non-reactive case [7].

The work of adhesion,  $W_X^{ad}$ , is the work against surface forces required to separate the pure liquid element X from a

segregation of Y in Mg–0.5Y–HSMC right-hand micrographs (c, d). Both melts were treated by high shear melt conditioning, HSMC, before casting [1]

ceramic substrate such as MgO. It is related to the three  $11^{19}$  interfacial energies involved,  $\gamma^{i}_{MgO/vapor}$ ,  $\gamma^{i}_{X(L)/vapor}$ , and  $\gamma^{i}_{X(L)/MgO}$  [7]:  $1^{21}$ 

$$W_{\rm X}^{\rm ad} = \gamma^i_{\rm MgO/vapor} + \gamma^i_{\rm X(L)/vapor} - \gamma^i_{\rm X(L)/MgO} \eqno(1)$$

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and to the experimentally determined contact angle  $\boldsymbol{\theta}$ 

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$$W_{\rm X}^{\rm ad} = \gamma_{\rm X(L)/vapor}^i (1 + \cos \theta) \tag{2}$$

Therefore, the difference in work of adhesion of reactive Y(L),  $W_Y^{ad-react}$ , and non-reactive Mg(L),  $W_M^{ad-Non-react}$ , on MgO is given as

$$W_{\rm Y}^{\rm ad-react} - W_{\rm Mg}^{\rm ad-Non-react} = \gamma_{\rm Y(L)/vapor}^{i} - \gamma_{\rm Mg(L)/vapor}^{i} - \gamma_{\rm Mg(L)/vapor}^{i} + \gamma_{\rm Mg(L)/MgO}^{i} - \gamma_{\rm Y(L)/MgO}^{i}$$
(3)

Inserting the difference in interfacial energies of the condensed phases,  $\Delta \gamma = \gamma_{Y(L)/MgO}^i - \gamma_{Mg(L)/MgO}^i$ , we obtain

$$W_{\rm Y}^{\rm ad-react} - W_{\rm Mg}^{\rm ad-Non-react} = (\gamma_{\rm Y(L)/vapor}^{i} - \gamma_{\rm Mg(L)/vapor}^{i}) - \Delta\gamma \gg 0$$
(4)

Assuming that the difference in surface tensions, the term 135 in the brackets in Eq. (4), is not dominant compared to  $\Delta \gamma$ 137 we obtain at least  $\Delta \gamma < 0$ , as required to cancel the remaining 138 impeding effect on Y-segregation detailed above. The value 139 of  $\Delta \gamma = -1.39$  J/m<sup>2</sup> related to a reasonable atomic segre-140 gation of factor 10 may not be quantitatively precise as it 141 depends on the accuracy of input data and assumptions in 142 the model. It is emphasized that a significant Y-segregation 143 towards the Liquid/MgO interface from the bulk Mg-0.5Y 144 melt is verified experimentally [1]. This changes the struc-145 tural and chemical configuration at the interface, thus the 146 nucleation potency of native MgO particles as well as the 147 as-cast grain size. 148

## **Thermodynamics and Phase Diagram**

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The thermodynamic conditions for the formation of bulk 150  $Y_2O_3$  particles in Mg-0.5Y, are revealed by the isothermal 151 section at 700 °C and ambient pressure of the Mg-Y-O 152 ternary equilibrium phase diagram. Figure 3 is calculated 153 using Pandat and the PanMg database [4]. The oxygen sol-154 ubility in liquid-Mg shown in the magnified Mg-rich part in 155 Fig. 3b was verified by the detailed analysis of the experi-156 mental phase diagram and thermodynamic data [8]. It shows 157 that the bulk Mg-0.5Y liquid alloy is saturated at 0.24 wt.% 158 O with MgO. This small oxygen content is readily picked up 159 from the ambient during melting because of the extremely 160 low partial pressure of  $O_2$ ,  $p(O_2) = 5 \times 10^{-54}$  bar, calculated 161 at the tie line Liquid + MgO. Therefore, MgO is the only 162 stable native oxide in that Mg-0.5Y alloy which is also 163 observed experimentally. This tie line also proves that the 164 interface Mg(L)/MgO is non-reactive whereas no tie line 165 exists from MgO to any Y-rich liquid indicating that strong 166 reactions are expected at the Y(L)/MgO interface, as stated 167 above. More than 3.9 wt.% Y in the liquid alloy is required 168 to expect  $Y_2O_3$  as the stable bulk oxide. The liquid phase 169 from 3.9 to 46 wt.% Y is in equilibrium with  $Y_2O_3$ . It is <u>1</u>70 interesting to note that under the assumed segregation of 171 factor 10 with 4.0 wt.% Y in the liquid monolayer at the 172 Liquid/{111}<sub>MgO</sub> interface one could obtain a local 173 three-phase equilibrium with Y<sub>2</sub>O<sub>3</sub> at that interface. 174



**Fig. 3** Isothermal section at 700 °C of the Mg–Y–O equilibrium phase diagram calculated by Pandat and PanMg: **a** complete composition range and **b** Mg-rich corner with Y content up to 8 wt.%

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Thermodynamics of Mg-Y-O Alloys and Segregation at the Mg/MgO Interface

## <sup>175</sup> Solidification Simulations

Finally, solidification simulations of the Mg–0.5Y–0.24O (wt.%) alloy, which is just saturated with MgO at 700 °C according to Fig. 3b, reveal the expected solid phases. The results obtained using the Pandat software are shown in Figs. 4 and 5.

Under equilibrium conditions, Fig. 4a, a tiny phase fraction of up to 0.2% of MgO grows from 700 to 647 °C due to the retrograde oxygen solubility in Liquid. From 647 to 643 °C, the bulk of (Mg) solid solution (Hcp) is formed (phase fraction from 0 to 99.27%) together with the growth

of MgO from 0.2 to 0.73%. Solidification terminates in this monovariant eutectic reaction, Liquid  $\rightarrow$  (Mg) + MgO at 643 °C without reaching an invariant ternary eutectic.

The distribution of solute Y between Liquid and (Mg) in 190 Fig. 4b starts at the initial 0.5 wt.% in Liquid and increases <u>1</u>91 rapidly from 0.5 to 2.3 wt.% Y during the bulk crystalliza-192 tion of (Mg). The (Mg) solid solution hosts from 0.1 to 0.5 193 wt.% Y in that secondary step from 647 to 643 °C. Only the 194 two-phase equilibrium (Mg) + MgO exists from 643 to 195 490 °C. At 490 °C the solubility of 0.5 wt.% Y at the apex 196 of the three-phase equilibrium  $(Mg) + MgO + Y_2O_3$  is 197 attained. Here we have a similarity to the 3.9 wt.% Y in the 198



**Fig. 4** Solidification simulation of the Mg-0.5Y-0.24O (wt.%) alloy under equilibrium conditions: **a** phase fractions shown up to 1% to reveal the minority phases, **b** distribution of solute Y between liquid and (Mg) phases





**Fig. 5** Solidification simulation of the Mg-0.5Y-0.24O (wt.%) alloy under Scheil conditions: **a** phase fractions shown up to 1%, **b** distribution of solute Y between liquid and (Mg) phases; note that the

average (total) wt.% of Y solute in (Mg) is plotted, ranging from 0.1 to 0.42 wt.% Y in the assumed layered growth of (Mg) under Scheil conditions

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liquid alloy at the apex of the three-phase equilibrium Liquid + MgO +  $Y_2O_3$  at 700 °C in Fig. 3b. Below 490 °C the solubility of Y at the three-phase equilibrium (Mg) + MgO +  $Y_2O_3$  decreases as shown in Fig. 4b and the liberated Y forms  $Y_2O_3$  at the cost of MgO in a solid-state reaction as given in Fig. 4a. The solubility of oxygen in (Mg) is negligibly small and both oxides MgO and  $Y_2O_3$  are stoichiometric phases in this ternary system.

The results of solidification simulation of the same alloy under Scheil conditions, explained in Ref. [9], are given in Fig. 5. Initially the phase development in Fig. 5a is exactly the same as under equilibrium because there is no solid solution in the primary crystallizing MgO. At 647 °C the bulk of (Mg) starts crystallizing in the same monovariant eutectic reaction, Liquid  $\rightarrow$  (Mg) + MgO. However, since back-diffusion of Y into the growing (Mg) phase is blocked the Y-enrichment in Liquid is huge, as shown in Fig. 5b. Below 640 °C Y<sub>2</sub>O<sub>3</sub> starts growing while the phase fraction of MgO is frozen-in at 0.7%; the reaction switches to Liquid  $\rightarrow$  (Mg) + Y<sub>2</sub>O<sub>3</sub> until the ternary invariant eutectic Liquid  $\rightarrow$  (Mg) + Y<sub>2</sub>O<sub>3</sub> + Y<sub>5</sub>Mg<sub>24</sub> reaction terminates solidification at 576.4 °C. The solidified non-equilibrium constitution comprises four phases, the phase fractions are also plotted for better readability down to the arbitrary cut-off at 550°C in Fig. 5b: 99.17% (Mg) + 0.70% MgO + 0.10% Y<sub>5</sub>Mg<sub>24</sub> + 0.03% Y<sub>2</sub>O<sub>3</sub>. That is considered a good approximation of the as-cast microstructure of that alloy. The very small fraction of 0.1% Y<sub>5</sub>Mg<sub>24</sub> may be too small to be detected. Also, the initial alloy is certainly not single-phase Liquid at 700 °C but contains more oxygen in the form of MgO which was observed experimentally as highly dispersed native MgO particles after treatment by high shear melt conditioning before casting [1]. That phase

231 267 268 fraction of MgO already present at 700 °C is simply added as inert basis to the MgO formed during the solidification simulations in Figs. 4a and 5a, at the cost of (Mg). This will reduce the tiny fraction of  $Y_5Mg_{24}$  even below 0.1%.

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