

# Synthesis of Biomass Combustion Fly Ash Derived Zeolites for CO<sub>2</sub> Adsorption: Optimisation of Hydrothermal Synthetic Pathway

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## Abstract

Industrial biomass combustion fly ash has been investigated as a precursor for zeolites with a view to evaluate the potential for adsorption of CO<sub>2</sub>. The synthesis methodology has been optimised *via* Design of Experiment by employing a Taguchi L9 array. Three variables were identified as statistically significant, the crystallisation temperature, crystallisation time and the liquid to solid ratio. Analysis of the main effects revealed an optimum set of conditions which produced a sample with the highest adsorption capacity of those prepared, 1.84 mmol g<sup>-1</sup> at 50 °C. This was a result of the conversion of the as-received fly ash into type A (LTA) and type X (FAU) zeolites after alkaline fusion with NaOH and hydrothermal treatment. The enthalpy of adsorption was estimated at -40.2 kJ mol<sup>-1</sup> and was shown to be dependent on surface coverage; the isosteric enthalpy of adsorption at zero coverage was -86 kJ mol<sup>-1</sup>. The working capacity of the adsorbent was maintained at 85% of the first adsorption uptake after a total of 40 cycles in a simulated temperature swing adsorption process (50 °C/150 °C adsorption/desorption). The equilibrium and kinetic CO<sub>2</sub> adsorption isotherms are presented and modelled through non-linear regression to reveal the adsorption mechanisms demonstrated by the fly ash-derived zeolites. Significant heterogeneity exists within the multi-phase zeolite which presents both micro and mesoporosity. The developed adsorbent presents a feasible route to valorisation of biomass combustion fly ash with good potential for application in the separation of CO<sub>2</sub>.

**Keywords:** Carbon Capture, Adsorption, Biomass Combustion Ash, Zeolite

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## Nomenclature

<b>Acronyms</b>	
ANOVA	Analysis of Variance
BET	Brunauer - Emmet - Teller
BFA/FA	Biomass Combustion Fly Ash/Fly Ash
BJH	Barret-Joyner-Halenda
CBU	Composite/Secondary Building Units
CCS	Carbon Capture and Storage
CCUS	Carbon Capture, Utilisation & Storage
CDR	Carbon Dioxide Removal
D4R	Double 4-rings
D6R	Double 6-rings
DAC	Direct Air Capture
DoE	Design of Experiment
EDS	Energy Dispersive X-Ray Spectroscopy
FAU	Faujasite
IPCC	Intergovernmental Panel on Climate Change
IPD	Weber & Morris Intraparticle Diffusion Model
IUPAC	International Union of Pure and Applied Chemistry
LTA	Linde Type A
MR	Member Ring
PFO	Pseudo First Order
PSO	Pseudo Second Order
RMSE	Root Mean Squared Error
SEM	Scanning Electron Microscopy
SESAMI	Script to Estimate the Surface Area of Materials from their Isotherms
SNR	Signal to Noise Ratio
TGA	Thermogravimetric Analysis
XRD	X-ray Diffraction
<b>Symbols</b>	
$S_{BET}$	Surface Area (BET)
$L/S$	Liquid to Solid Ratio
$T_{cry}$	Crystallisation Temperature
$t_{cry}$	Crystallisation Time
$NaOH/FA$	Sodium Hydroxide to Fly Ash Ratio
$P$	Pressure
$P_0$	Saturation Pressure
$\text{Å}$	Angstrom
$R_2$	Coefficient of Determination
$adj- R_2$	Adjusted $R^2$
$q_{max}$	Predicted Saturation Capacity
$K_T$	Toth Affinity Parameter
$n_T$	Toth Constant
$q_t$	Adsorbed Amount at Time t
$k_{IPD}$	Intraparticle Diffusion Model Rate Constant

1 **1. Introduction**

2 The first UK CCUS projects are due to come online in 2027 with further expansion anticipated  
3 throughout the decade. The intention for these clusters is to remove and store 20 – 30 Mt CO<sub>2</sub> per year  
4 by 2030 [1]. These efforts however, may not be sufficient to avoid the 1.5 °C warming by 2050 [2,3].  
5 The Intergovernmental Panel on Climate Change (IPCC) anticipates that current trends will lead to a  
6 breach of the 1.5 °C limit in the first half of the 2030s [4]. As a complement to the decarbonisation of  
7 power and industry, net Carbon Dioxide Removal (CDR) is gaining increasing attention, with most  
8 efforts aligned to either Direct Air Capture (DAC) [5] or Bioenergy with CCS (BECCS) [6]. BECCS  
9 can create a net-negative flow of CO<sub>2</sub> from the atmosphere into storage since CO<sub>2</sub> is sequestered in the  
10 biomass during growth; if this same CO<sub>2</sub> is then captured and stored at the end-use of the biomass (e.g.  
11 as a fuel in combustion) there is net-removal of CO<sub>2</sub> from the wider environment. In the UK, during  
12 their sixth carbon budget, the Committee on Climate Change estimated that BECCS could facilitate  
13 CO<sub>2</sub> removal of up to 22 Mt CO<sub>2</sub> per year by 2035 and up to 53 Mt CO<sub>2</sub> per year by 2050 [7,8]. In 2022,  
14 biomass provided 11 % of the UK’s 135 TWh of renewable generation making it the 2<sup>nd</sup> largest  
15 renewable energy source second only to the combined output of offshore and onshore wind power  
16 [9,10]. The largest power station in the UK, Drax power station, Selby runs exclusively on biomass  
17 (BE) and has ambitions to become carbon negative (BECCS) by 2030 [11].

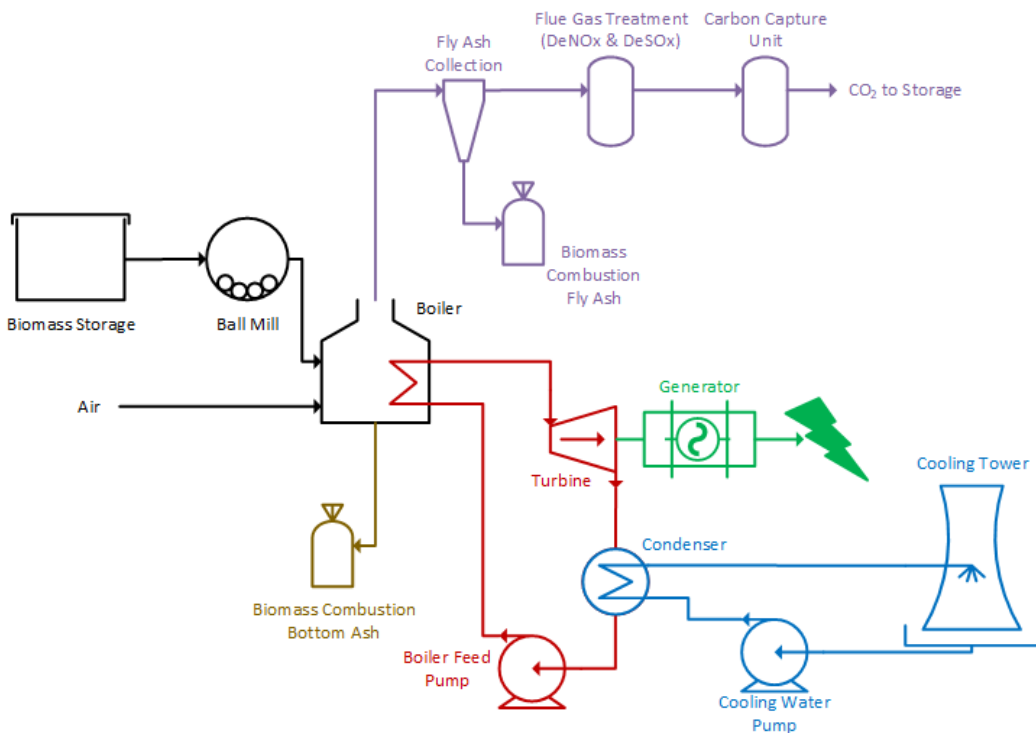


Figure 1: Schematic diagram of a thermal biomass-fired power plant.

18 Production of heat and electricity is typically achieved through combustion processes (Figure 1) and  
19 the industrial by-products of solid biomass or fossil fuel combustion consists of bottom and fly ashes.  
20 The former is dry or melt discharge and the latter from flue gas discharge systems, often electrostatic

21 precipitators or candle filters, or both. Raw biomass is a mixture of organic and inorganic matter, their  
22 ashes are generally embodied by a mixture of  $\text{SiO}_2$ ,  $\text{Al}_2\text{O}_3$ ,  $\text{CaO}$ ,  $\text{MgO}$ ,  $\text{K}_2\text{O}$ ,  $\text{Fe}_2\text{O}_3$ ,  $\text{P}_2\text{O}_5$ , and  $\text{SO}_3$  [12].  
23 There are however, significant variations in their compositions based on the biomass species used in  
24 the combustion process, growing conditions, harvest time/technique, transport and storage, method of  
25 processing and the combustion [13]. Biomass ashes present lower levels of toxic metals (vs coal) [14]  
26 and higher levels of alkali and alkaline earth elements [15]. This elevated alkali/alkaline earth metal  
27 renders them somewhat dissimilar to coal ashes and ultimately, owing to the range of variation, limits  
28 their secondary applications [16]. Considering the main constituents (silica and alumina) of these ash  
29 residues and the challenges associated with employing biomass-derived fly ash in typical secondary  
30 applications, these specific components could be recovered and employed in the synthesis of value-  
31 added products. Maximising the yield from such a waste, zeolites, a class of solid materials employed  
32 in adsorption and catalytic operations are extremely promising, a potential coup de grâce. Zeolite  
33 synthesis from waste residues is not a new research focus and has been of interest since the 1990s. There  
34 are however, limited studies pertaining to industrial-grade biomass combustion residues. Ash in the  
35 truest sense describes the residual solids after complete conversion of the solid precursor [17]. Despite  
36 this, most literature is inconsistent with this definition, and ash has often been referred to as any residue  
37 remaining after some physical or chemical conversion. The amount, chemical composition and size  
38 distribution of ash is highly dependent on the fuel and the form of the inorganic constituents as well as  
39 the configuration of the combustion system (temperatures, atmospheres), fuel preparation (*e.g.* grinding,  
40 washing) and boiler type [18]. The production of ash in a laboratory environment is inevitably unable  
41 to replicate both the temperature-profile and oxidising/reducing atmospheres within an industrial  
42 furnace. These factors have a significant effect on the physicochemical properties of the ash such as the  
43 development of particle structures, the fragmentation behaviour of char and ultimately the mechanism  
44 by which ash is formed [19].

45 The first CCS plants to come online will make use of absorption processes that require significant  
46 energy requirements for the regeneration of the working solvent [20]. An adsorption process operating  
47 *via* pressure or vacuum swing requires only a small pressure change to regenerate the adsorbent [21].  
48 Two classes of materials alternative to zeolites are often investigated for  $\text{CO}_2$  adsorption: carbonaceous  
49 adsorbents and metal-organic frameworks (MOFs). Carbonaceous materials in their non-functionalised  
50 form present good hydrophobicity but relatively weak interactions with  $\text{CO}_2$  [22]. This weak interaction  
51 can lead to a low adsorption capacity and selectivity at low partial pressures. When tuning both the  
52 textural properties (pore size, volume, surface area) through activation or surface functionality through  
53 modification/doping, these can be improved, often quite significantly [23]. Doping with nitrogen,  
54 however, typically increases the enthalpy of adsorption (and selectivity of  $\text{CO}_2/\text{N}_2$ ) but to the detriment  
55 of moisture sensitivity [24]. MOFs, arguably encompass a larger class of materials than that of zeolites  
56 and are characterised by extremely high specific surface areas and hence, comparable adsorption

57 capacities at elevated pressure [25,26]. In the context of post-combustion carbon capture, MOFs can be  
 58 less suitable as CO<sub>2</sub> partial pressures are typically much lower (0.05 – 0.15 bar(a)) and the interaction  
 59 between these materials and CO<sub>2</sub> is often lower than that exhibited by zeolites. Due to this, zeolites are  
 60 often able to reach their maximum CO<sub>2</sub> uptake at low adsorption pressures. This phenomena is a result  
 61 of the strong electrostatic interactions between CO<sub>2</sub> and the zeolite framework cations (Figure 2 (a) and  
 62 (b) [27].

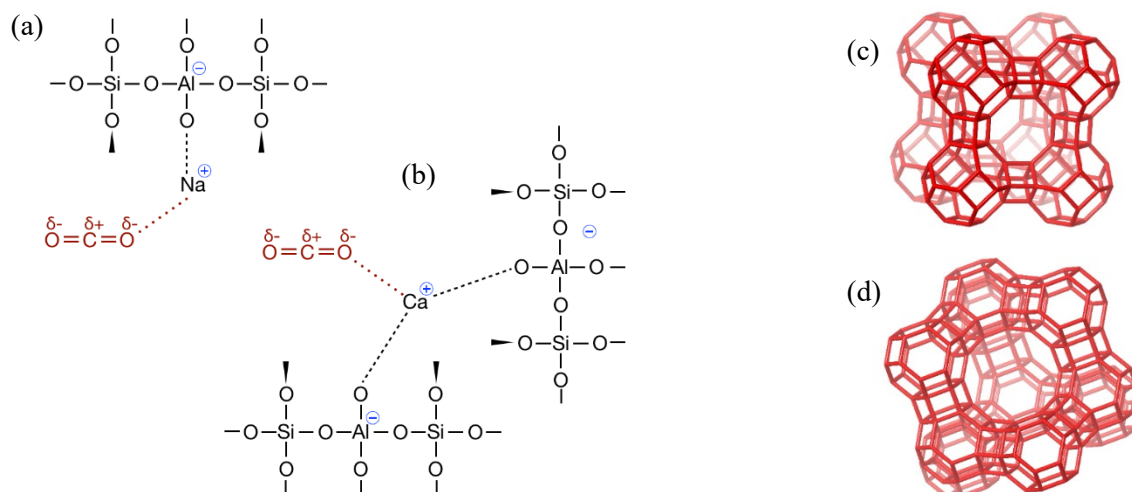


Figure 2: Interactions between CO<sub>2</sub> and monovalent (a) and divalent (b) cations in the zeolite framework; (c) Unit cell of Linde Type A (LTA); and (d) unit cell of Faujasite (FAU)[103].

63 The traditional hydrothermal scheme for the synthesis of crystalline zeolites involves mixing a source  
 64 of both silica and alumina alongside a cation source in a basic medium. With the subsequent application  
 65 of heat in a sealed autoclave [28], spontaneous nucleation and crystallisation processes are initiated  
 66 [29]. In the context of gas separation processes, synthetic zeolites which possess Linde Type A (LTA)  
 67 and Faujasite (FAU) structures are commonplace. These two unit cells (Figure 2 (c) and (d)) present  
 68 the same connected cage topology and comprise similar CBUs with sodalite cages linked by double 4-  
 69 rings (D4R) for the former and double 6-rings (D6R) for the latter [30]. The morphology of these,  
 70 however, is significantly different, LTA structures present cubic arrangements, FAU hexaoctahedral  
 71 [31]. As a source of both aluminium and silicon (and to some extent the cations), fly ashes, which  
 72 present both crystalline and amorphous [32] aluminosilicate phases require pre-treatment to maximise  
 73 availability of the primary building units. Fly ash zeolite synthesis pathways are diverse and the authors  
 74 would direct the reader to a number of comprehensive reviews on the topic [12,14,33,34]. A common  
 75 feature is the need to increase the solubility of the silicon and aluminium species in the fly ash. Fusion  
 76 with an alkali such as NaOH is typical and results in soluble sodium aluminosilicates [12,35] which can  
 77 be dispersed into an aqueous solution before aging and subsequent hydrothermal treatment [36].

78 Although there has been a steady increase in the number publications on the topic of “fly ash” and  
 79 “zeolite” since the 1990’s, publications which feature “biomass fly ash” and “zeolite” are only present

80 from the late 2000's with significant increase in the last 10 years (Figure 3). In this work, the  
81 hydrothermal pathway for zeolite synthesis from biomass ash is optimised *via* Taguchi Design of  
82 Experiment. The fly ash precursor and optimum zeolite product is comprehensively characterised in  
83 respect of material properties. The optimum zeolite product is evaluated for its performance in CO<sub>2</sub>  
84 adsorption using thermogravimetric and volumetric equipment further supported by estimation of  
85 adsorption equilibria and kinetics.

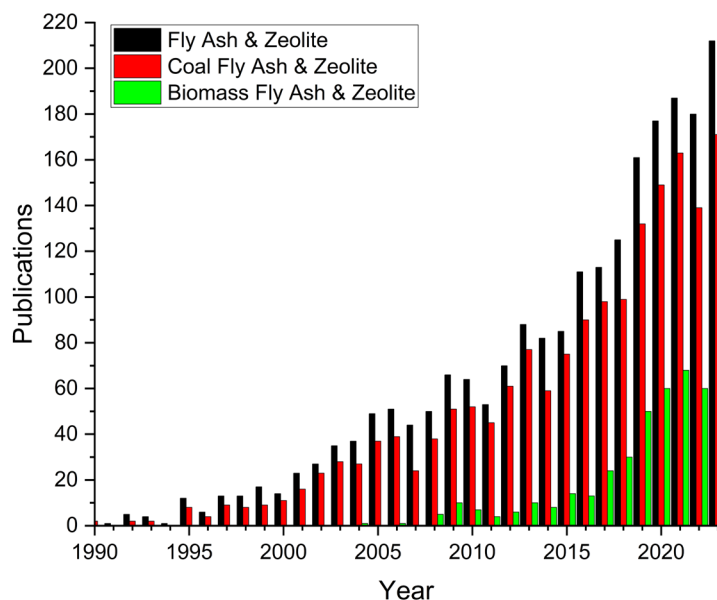


Figure 3: Publications indexed on SCOPUS by publication year.

## 86 2. Materials and Methodology

87 Biomass combustion fly ash (BFA) was sourced from Drax Power Station, Selby, UK, and is produced  
88 through combustion of imported white wood pellets. Sodium hydroxide was procured from Sigma  
89 Aldrich ( $\geq 97\%$ ) whilst the CO<sub>2</sub> (N2.8) and N<sub>2</sub> (N4.8) gases were sourced from BOC, UK. The alkaline  
90 fusion-assisted hydrothermal procedure was developed from previous works [30,37] and adjusted for  
91 each synthesis as per the experimental design. For each synthesis 5 g BFA was mixed with NaOH and  
92 ground manually in an unglazed alumina pestle and mortar for 5 minutes. Subsequently the mixture was  
93 placed into a nickel crucible and fused in a muffle furnace at 550 °C for 1 h (ramp rate of 5 °C·min<sup>-1</sup>  
94 from ambient). The fused product was crushed and ground in a pestle and mortar before adding to  
95 deionised water in a PTFE liner. This mixture was then aged under mechanical/magnetic stirring at 500  
96 RPM, 25 °C for 16 h. After insertion of the liner into a stainless-steel pressure vessel (Berghof DAB-  
97 3) it was then heated in an oven to a set temperature (ramp rate of 0.5 °C·min<sup>-1</sup> from ambient). Upon  
98 completion the system was allowed to cool to around 40 °C before removing the liner and decanting  
99 and disposing of the supernatant. The solid product was separated and washed *via* vacuum filtration to  
100 a pH of 9. Finally, the product is dried overnight at 110 °C before grinding to a fine powder and  
101 weighing.

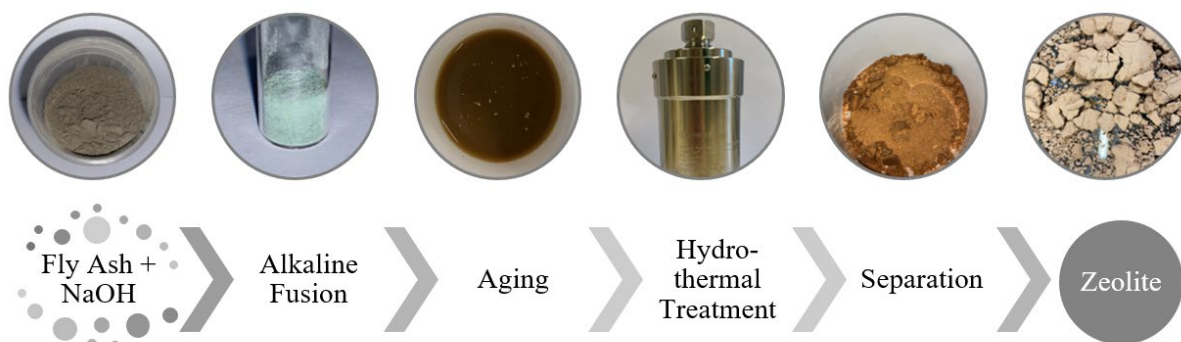


Figure 4: The procedure for synthesising fly-ash derived zeolites employed in this work.

## 102 2.1. Experimental Design – L9 Taguchi O.A.

103 The use of statistical techniques in the design and optimisation of experimental campaigns is of varied  
 104 efficacy and is heavily dependent on the appropriate application of such tools including the selection of  
 105 suitable factors and their levels [38]. A Taguchi L<sup>9</sup> design is employed in this work to study the effect  
 106 of 4 factors on the CO<sub>2</sub> adsorption capacity of zeolitic adsorbents produced hydrothermally. The 4  
 107 factors and their 3 levels (+1, 0 and -1) are provided in Table 1. Selection of these factors is based on  
 108 their key influence in the hydrothermal and alkaline-fusion hydrothermal synthesis procedures [12].  
 109 This work aims to identify an optimum BFA-derived zeolite with the least additional cost or complexity,  
 110 control of factors aside from those directly influencing the synthesis methodology such as Si/Al ratio  
 111 have not been considered as these become increasingly important when targeting a specific zeolite  
 112 structure. The levels selected in this work were informed through previous works [30,37] which sought  
 113 to reveal the experimental domain suitable for production of crystalline zeolitic products appropriate  
 114 for CO<sub>2</sub> capture (*i.e.* FAU and LTA). The objective function for optimisation is the maximisation of  
 115 equilibrium CO<sub>2</sub> adsorption capacity at 1 atm and 50 °C estimated gravimetrically *via* TGA. The  
 116 temperature was selected to align with that of a thermal power plant after exhaust gas cleaning units.  
 117 The two statistical tools employed in this work to analyse the L<sup>9</sup> Taguchi DoE are the signal-to-noise  
 118 ratios (SNR) and Analysis of Variance (ANOVA) [39]. With regards to the former, of the three  
 119 individual forms, the ‘larger the better’ SNR is used. The technique of ANOVA dissects variation into  
 120 their respective sources and facilitates interpretation of the results with identification of those factors  
 121 with statistical significance.

122 Table 1: Taguchi L9 O.A. exhibiting the 4 factors and respective levels studied in this work.

Run	NaOH/FA (w/w)	Crystallisation Time (h)	Crystallisation Temp (°C)	Liquid/Solid (w/w)	Sample Name
1	1.8	2	50	5	Z - 1.8/2/50/5
2	1.8	6	70	6	Z - 1.8/6/70/6
3	1.8	10	90	7	Z - 1.8/10/90/7



4	2	2	70	7	Z - 2/2/70/7
5	2	6	90	5	Z - 2/6/90/5
6	2	10	50	6	Z - 2/10/50/6
7	2.2	2	90	6	Z - 2.2/2/90/6
8	2.2	6	50	7	Z - 2.2/6/50/7
9	2.2	10	70	5	Z - 2.2/10/70/5

## 2.2. Material Characterisation

The as-received industrial-grade BFA and the optimum zeolite product have been characterised *via* Scanning Electron Microscopy (SEM) using a Zeiss LEO 1455VP instrument after gold-coating *via* the sputtering technique to minimise charging of the non-conductive samples during analysis. The elemental analysis of both the BFA and zeolite was evaluated through Energy Dispersive X-Ray Spectroscopy (EDS) using an Oxford INCAx-act system. The phases present in the BFA precursor and zeolite product were identified through X-Ray Diffraction (XRD) using a Bruker D8 diffractometer equipped with a copper tube and Lynxeye position sensitive detector in a 2theta range of 5 – 70 °, with a scan step size equal to 0.01°. The phases present within each product were identified using the Bruker Diffrac.EVA software package. The equilibrium CO<sub>2</sub> adsorption capacity of each sample was employed as the dependent variable for the optimisation. The equilibrium CO<sub>2</sub> adsorption capacity was measured using thermogravimetric analysis (TGA, Mettler Toledo TGA 2) under a stream of pure CO<sub>2</sub> at 50 °C after an initial degassing at 150 °C under pure N<sub>2</sub> for 2 h. The effect of temperature on the adsorption kinetics and equilibrium capacity has also been assessed *via* TGA at 25, 50 and 75 °C. The working capacity of the optimum zeolite has been evaluated at 50 °C by repeating the TGA programme for 40 adsorption/desorption cycles. Equilibrium adsorption isotherms have been generated *via* volumetric analyses (Micromeritics ASAP 2020) at 0, 10, 20, 25, and 40 °C between 0 and 1 bar(a). Nonlinear regression has been employed to fit models to both the kinetic and equilibrium data. The enthalpy of adsorption has been calculated *via* the Clausius Clapeyron equation with the equilibrium isotherms produced at 5 different temperatures. The porous surface area (S<sub>BET</sub>) was obtained following the Brunauer – Emmett – Teller Method [40] using a Micromeritics 3Flex Analyser under pure N<sub>2</sub> at 77K after degassing at 350 °C for 12 h (10 °C·min<sup>-1</sup>) with microporosity estimations *via* the t-plot method.

## 3. Results and Discussions

### 3.1. Taguchi Optimisation

The results from the synthesis campaign are presented in Table 2. The yields are calculated with reference to the initial mass of BFA (5 g) added prior to fusion with NaOH:

149 
$$\frac{\text{mass of product (g)}}{\text{mass of BFA (g)}} \times 100 = \text{Yield (\%)}$$

150 The equilibrium uptakes ( $\text{mmol}\cdot\text{g}^{-1}$ ) were estimated *via* TGA using pure  $\text{CO}_2$  at 1 bar(a) and  $50^\circ\text{C}$  after  
 151 purging the samples under  $\text{N}_2$  at  $150^\circ\text{C}$  for 1 h. The results demonstrate that the products' uptakes are  
 152 centred at either 0.6 and  $1.6\text{ mmol}\cdot\text{g}^{-1}$  which when considering the x-ray diffractograms (Figure 8)  
 153 would suggest the former is indicative of amorphous aluminosilicates and the latter of crystalline  
 154 zeolitic phases.

155 *Table 2: Product yield (as percent of initial BFA weight) and equilibrium  $\text{CO}_2$  adsorption capacity at  $50^\circ\text{C}$  and 1 atm.*

Sample	Yield (% of BFA converted)	Equilibrium Uptake @ $50^\circ\text{C}$ ( $\text{mmol}\cdot\text{g}^{-1}$ )
Z - 1.8/2/50/5	70.75	0.65
Z - 1.8/6/70/6	75.31	0.61
Z - 1.8/10/90/7	80.86	1.51
Z - 2/2/70/7	71.44	0.56
Z - 2/6/90/5	71.47	1.67
Z - 2/10/50/6	73.53	0.56
Z - 2.2/2/90/6	71.35	0.59
Z - 2.2/6/50/7	72.34	0.49
Z - 2.2/10/70/5	72.92	1.70

156 Signal-to-noise ratios can be used for identification of the factor levels which minimise the variability  
 157 in the response, in this case the objective is to maximise the equilibrium  $\text{CO}_2$  adsorption capacity. The  
 158 “larger the better” equation is adopted for calculation of the SNRs (EQ. 1). The SNRs are given in Table  
 159 3. The delta values represent the variation in the mean SNR values across the studied levels, and allow  
 160 ranking of the factors' relative importance on the equilibrium  $\text{CO}_2$  uptake when varied within the design  
 161 space [39]. The analysis suggests a sequence that follows  $L/S > T_{\text{cry}} > t_{\text{cry}} > \text{NaOH/FA}$ .

$$\frac{S}{N} = -10 \cdot \log \left( \sum \left( \frac{1}{y^2} \right) / n \right) \quad (\text{EQ. 1})$$

162 *Table 3: Response table for the signal to noise ratios.*

Level	NaOH/FA Ratio	Crystallisation Time	Crystallisation Temperature	Liquid/Solid Ratio
1	-1.485	-4.454	-4.991	1.774
2	-1.873	-2.012	-1.574	-4.638
3	-2.057	1.041	1.15	-2.551
Delta	0.571	5.504	6.142	6.411
Rank	4	3	2	1

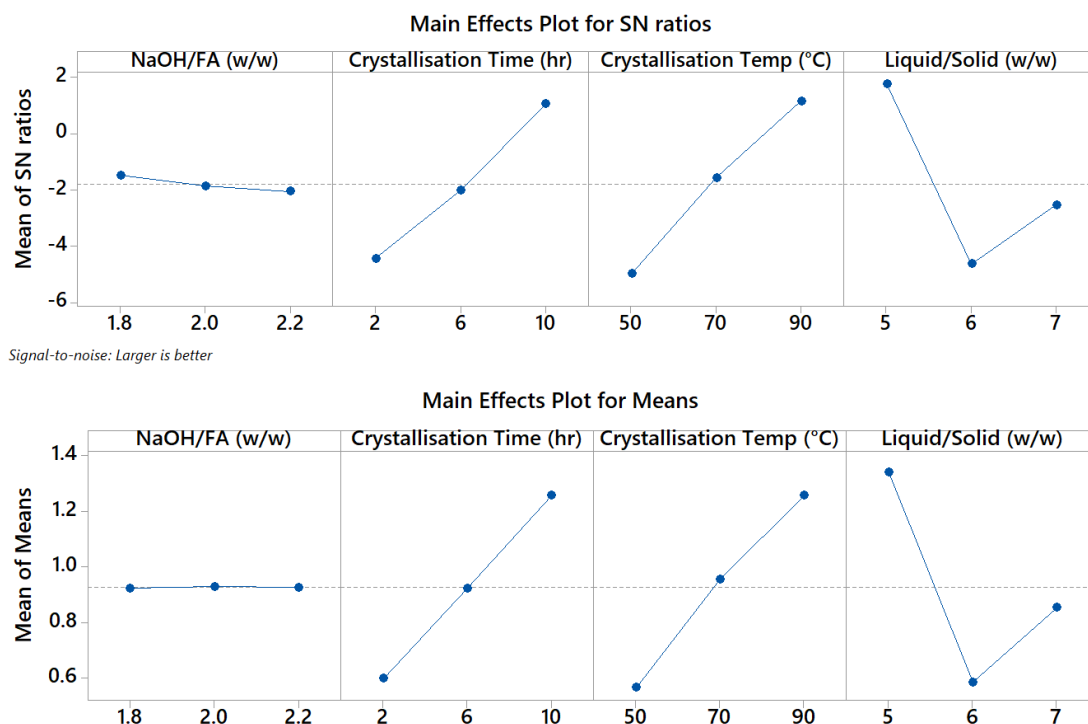


Figure 5: Main effects plot for the signal to noise ratios (top) and means (bottom).

163 The relative importance of each factor can also be observed graphically by plotting the main effects for  
 164 the SNR ratios, provided in Figure 5. From this plot the *NaOH/FA* ratio has a minimal effect on the  
 165 SNR ratio when compared to the other 3 factors. A factor which presents a large variation in the SNR  
 166 between levels is a significant contributor to the dependent variable [41]; the SNR for *L/S*,  $T_{cry}$  and  $t_{cry}$   
 167 all exhibit strong main effects (gradient) in agreement with the delta values and subsequent ranking.  
 168 The main effects have also been plotted for the means and are consistent with those for the SNRs except  
 169 for the *NaOH/FA* ratio. Optimisation based on the main effects plots depends on the objective, either to  
 170 minimise variability (SNR) or to simply maximise the response (mean). In this case and based on the  
 171 main effects plot for the means, the optimum configuration of factors and levels would be: *NaOH/FA*  
 172 ratio of 2.2,  $t_{cry}$  10 hours,  $T_{cry}$  equal to 90 °C, and *L/S* equal to 5. One limitation with employing an L9  
 173 array to study four factors at three levels is that the model is overfit due to the presence of more fitting  
 174 terms than observations (degrees of freedom) in the model [42]. Removal of some terms can facilitate  
 175 the statistical analysis. In this case, based on the main effects plot, the *NaOH/FA* ratio term was  
 176 removed. The ANOVA results for the remaining factors can be found in Table 4. Each of the factors  
 177 present a p-value < 0.05 with significantly large F-values. The liquid to solid ratio (*L/S*) was identified  
 178 as the most statistically significant factor. Within the employed synthesis, the *L/S* ratio determines both  
 179 the relative alkalinity of the solution and the water content in the mixture. Both are key factors in the  
 180 synthesis of zeolites [34] and will influence both the product structure type and crystallinity [43]. The  
 181 percentage contribution of each factor to the equilibrium uptake is around 30 % for  $T_{cry}$  and  $t_{cry}$  rising  
 182 to 39% for *L/S*; this agrees with the ranking identified in the SNR response table and main effects plot.

Factor	Percentage Contribution (%)	F-value	p-value	Order of Significance
<b>Crystallisation Time (<math>t_{cry}</math>)</b>	29.49	5721.91	0.000	3
<b>Crystallisation Temperature (<math>T_{cry}</math>)</b>	31.87	6183.58	0.000	2
<b>Liquid/Solid Ratio (<math>L/S</math>)</b>	38.63	7495.90	0.000	1

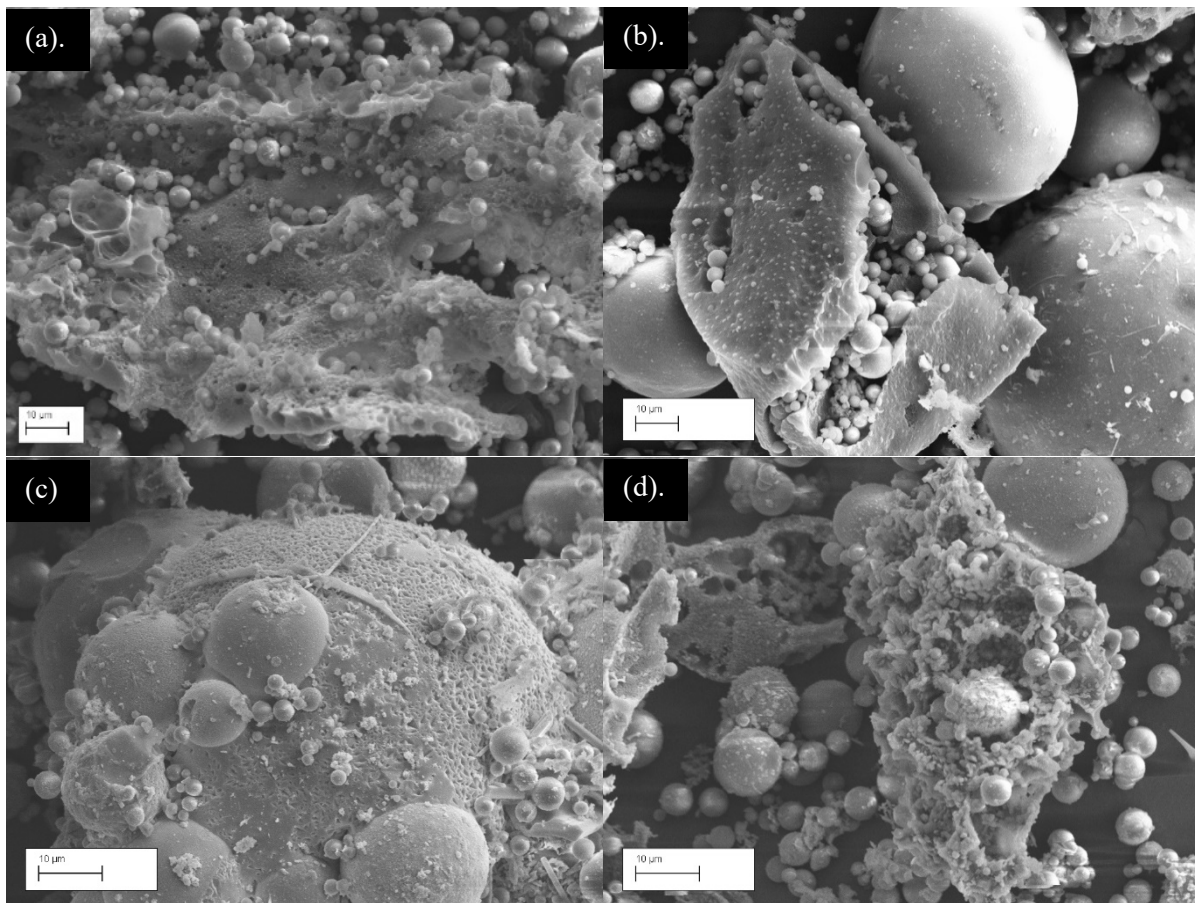
184 **3.1. Scanning Electron Microscopy and Energy Dispersive X-ray Spectroscopy**

Figure 6: SEM images of the as-received biomass combustion fly ash: a) 20 kV, 500 pA; b) 20 kV, 300 pA; c) 10 kV, 50 pA; and d) 10 kV, 100 pA.

185 The BFA samples present predominately spherical particles of varying diameter with some of these in  
 186 large clusters. Typical ash particle shapes include molten spherical particles (Figure 6); cenosphical  
 187 particles with variable wall thickness typical of light ashes, which form during the sudden cooling post-  
 188 combustion [44]; plerospherical particles (hollow spheres filled with smaller ash particles) (not  
 189 observed); angular, sharp and unmolten particles (Figure 6 (a), (c) and (d)); loose, irregular shaped and  
 190 highly porous solids (Figure 6 (a), and (e)); and agglomerations of small ash particles (Figure 6 (a), (b)  
 191 and (d)) [18]. Biomass ashes present more varied morphologies than coal ashes and in the case of woody  
 192 biomass, loosely bound and irregularly shaped Ca-rich particles are frequently reported with sub-micron  
 193 salt particles (Figure 6 (c)) [18]. The abundance of calcium in wood-based fuels generally increases ash

194 melting temperatures by approximately 100 – 200 °C although this is dependent on the presence of  
 195 other components within the ash [45]. Increased melt temperatures result in particles with more angular  
 196 morphologies that haven't undergone melt/fusion, often composed of quartz or feldspars [17]. The  
 197 elevated presence of inorganic constituents which during combustion vaporise is important during ash  
 198 formation/deposition mechanisms as they lead to coagulation and agglomeration. The EDS revealed  
 199 predominantly Si and Al in the BFA alongside Ca, K, Fe, Mg and Na. An average weight percentage  
 200 has been calculated based on analysis of five sites on the BFA and are provided as part of Table 5. The  
 201 measured diffractogram corroborates the elemental composition of the BFA. Crystalline quartz, mullite,  
 202 hematite, portlandite and calcite were identified. Quartz can indeed remain unchanged during the  
 203 combustion process and may maintain its sharp angular structure [46]; however, it can also form by  
 204 conversion of kaolinite to mullite and amorphous quartz at around 900 °C [17]. Hematite is a high  
 205 melting mineral and often forms from the decomposition of pyrite either through thermal decomposition  
 206 and subsequent oxidation or direct oxidation [47]. Elements such as S and P (among others) and to some  
 207 extent Ca, K, Mg and Na vaporise during the combustion reaction and then re-condense and form  
 208 aerosols during cooling [18]. Sodium is well known to facilitate the formation of sodalite and other  
 209 CBUs such as double-4 rings, whereas both Ca and K can present structure breaking effects [48]. The  
 210 quantity of Al and Si highlights the potential suitability of this BFA as a zeolite-precursor. The inclusion  
 211 of Ca within zeolites has also been reported as beneficial for CO<sub>2</sub> adsorption by enhancing the acidic-  
 212 basic interactions [49]. Although not often considered a route for improvement of CO<sub>2</sub> adsorption, the  
 213 presence of Fe as a charge compensating cation has been observed to improve the catalytic performance  
 214 of FA-derived zeolites [50]. Both Fe and Ca oxides however, are known to hinder the zeolite nucleation  
 215 rate [29] with the former a result of the lattice strains associated with the high Fe-O bond length (1.9  
 216 Å) and the latter due to the possible formation of calcium silicate hydrate over zeolitic phases [51,52].

217 *Table 5: The EDS elemental analysis of the BFA and ZOFT averaged from five sites.*

<b>Element</b>	<b>Biomass Fly Ash Avg. Weight (%)</b>	<b>Zeolite (ZOFT) Avg. Weight (%)</b>
Na	1.66	3.71
Mg	2.01	1.42
Al	9.15	10.05
Si	14.28	18.55
P	0.13	0.07
S	0.70	0.06
K	7.91	0.66
Ca	8.54	15.56
Fe	3.78	4.21



O	51.84	45.71
---	-------	-------

218 The morphology of the ZOPT sample can be observed in Figure 7. Examples of both cubic LTA and  
 219 octahedral FAU are present confirming the findings of the XRD. The sample presents a relatively  
 220 consistent individual crystal size of around 2  $\mu\text{m}$  although the majority of these crystals are present in  
 221 larger agglomerations of both crystals and what is assumed to be an amorphous mass. This amorphous  
 222 mass will be the remaining aluminosilicates not consumed in the zeolite crystallisation process. None  
 223 of the observed morphologies in the fly ash precursor remain further highlighting the efficacy of alkaline  
 224 fusion to maximise the availability of soluble Si and Al containing species. As a complement to SEM  
 225 and XRD, EDS can elucidate the presence of specific cations and their distributions within the  
 226 crystalline frameworks and the amorphous constituent. Calcium was identified in most of the crystalline  
 227 morphologies, and often at a higher weight percent than sodium. EDS analysis of five crystalline areas  
 228 suggests the zeolitic phases present an average Si/Al weight ratio of approximately 1.85. Both iron and  
 229 calcium are present in the sample at around 4 and 16 wt% so one could infer that there exists within  
 230 ZOPT calcium exchanged type A and type X zeolites phases. EDS however, is semi-quantitative and  
 231 fails to accurately measure low atomic number elements such as sodium due to their lower energy  
 232 characteristic X-rays which are more difficult to reliably detect and often absorbed by the sample. A  
 233 bulk analysis however, would be unable to accurately measure the composition of specific crystalline  
 234 phases due to the presence of amorphous aluminosilicates.

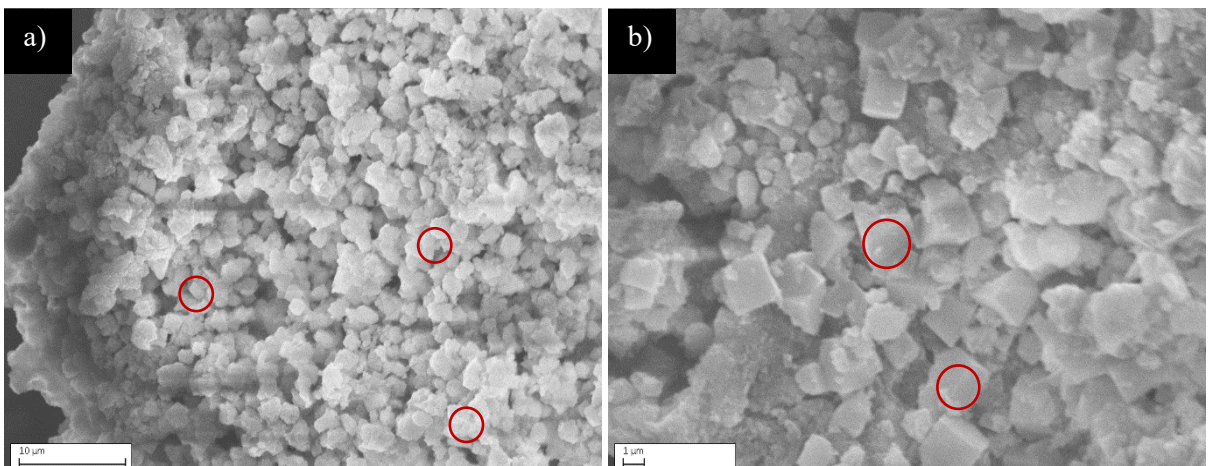


Figure 7: SEM images of ZOPT, a) 15kV and 40 pA and b) 15kV and 40 pA. Red circles indicating site location for EDS analysis.

235 **3.2. X-ray Diffraction**

236 Powder X-ray diffraction is used to identify crystalline phases and of the 9 samples synthesised, 3 are  
 237 distinctly crystalline: Z-1.8/10/90/7, Z-2/6/90/5 and Z-2.2/10/70/5. The remaining six samples all  
 238 present a broad ridge centred at 30 ° 2theta which is indicative of amorphous aluminosilicates [53,54].  
 239 This ridge can also be seen in the crystalline phases indicating a non-complete conversion of these  
 240 amorphous components into crystalline frameworks [30]. Sample Z-2/6/90/5 presents peaks with the  
 241 largest intensities relative to the other samples as well as a less well-defined amorphous region  
 242 corroborating the findings of the DoE analysis which identified a region of high capacity at elevated

243 hydrothermal temperatures. The phases identified in each of the crystalline samples were LTA and FAU  
 244 zeolites. Although these phases possess similar building blocks they do present distinct diffraction  
 245 patterns with some overlap. The samples which exhibit the higher CO<sub>2</sub> adsorption capacities tend to  
 246 possess diffractograms with greater intensities of peaks characteristic of FAU zeolites such as the peak  
 247 at a 2θ value of approximately 6 ° corresponding to the lattice plane (111). The peak centred at a 2θ  
 248 value of approximately 7 ° is characteristic of LTA zeolites (200) and not present in FAU  
 249 diffractograms, with the greatest intensity shown for Z-2.2/10/70/5. Although inference of mass ratios  
 250 (LTA/FAU) through analysis of the relative intensity of diffractogram peaks is of poor accuracy, the  
 251 uptakes corroborate the notion that samples Z-2.2/10/70/5 and Z-2/6/90/5 may possess a larger  
 252 proportion of FAU than Z-1.8/10/90/7. The diffractograms generated for the 3 crystalline samples and  
 253 the optimum (ZOPT) are provided in Figure 8 alongside those of type X (PDF: 01-070-2168) and type  
 254 A (PDF: 01-089-8015) zeolites. As shown, ZOPT presents a better-defined pattern with increased peak  
 255 intensities over the 3 other samples suggesting the optimisation has improved the samples crystallinity.  
 256 Both the LTA (200) and FAU (111) peaks are more pronounced with ZOPT suggesting the synthesis  
 257 conditions are more favourable for zeolite crystallisation also evidenced by a less pronounced  
 258 amorphous ridge. The inference is that more of the alkali fused BFA has been consumed during  
 259 crystallisation, hence the increased peak intensities. Interestingly, no phases which existed in the BFA  
 260 precursor are present in any of the produced samples, suggesting the alkali fusion step in the synthesis  
 261 has successfully converted the BFA into soluble Al and Si containing species.

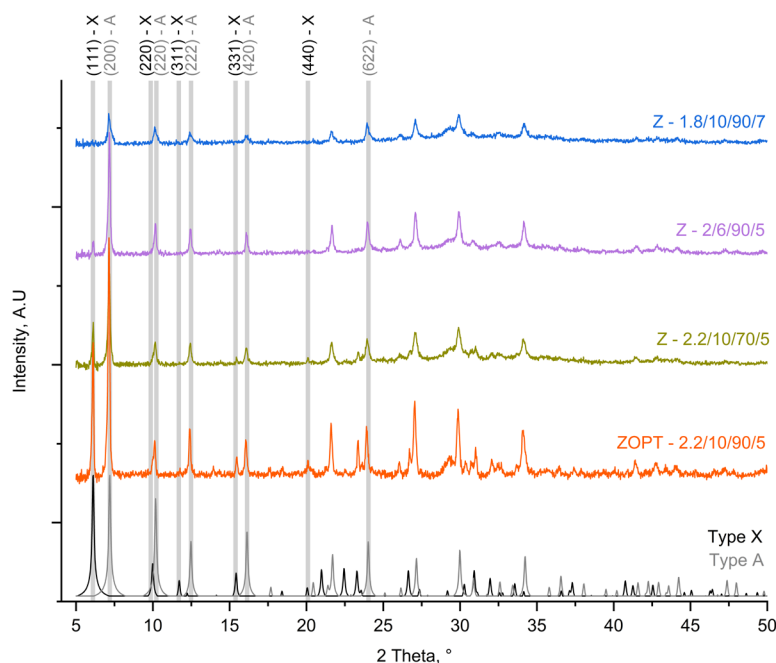


Figure 8: Powder x-ray diffractogram for crystalline zeolites produced in the L9 OA and the predicted optimum, ZOPT. Diffractograms provided for type X and type A zeolites adjacent to the y-axis.

### 262 3.3. Porosity and Surface Area Analysis

263 The BET surface area was estimated for ZOPT *via* isothermal N<sub>2</sub> adsorption and desorption at 77 K  
 264 (Figure 9). The isotherm is of the type IV IUPAC classification, the initial knee indicative of primary  
 265 micropore filling in pores of molecular dimensions at low relative pressures [55]. This is followed by  
 266 the onset of capillary condensation in larger mesopores as  $P/P_0$  increases [56]. A narrow hysteresis loop  
 267 can be seen after  $0.4 < P/P_0$ ; the adsorption branch being a composite of both type I and II isotherms  
 268 suggests this to be an example of a H4 hysteresis [57]. This phenomena is typical for mixed micro-  
 269 mesoporous materials [31] and can be a result of development of mesoporosity through aggregation of  
 270 the individual zeolite crystals [58,59] and in this case can also include the contribution from the  
 271 amorphous phase. Type IV isotherms often feature a plateau in adsorption when the relative pressure  
 272 tends to 1 due to complete saturation/occupation of the adsorbent's mesopores *via* capillary  
 273 condensation. This is not present in ZOPT resulting from the presence of macropores [60] causing an  
 274 asymptotic increase in the adsorbed quantity at high relative pressures due to unrestricted multilayer  
 275 formation. This phenomenon may result from significant structural defects in the crystalline phase or  
 276 through aggregation [61]. The BET surface area has been calculated to be 321.60 m<sup>2</sup>·g<sup>-1</sup>, t-plot  
 277 micropore area of 218.56 m<sup>2</sup>·g<sup>-1</sup> with total (BJH) and t-plot micropore volumes of 0.23 cm<sup>3</sup>·g<sup>-1</sup> and 0.09  
 278 cm<sup>3</sup>·g<sup>-1</sup>, respectively. The BET surface area has been estimated in the  $P/P_0$  range of 0.016 and 0.059 to  
 279 satisfy the criteria proposed by Rouquerol [62]; this deviates from the traditional range for BET surface  
 280 area analysis (0.05 – 0.3) due to significant microporosity in the samples. The linear BET plot for N<sub>2</sub>  
 281 at 77 K is provided as an inset to Figure 9.

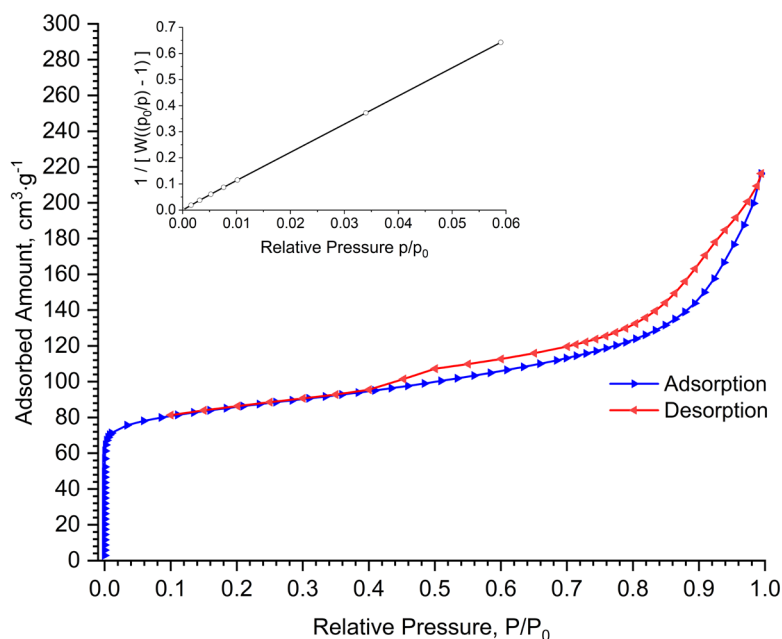


Figure 9: N<sub>2</sub> adsorption/desorption isotherm measured at 77 K (BET).



282 The surface area has also been estimated *via* analysis of the CO<sub>2</sub> adsorption isotherm at 0 °C. This  
 283 method which is often used for characterising carbonaceous adsorbents overcomes the kinetic  
 284 limitations associated with nitrogen adsorption at 77K [57]. The smaller kinetic diameter of CO<sub>2</sub> and  
 285 the elevated temperature and pressure of analysis facilitate diffusion into narrow micropores  
 286 inaccessible to N<sub>2</sub> at 77K. The high saturation pressure of CO<sub>2</sub> at these conditions however limits the  
 287 maximum pore size that can be characterised to approximately 1 nm [63]. The calculations have been  
 288 performed using SESAMI [64] with an adsorbed cross-sectional area of 21.8 Å and saturation pressure  
 289 of 3.851408x10<sup>6</sup> Pa. Analysis of the linear region suggests a surface area of 432.30 m<sup>2</sup>g<sup>-1</sup>. This value  
 290 represents a 111 m<sup>2</sup>g<sup>-1</sup> increase suggesting a large number of small micropores (<1 nm) in ZOPT which  
 291 were not accessible to N<sub>2</sub> at 77K. Type A and X zeolites typically possess pores of size 4 and 7 Å,  
 292 respectively which would explain the underestimation of surface area when using N<sub>2</sub>. The analysis of  
 293 ZOPT's pore size distribution has not been carried out due to the stronger quadrupole moment of CO<sub>2</sub>  
 294 and the presence of polar groups within the zeolite making correlation of pore size and CO<sub>2</sub> pore filling  
 295 pressure difficult [57].

### 296 3.4. CO<sub>2</sub> Adsorption

#### 297 3.4.1. Screening

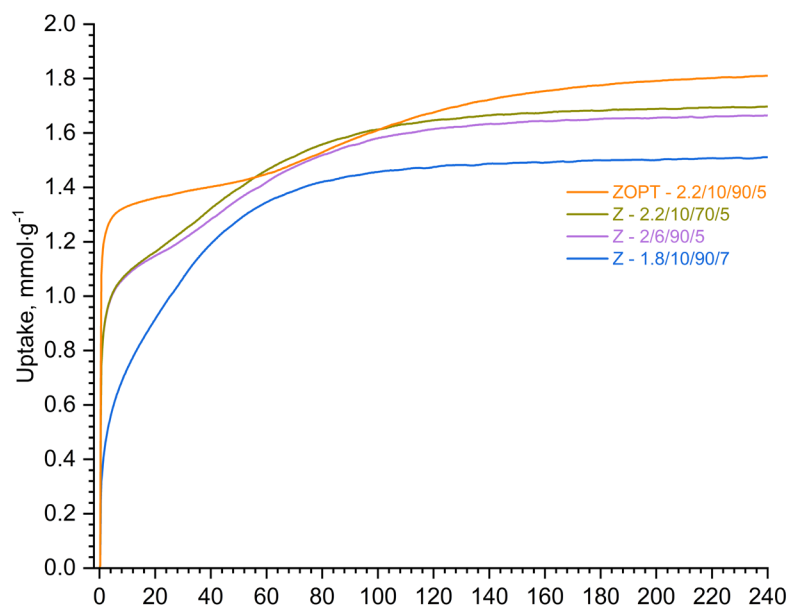


Figure 10: CO<sub>2</sub> uptake capacity measured via TGA under 1 atm at 50 °C.

298 The uptake capacity was used as the dependent variable for the Taguchi optimisation. Measured *via*  
 299 TGA at 50 °C with pure CO<sub>2</sub> at 1 atm, the equilibrium uptakes are given in Table 2. The samples which  
 300 lacked distinct crystalline phases all exhibit an equilibrium uptake of between 0.39 and 0.65 mmolg<sup>-1</sup>.  
 301 Although less than the crystalline counterpart, it is in agreement with the literature [65] and represents  
 302 promising potential for geopolymer sorbents in the remit of CO<sub>2</sub> capture, especially if sourced from  
 303 BFA. The three crystalline phases illustrate the efficacy of uniform-pore structure in gas adsorption

304 with equilibrium capacities between 1.50 to 1.70 mmol $g^{-1}$ . The adsorption characteristics of Z-  
305 1.8/10/90/7 differ slightly from the two alternative crystalline samples, the initial phase of adsorption  
306 is slower, suggesting a crystalline phase or ratio of phases which is different to Z-2.2/10/70/5 and Z-  
307 2/6/90/5. These three samples have been synthesised at each of the NaOH/FA ratios, hence the  
308 associated statistical insignificance; None of the samples produced at a  $T_{cry} = 50$  °C and  $\underline{L/S} = 6$   
309 displayed high adsorption capacities, potentially as a result of failing to facilitate zeolitisation from the  
310 fused BFA. An extended measurement (4-hour adsorption time) was completed for ZOPT and the three  
311 crystalline samples produced according to the DoE (Figure 10). The sample with the highest equilibrium  
312 capacity is ZOPT at 1.84 mmol $g^{-1}$ . This value represents an 8.2% increase over Z-2.2/10/70/5 and is  
313 comparable to the literature on other fly ash zeolites [31,66,67] and industrial biomass bottom ash  
314 derived adsorbents [16,42]. The only difference between the synthesis conditions of ZOPT and Z-  
315 2.2/10/70/5 is the elevated crystallisation temperature (90 vs 70 °C), suggesting that higher  
316 hydrothermal temperatures can preferentially produce FAU as observed in the XRD diffractograms  
317 (Figure 8). The CO $_2$  adsorption kinetics for FAU and LTA are markedly different, considering they  
318 both present the connected cage topologies [68]. The latter is considered a small pore zeolite, presenting  
319 a pore size of between 3 and 5 Å depending on the cation, whilst the former is above 7 Å [27]. The  
320 lower pore size is comparable to the kinetic diameter of CO $_2$  (3.3 Å) which can lead to a configurational  
321 diffusion regime with much lower gas diffusivity and consequently, slower adsorption kinetics. In a  
322 fixed bed configuration, slow diffusion of CO $_2$  into the zeolite pores would hinder mass transfer and  
323 result in a tendency for the CO $_2$  to flow through the bed rather than be adsorbed [27], reducing the  
324 breakthrough time and increasing the required bed height, cycle time and ultimately cost [69]. Type X  
325 zeolites (FAU) which present a 12-member ring, MR aperture (vs 8 for LTA) can facilitate diffusion in  
326 the Knudsen regime as the channel diameter is larger relative to the molecular diameter of CO $_2$ . The  
327 transition from configurational diffusion to Knudsen occurs when the ratio of molecular to channel  
328 diameter,  $\lambda$  is below 0.6 (typically) however, for FAU this value is 0.45 [27,68]. The location and type  
329 of cations can also significantly affect the kinetics of CO $_2$  adsorption and is often more pronounced  
330 with type A than type X. The exchange of Na $^+$  with K $^+$  in LTA zeolites reduces the pore size of the  
331 zeolite from approximately 4 to 3 Å with site II being the preferential site (centre of the D8R) hindering  
332 diffusion by obstructing access to the alpha cage [70,71]. Exchange with a divalent atom such as Ca $^{2+}$   
333 reduces the occupation of site II and increases both the pore size (5 Å) and volume by improving  
334 accessibility to the alpha cage [72,73].

### 335 **3.4.2. Equilibrium Adsorption**

336 The equilibrium CO $_2$  adsorption isotherms have been measured volumetrically at 0, 10, 20, 25 and 40  
337 °C in the total pressure range of 0 – 1 bar and are presented in Figure 11 . These isotherms are classical  
338 type I IUPAC isotherms featuring a sharp increase in the adsorbed quantity in the low pressure region  
339 [74]. This characteristic is influenced largely by the Si/Al ratio of zeolites as the aluminium content

dictates the required quantity of extra-framework cations [75] and hence any increase in Si/Al ratio would decrease the number of adsorption sites per unit mass of adsorbent [27]. Due to the lower electronegativity of Al (3+ vs 4+ for Si) there is a requirement for additional cation charge compensation which modifies the local electric field and hence increases the electric field gradient as Al content increases [76]. Structures such as LTA which typically possess an Si/Al ratio close to 1 and Type X (FAU) around 1.5, will exhibit good adsorption performance for CO<sub>2</sub>. This also increases the co-adsorption of moisture [77] as the dipole moment of H<sub>2</sub>O strongly competes with quadrupoles of CO<sub>2</sub> (despite being a non-polar molecule) for adsorption sites [78].

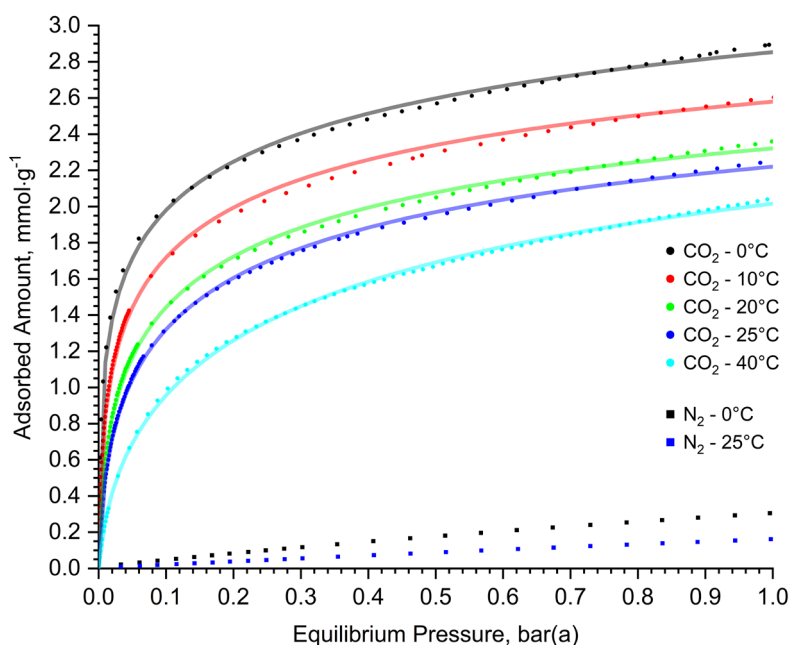


Figure 11: Measured equilibrium CO<sub>2</sub> adsorption isotherms (discrete data) and the Toth isotherm model (continuous data) fitted via non-linear regression analysis. Equilibrium N<sub>2</sub> isotherms measured at 25 °C and 50°C are also provided.

A lower Si/Al ratio however, can reduce the total pore volume and ultimately the equilibrium capacity (at higher adsorption pressures) of a zeolite due to the steric hinderance of the additional (and potentially much larger, e.g. K) cations in the framework [48]. Modelling of the equilibrium isotherms is critical for proper understanding of the mechanisms and enables effective design of an adsorption system [79–81]. In this work, four individual isotherm models have been assessed for quality of fit (Table 6). The models have been fitted via non-linear least squares regression using MATLAB r2023a with the goodness-of-fit estimated through the coefficient of determination (R<sup>2</sup>) which has been adjusted for the number of predictors in the model (adj-R<sup>2</sup>), and the root mean squared error (RMSE).

Table 6: Adsorption isotherm models assessed in this work.

Model	Equation	Fitting Parameters
Freundlich	$q_e = K_F \cdot P^{1/n_F}$	$K_F, n_F$

Langmuir	$q_e = \frac{q_{max} \cdot K_L \cdot P}{1 + K_L \cdot P}$	$q_{max}, K_L$
Sips	$q_e = \frac{q_{max} \cdot K_S \cdot P^{n_s}}{1 + K_S \cdot P^{n_s}}$	$q_{max}, K_S, n_s$
Toth	$q_e = \frac{q_{max} \cdot P}{(b + P^{n_T})^{\frac{1}{n_T}}}$	$q_{max}, b = \frac{1}{K_T}, n_T$

357 The Toth equilibrium isotherm model was identified as the best fit for the measured data and the results  
358 of the analysis are provided in Table 7. The best fitting model (Toth) is plotted alongside the discrete  
359 experimental data in Figure 10. The three model parameters  $q_{max}$ ,  $K_T$  and  $n_T$  represent the predicted  
360 saturation capacity, the affinity parameter and the Toth constant, respectively. The Toth constant  
361 denotes the inhomogeneity of an adsorbent surface and is typically less than 1; when  $n_T = 1$ , the equation  
362 reduces to the Langmuir model demonstrating homogeneity [82]. The Toth constant is temperature  
363 dependent and is expected to approach unity as the temperature increases [83]. This can be seen in Table  
364 7 with significant deviation from unity at 0 °C ( $n_T = 0.227$ ) increasing two-fold at 40 °C ( $n_T = 0.415$ ).  
365 The heterogeneity of the samples is a result of the presence of multiple phases which can facilitate CO<sub>2</sub>  
366 adsorption, in this case type A and type X frameworks alongside amorphous geopolymers each of which  
367 can present very different adsorption mechanisms and hence affinities [84]. Even for pure phases,  
368 zeolites possess energetically different adsorption sites largely due to the type and distribution/position  
369 of framework cations [27]. For both type A and type X zeolites there are multiple possible cation sites  
370 which have varying levels of occupation dependant on the Si/Al ratio of the zeolite and both the size  
371 and charge of the cations [73]. The reduction in heterogeneity with an increase in temperature could be  
372 attributed to an increase in the adsorbate mobility and/or lateral interactions (adsorbate-adsorbate) [85],  
373 narrowing the distribution of adsorption site energies [86], as the low energy sites become less viable  
374 such as those which rely on contribution from van der Waals dispersion interactions (i.e. Debye, London  
375 and Keesom) between CO<sub>2</sub> and the zeolite framework.

376 *Table 7: Results of the non-linear regression with Toth isotherm model fitting.*

Temperature, °C	Model Parameters			Adj-R <sup>2</sup>	RMSE
	$q_{max}$	$K_T$	$n_T$		
0	5.173	6.930	0.227	0.9977	0.0337
10	3.956	6.840	0.319	0.9986	0.0301
20	3.541	5.963	0.368	0.9992	0.0208
25	3.403	5.488	0.392	0.9995	0.0143
40	3.749	3.409	0.415	0.9994	0.0171

377 Table 8 presents examples of ash-derived zeolites synthesised using alkaline fusion hydrothermal  
 378 (AFHT) or hydrothermal (HT) procedures. The CO<sub>2</sub> adsorption capacity of the zeolite produced in this  
 379 work is well aligned with the capacities of similar sorbents in the literature. Due to the limited number  
 380 of studies pertaining to industrial-grade biomass combustion ashes, comparison is made to coal fly-ash  
 381 (CFA) derived zeolites which have a slightly higher adsorption capacity and selectivity. Of the  
 382 examples in Table 9, only two [87,88] have been produced using a similar methodology (*i.e.* not  
 383 requiring pretreatment or the addition of extra aluminium). The simple synthesis procedure employed  
 384 in this work demonstrates a potential pathway for industrially produced biomass ash valorisation.

385 *Table 8: Ash-derived zeolites in the published literature and their CO<sub>2</sub> adsorption capacities. \*Capacity estimated from*  
 386 *isotherm plot.*

Precursor	Synthesis Method	Zeolite Type	Degassing Conditions	CO <sub>2</sub> Adsorption Capacity	CO <sub>2</sub> /N <sub>2</sub> Selectivity	Ref
Coal Fly Ash	AFHT	X	260 °C Helium	3.21 (0 °C, 1 bar)		[31]
Coal Fly Ash	AFHT	X	300 °C Vacuum	3.25* (50 °C, 1 bar)		[67]
Coal Fly Ash	AFHT	A	300 °C Vacuum	2.47* (50 °C, 1 bar)		[67]
Coal Fly Ash	AFHT	X	260 °C Helium	3.1 (0 °C, 1 bar)	24.2	[87]
Coal Fly Ash	AFHT	X	400 °C Nitrogen	3.03 (0 °C, 1 bar)		[50]
Coal Fly Ash	AFHT	X	450 °C	2.43 (40 °C, 1 bar)		[58]
Coal Fly Ash	AFHT	X	300 °C	3.23* (50 °C, 1 bar)	21.5	[89]
Coal Fly Ash	AFHT	A	300 °C	2.42* (50 °C, atm)	17.3	[89]
Coal Fly Ash (gasification)	AFHT	X	500 °C Argon	3.3 (25 °C, 1 bar)		[88]
Palm Oil Fly Ash	AFHT	X		4.47* (32 °C, 1 bar)		[90]
Rice Husk Ash	HT	X	250 °C Vacuum	4.7 (40 °C, 1 bar)		[91]
Rice Husk Ash	HT	X	350 °C	3.12 (0 °C, 1 bar)	20.3	[92]
Rice Husk Ash	HT	A	350 °C	1.46 (0 °C, 1 bar)	9.7	[92]
Biomass Fly Ash	AFHT	A & X	350 °C N <sub>2</sub>	2.92 (0 °C, 1 bar) 2.27 (25 °C, 1 bar)	9.4 14.2	This work

### 387 3.4.3. Adsorption Kinetics

388 The kinetics associated with ZOPT's adsorption of CO<sub>2</sub> has been evaluated by fitting kinetic models to  
 389 the measured TGA uptake data at 50 °C and 1 bar CO<sub>2</sub>. Although not representative of the scale or  
 390 configuration of the adsorption process, this still provides some insight into the specific mechanisms  
 391 which underpin, and ultimately limit the rate of adsorption. The data was fitted with 5 individual kinetic  
 392 models: Pseudo first (PFO) and second order (PSO), Elovich, Weber & Morris Intraparticle diffusion

393 (IPD) and Avrami models. Both the PFO and PSO fit the data poorly; the other three models together  
 394 with the fitting results are presented in Table 9.

395 *Table 9: Results of the non-linear kinetic model fitting.*

Model	Equation	Model Parameters	R <sup>2</sup>	RMSE
Elovich	$q_t = \frac{1}{\beta} \ln(1 + \alpha\beta t)$	$\alpha = 190.1$ $\beta = 0.103$	0.943	2.376
W&M Intraparticle Diffusion	$q_t = k_{IPD} \cdot t^{1/2} + C$	$k_{IPD} = 2.62$ $C = 45.55$	0.921	2.795
Avrami	$q_t = q_e(1 - e^{(-k_A t)^{n_A}})$	$k_A = 0.09$ $n_A = 0.394$	0.877	3.491

396

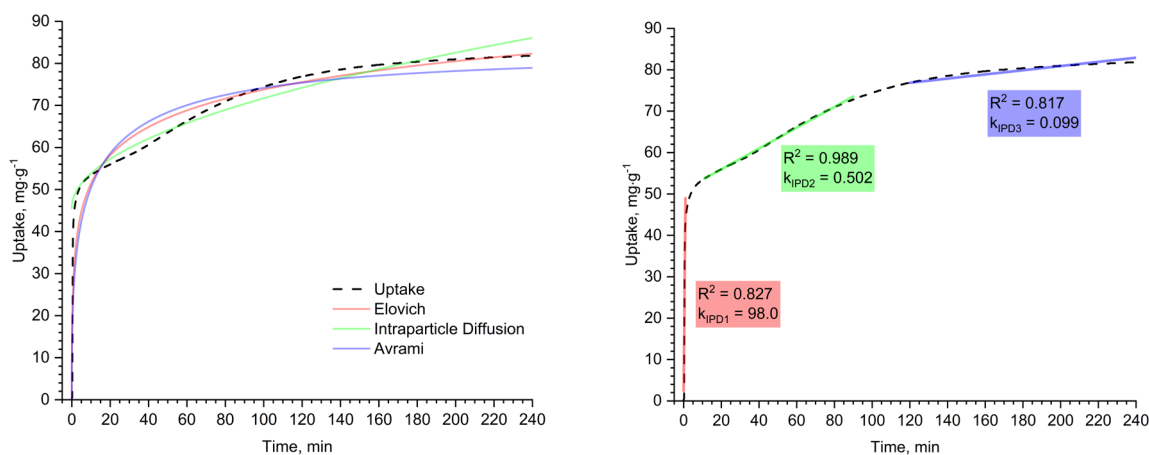


Figure 12: Left - ZOPT CO<sub>2</sub> adsorption kinetic model fitting; Elovich, Avrami and W&M Intraparticle Diffusion model shown. Right - CO<sub>2</sub> adsorption kinetics (ZOPT) at 50 °C and 1 bar fitting with piecewise Intraparticle Diffusion model.

397 Based on the R<sup>2</sup> and RMSE values, the Elovich model can be seen to best fit the measured data (Figure  
 398 12, left). The Elovich model is empirical and lacks a definitive physical meaning of the model  
 399 parameters [93] however, it is commonly employed to describe heterogeneous systems and/or  
 400 chemisorption in gas-solid systems [94]. The equation describes the process of adsorption as a  
 401 collection of reactions which includes diffusion (of the bulk phase, surface diffusion and active catalytic  
 402 surfaces); it also considers the variation of energetics in relation to surface coverage and the decrease  
 403 in adsorption rate [95,96], further supporting the hypothesis of ZOPT's heterogeneity. Visually  
 404 however, all three of the kinetic models fail to accurately describe the three (visually) distinct regions  
 405 in the measured data. This can be a result of the existence of multiple diffusion mechanisms,  
 406 determining the rate of adsorption [97]. This was confirmed by plotting  $q_t$  vs  $t^{1/2}$  which revealed the  
 407 three individual linear regions. The data has therefore, been fitted with a piecewise IPD function which

408 is theoretically consistent with the original model based on the recommendations of Wang and Guo  
 409 [98]; the equations are provided in EQ. 2, EQ. 3 and EQ. 4, and the fitted plot in Figure 12 (right).

$$q_t = k_{IPD1} \cdot t^{1/2} \quad \text{EQ. 2}$$

$$q_t - q_{t1} = k_{IPD2}(t - t_1)^{1/2} \quad \text{EQ. 3}$$

$$q_t - q_{t2} = k_{IPD3}(t - t_2)^{1/2} \quad \text{EQ. 4}$$

410 The IPD model can only represent the mass transfer step which is limited by intraparticle diffusion. It  
 411 has however, revealed that three main steps exist in the adsorption of CO<sub>2</sub> by ZOFT. It can be seen that  
 412 the rate constant decreases in the order of  $k_{IPD1} < k_{IPD2} < k_{IPD3}$  suggesting a gradual reduction in  
 413 adsorption rate and an increase in the diffusional resistance [58]. The initial adsorption rate is significant  
 414 as a result of strong adsorbent-adsorbate interactions [99], lending ZOFT towards application in kinetic  
 415 separations, within the first minute, the adsorption capacity was recorded at 1.2 mmol g<sup>-1</sup>, 65 % of the  
 416 measured equilibrium.

### 417 **3.5. Enthalpy of CO<sub>2</sub> Adsorption**

418 The enthalpy of adsorption can be estimated for a specific adsorptive through analysis of the adsorbent's  
 419 equilibrium adsorption isotherms. It can be calculated *via* the Clausius-Clapeyron equation which is  
 420 provided in EQ. 5 where  $p$  is the vapor pressure,  $T$  is the absolute temperature and  $\Delta H_{ads}$  is the molar  
 421 enthalpy of adsorption.

$$\frac{dp}{dT} = \frac{p \cdot \Delta H_{ads}}{-RT^2} \quad \text{EQ. 5}$$

422 In this research the methodology provided by Nuhnen and Janiak [100] is adopted using the model  
 423 parameters provided by the Toth isotherm fitting. Knowledge of this property facilitates estimation of  
 424 the energy requirement for removing the adsorbate from the spent adsorbent. In the context of  
 425 temperature swing processes this would increase the heat demand for regeneration. The isosteric  
 426 enthalpy of adsorption for ZOFT has been calculated as -40.2 kJmol<sup>-1</sup>. This value increases at lower  
 427 loadings, reaching a maximum at around -86 kJmol<sup>-1</sup> close to zero coverage, further supporting the  
 428 notion that ZOFT presents significant heterogeneity. This heterogeneity results in the few adsorption  
 429 sites which have the highest energies being occupied at the lowest coverage [100]. These sites are those  
 430 provided by the cations within the framework which have been reported to present enthalpies of  
 431 adsorption between -30 and -90 kJmol<sup>-1</sup> [27]. The enthalpy of adsorption is expected to drop to a value  
 432 between -20 to -30 kJmol<sup>-1</sup> at higher adsorption pressures (> 1 bar). Here, the main adsorbate-adsorbent  
 433 interactions arise from the interaction of CO<sub>2</sub> with the framework oxygen [101].

### 3.6. Working capacity

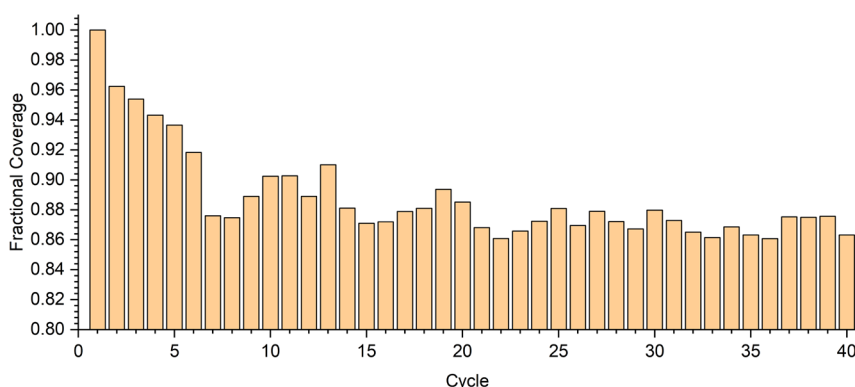


Figure 13: Working CO<sub>2</sub> adsorption capacity of the optimised BFA-derived zeolite. Adsorption at 50 °C, 100 mol%CO<sub>2</sub> at 1 atm for 2 h; desorption at 150 °C, 100 mol%N<sub>2</sub> at 1 atm for 1 h.

435 Although knowledge of the isosteric enthalpy of adsorption facilitates approximation of the energy  
 436 demand for adsorbent regeneration, in order to understand the working capacity of ZOFT, a simulated  
 437 temperature swing adsorption process has been employed. Repetition of an adsorption (50°C, 50  
 438 mLmin<sup>-1</sup> CO<sub>2</sub>, 1 atm) and desorption (150°C, 50 mLmin<sup>-1</sup> N<sub>2</sub>, 1 atm) step for a total of 40 complete  
 439 cycles was carried out *via* TGA. The duration of the adsorption and desorption steps was 2 and 1 h,  
 440 respectively. The data is presented in Figure 13 where  $\theta$  is the uptake as a fraction based on the original  
 441 uptake. There is a strong decline in capacity between cycle 1 and cycle 6 before the value stabilises at  
 442 a 0.85 with some oscillation for the subsequent cycles. This reduction is quite significant after 40 cycles  
 443 as most commercial adsorbents are expected to stay in operation for significantly longer. This could be  
 444 the result of insufficient cycle times for both the adsorption and more importantly the desorption steps  
 445 which may fail to fully regenerate the adsorbent. Hysteresis is quite commonly reported for type A  
 446 zeolites which belong to the small-pore classification, where adsorption tends to be limited by the  
 447 diameter of the  $\alpha$ -cages whilst desorption is controlled by the effective pore aperture [102].

### 448 4. Conclusion

449 The hydrothermal conditions of an alkaline fusion-assisted synthesis have been optimised through  
 450 Taguchi Design of Experiment employing an L9 OA by evaluating the effect of 4 parameters at 3 levels  
 451 on the prepared adsorbent's equilibrium CO<sub>2</sub> uptake. Both the temperature and duration of the  
 452 hydrothermal treatment alongside the liquid to solid ratio were observed to be statistically significant  
 453 with an optimum set of conditions identified with a 90 °C hydrothermal treatment for 10 h employing  
 454 a liquid to solid ratio of 5. The ratio of NaOH to fly ash was revealed have no statistically significant  
 455 main effect on the dependent variable or signal to noise ratios. The optimum sample presented an  
 456 equilibrium CO<sub>2</sub> adsorption capacity of 1.84 mmolg<sup>-1</sup> measured with 100 mol%CO<sub>2</sub> *via* TGA at 50 °C;  
 457 volumetric measurements confirmed this capacity which reached a maximum of 2.92 mmolg<sup>-1</sup> at 0 °C  
 458 and 1 bar. Modelling of the equilibrium and kinetic isotherms revealed a heterogeneous adsorbent with



459 various adsorption sites and multiple rate-controlling mechanisms which is to be expected from a  
460 mixed-phase zeolite as confirmed by XRD. The enthalpy of adsorption was identified to be coverage  
461 dependent with a calculated value at zero coverage of  $-86 \text{ kJmol}^{-1}$  reducing to  $-40.2 \text{ kJmol}^{-1}$  at a  
462 coverage of  $2 \text{ mmolg}^{-1}$ . The working capacity of the adsorbent over 40 cycles was measured to be  
463 around 85% which was attributed to an insufficient desorption temperature and time. This work presents  
464 a feasible route to biomass combustion ash valorisation in the context of carbon capture and storage.  
465 The production of high performing zeolites detailed in this paper intends to reveal the potential value  
466 in this waste resource as a precursor to value-added adsorbents and catalysts. Future work should focus  
467 on scaling up the synthesis of zeolites before assessment of the adsorbent's performance in a  
468 representative process configuration to reveal the mass transfer phenomena and breakthrough  
469 performance. This will allow assessment of the expected efficiency for biomass-combustion fly ash-  
470 derived kinetic separations.

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## 485 **Author Contributions**

486 **BP:** Writing (Original Draft & Editing), Conceptualisation, Methodology, Investigation, Formal  
487 Analysis, Validation, Visualisation; **MG:** Methodology; Validation; Visualisation; **SMS**  
488 **(corresponding author):** Supervision, Funding Acquisition, Writing (Review & Editing), Resources,  
489 Conceptualisation, Project Administration.

## 490 **Data Availability Statement**

491 Data have been made available in Brunel University London’s repository *via* [Brunel Figshare database](#).

## 492 **Declaration of Competing Interest**

493 The authors declare that they have no known competing financial interests or personal relationships that  
494 could have appeared to influence the work reported in this paper.

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