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Nucleation competition and phase transformation mechanisms in recycled aluminium alloys: Insights into θ -Al₁₃Fe₄, Al₆(Fe,Mn) and α -Al₁₅(Fe, Mn)₃Si₂

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A R T I C L E I N F O	A B S T R A C T
Keywords: Phase competition Fe-bearing intermetallic compounds Solidification Phase transformation First-principles	Aluminium rich Fe-bearing intermetallic compounds (Fe-IMCs) plays a critical role in determining the me- chanical properties of recycled aluminium alloys due to inevitable Fe accumulation during recycling. The Fe- IMCs which have a needle-/plate-like morphology are particularly detrimental, impairing the ductility and overall performance of aluminium alloys. Consequently, optimizing phase selection to favour less harmful Fe- IMCs is a critical strategy for improving alloy design and enhancing material properties. The nucleation of Fe- IMCs, however, is challenging because it requires precise structural and compositional templating, involving multiple alloying elements at specific atomic positions, and thus necessitates substantial undercooling. This study examines a complicated primary phase selection among θ -Al ₁₃ Fe ₄ and Al ₆ (Fe,Mn) and α -Al ₁₅ (Fe,Mn) ₃ Si ₂ in an Al-5Mg-2Si-0.6Mn-1.3Fe alloy. Experimental results show θ -Al ₁₃ Fe ₄ and Al ₆ (Fe,Mn) solidify as non-equilibrium primary phases ahead of the equilibrium α -Al ₁₅ (Fe,Mn) ₃ Si ₂ , with subsequent transformation to α -Al ₁₅ (Fe,Mn) ₃ Si ₂ during later stages. Phase competition and transformation mechanisms were characterized using scanning electron microscope (SEM), electron backscatter diffraction (EBSD) and transmission electron microscope (TEM), with experimental results supported by first-principles modelling. Particular focus was given to the transition from the silicon-unfavourable Al ₆ (Fe,Mn) to the silicon-rich α -Al ₁₅ (Fe,Mn) ₃ Si ₂ . The findings provide a novel framework for designing recycled aluminium alloys with enhanced mechanical properties by optimizing Fe-IMC phase selection and transformation pathways.

1. Introduction

Full metal circularity, in which the global demand for metallic materials met by the circulation of secondary metals through reduction, reuse, remanufacture, recycling and recovery, is a vital response to this challenge [1,2]. Aluminium recycling only costs 5 % energy and reduces 95 % greenhouse gas emission compared to the primary aluminium production [3,4]. Although currently majority of aluminium scraps have been recycled, most of them were downcycled or diluted with primary aluminium [5,6]. Impurities such as Fe in the scraps are one of the most important reasons for it [7,8]. Fe, as an unavoidable impurity in current aluminium (Al) industry, plays important role in determining the mechanical properties of Al-alloys. The accumulation of Fe content from the casting and recycling process has been an urgent issue to be solved for aluminium recycling.

Due to the low solubility of Fe in the aluminium, the Fe is easily to

form the aluminium rich Fe-bearing intermetallic compounds (Fe-IMCs) with Al. The Fe-IMCs are challenging to refine or modify once the alloys have solidified. However, there are two opportunities to alter these Fe-IMCs during the manufacturing process of Al alloys. The first opportunity arises during the solidification process (casting), where initial phase formation can be influenced. It is known that the equilibrium phase diagram is hardly to predict the formation of the Fe-IMCs due to the kinetical factors and nucleation competition among different types of Fe-IMCs [9]. Understanding the complexity of Fe-IMC formation has significantly advanced over the past decade [9–13]. This progress stems from recognizing the challenges of nucleation, which necessitate both structural and compositional templating [12]. These templates require multiple alloying elements to occupy specific atomic positions, resulting in the need for significant nucleation undercooling. It has been reported that the nucleation undercoolings of different types of Fe-IMCs follows the sequence: θ -Al₁₃Fe₄< Al₆(Fe,Mn) < α -Al₁₅(Fe,Mn)₃Si₂ [14]. This

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sequence reflects the increasing difficulty of nucleation, correlating with the number of the constitute alloying elements required. Subsequent technological advancements have demonstrated that the nucleation potency of the specific Fe-IMCs can be manipulated through composition and structural templating [12,15]. Studies revealed that pre-templating Fe and Si on the Al/(10 $\overline{1}$ 0)AlB₂ interface effectively facilitated the heterogeneous nucleation of α -Al₁₅(Fe,Mn)₃Si₂, leading to significant refinement of this compound [12].

The second opportunity is during heat treatment, which can facilitate the phase transformations and modify the morphology of small size Fe-IMCs. The composition and the crystal structure of these Al-Fe compounds are very flexible. For example, the Al-Fe compounds are easily incorporated with the other allying elements such as Si, Mn, Cr, Ni, Co, etc. [16–20]. Different alloying elements doping in the Al-Fe intermetallic compounds (IMCs) cause the composition and the crystal structure variation [16–21]. Therefore, there are more than 20 types of Fe-IMCs reported so far. Most of the alloying elements incorporating in the Fe-IMCs by replacing the atomic position of Al or Fe, such as Si replacing the Al atoms in θ -Al₁₃Fe₄, Mn replace the Fe atoms in most of the Fe-IMCs. Recent research reported that the vanadium can also possibly incorporate into θ -Al₁₃Fe₄ by partially occupying atomic position of Al [22].

The incorporation of Si is generally facilitating phase transformations among different types of the Fe intermetallic compounds [13,23,24]. A typical example showing the phase transformation sequence from θ -Al₁₃Fe₄ to α '-Al₈Fe₂Si, β -Al₅FeSi and then δ -Al₄Fe₂Si demonstrated that these phase transitions are diffusion control and the phase transition sequence follows the increasing Si concentration in these Fe-IMCs. The morphology of the Fe-IMCs can be modified due to the phase transition, which therefore benefits the mechanical properties. Recently research work [25] demonstrated the benefits of mechanical properties improvement from phase transformation between Al₆(Fe,Mn) and the α-AlFeSi during the heat treatment process, in which Si content in the crystals plays an important role. Meanwhile previous investigations on this type of phase transformation have primarily focus on describing composition and morphology and the understanding of the underlaying mechanism remains limited due to the absence of an observable specific crystallography orientation relationship.

In this study, the co-selection of three different types of primary Fe-IMs including $\theta\text{-Al}_{13}\text{Fe}_4$, Al_6(Fe,Mn), $\alpha\text{-Al}_{15}(\text{Fe},\text{Mn})_3\text{Si}_2$ was observed during the solidification of an Al-5Mg-2Si-0.6Mn-1.3Fe alloy poured at 700 °C with a cooling rate of 3.5 K/s. The selected non-equilibrium $\theta\text{-Al}_{13}\text{Fe}_4,\ \text{Al}_6(\text{Fe},\text{Mn})$ phase transformed into equilibrium $\alpha\text{-Al}_{15}(\text{Fe},$ Mn)₃Si₂ in the following solidification process. The complex competition among multiple primary Fe-IMCs will be examined using various characterization methods, ranging from SEM to crystallographic analysis. Phase transitions between θ-Al₁₃Fe₄/α-Al₁₅(Fe,Mn)₃Si₂, θ-Al₁₃Fe₄/ Al₆(Fe,Mn), and Al₆(Fe,Mn)/ α -Al₁₅(Fe,Mn)₃Si₂ are investigated by mean of a combination of experimental techniques including scanning electron microscope (SEM) and transmission electron microscope (TEM) and first-principles' modelling. Parameter-free first-principles method is employed to obtain insights into the intrinsic structural properties and energetics of related intermetallic compounds. This method provides valuable formation to understand the formation and transformation of Fe-IMCs during solidification [26–28].

2. Experimental

2.1. Casting and characterization

The nominal composition of the studied alloy is Al-5Mg-2Si-0.6Mn-1.3Fe. The actual composition of the studied alloy is 5.1 ± 0.5 Mg, 2.0 ± 0.3 Si, 0.6 ± 0.1 Mn and 1.3 ± 0.05 Fe (in wt%) with Al balance. The phase diagram and the solidification curve were calculated with Pandat software [29] with Scheil model [30] and displayed in Fig. 1. The



Fig. 1. (a) Calculated phase diagram of the Al-5.1Mg-2.0Si-0.6Mn-xFe alloy system, and (b) simulated solidification curve of the Al-5.1Mg-2.0Si-0.6Mn-1.3Fe alloy.

thermodynamics study showed that the solidification sequence of the studied Al-5.1Mg-2.0Si-0.6Mn-1.3Fe alloy was as: $L \rightarrow \alpha$ -Al₁₅(Fe,Mn)₃Si₂ (P-IMC), L $\rightarrow \alpha$ -Al₁₅(Fe,Mn)₃Si₂ (BE-IMC) + α -Al, and L $\rightarrow \alpha$ -Al₁₅(Fe, Mn)₃Si₂ (TE-IMC) + α Al + Mg₂Si. The calculated liquidus is 668.7 °C. The composition of the studied alloy is very close to the threshold required for solidification with primary 0-Al₁₃Fe₄. However, it is significantly different from the composition needed for solidification with primary Al₆(Fe,Mn). Commercially pure Al (>99.8 wt%), commercially pure (CP) Mg (>99.95 wt%), and master alloys of Al-50 wt% Si, Al-20 wt% Mn, and Al-38 wt% Fe were utilized for the castings. The vaporization of certain alloying elements, such as Mg, was taken into account, and an additional amount of master alloys was added to ensure the actual composition closely matched the nominal alloy composition. The CP-Al samples were melted at 750°C in electric resistance furnace. Subsequently, the other master alloys, excluding CP-Mg, were added to the Al melt and stirred thoroughly to ensure complete dissolution. At last, CP-Mg wrapped in a thin Al foil preheated to 200°C, was added to the melt. Once the Mg had completely melted, the melts were held for further 30 minutes. After removing the slag, the melt was cast into a Tp-1 mould preheated to 380 °C. The Tp-1 mould is specifically designed to provide a cooling rate of 3.5 K/s at the sample section 38 mm from the bottom, which is comparable to the cooling rate of directional chilled casting [31]. The pouring temperature is 700°C.

A phase competition between primary θ -Al₁₃Fe₄ and α -Al₁₅(Fe, Mn)₃Si₂ of this studied alloy, when casted at 720°C with a cooling rate of 3.5 K/s, has been reported in previous study [13]. The nucleation competition and the subsequent phase transformation, as well as the related transition mechanism between non-equilibrium θ -Al₁₃Fe₄ and equilibrium α -Al₁₅(Fe,Mn)₃Si₂, have been clearly investigated. In this study, an even complex phase competition among three different primary Fe-IMCs: Al₆(Fe,Mn), θ -Al₁₃Fe₄ and α -Al₁₅(Fe,Mn)₃Si₂, will be presented, and the subsequent phase transformation, among these three

different phases will be further examined. Multiple influencing factors, such as cooling rate, nucleation undercooling, elemental diffusion and composition segregation, and the relationship between composition, lattice parameters, and crystallography, will be investigated to explain the mechanism of this complex nucleation competition and phase transformation.

Metallographic specimens were prepared using the standard procedures. The as-cast microstructure characteristics of the samples were examined using a Zeiss optical microscope fitted with the Axio Vision 4.3 image analysis software. The electron backscatter diffraction (EBSD) technique was applied for phase identification and examining the phase relationships among the solidified Fe-IMCs in Al-5Mg-2Si-0.6Mn-1.3Fe alloy. The scanning step size was 0.1-0.5µm. To observe the 3-dimensional (3D) morphology of intermetallic compounds in this study, the as-cast samples were deep etched in 15 % HCl solution for 2–3 minutes followed the methanol bath. The EBSD and SEM investigation were made on a Zeiss Cross beam 340 FIB-SEM operated at an accelerating voltage of 20 kV. To investigate the interface between different Fe-IMCs, the transmission electron microscopy (TEM) sample was prepared with focused ion beam (FIB) on the Zeiss Cross beam 340 FIB-SEM. TEM examination was performed on a JEOL 2100 F transmission electron microscope equipped with EDX spectrometer operated at an accelerating voltage of 200 kV.

2.2. Computational methods

The first-principles Vienna *Ab initio* Simulation Package (VASP) [32] was utilized for the calculations in this work. VASP uses the density-functional theory within the projector-augmented wave (PAW) method [33]. The (spin-polarized) generalized gradient approximation was employed for the exchange and correlation energy terms [34]. The cut-off energy of the wave functions was set to be 550 eV and the cut-off energy of the augmentation functions was set to be 700 eV. The electronic wave functions were sampled on dense grids in the irreducible Brillouin zone (BZ) of the systems. Structural optimizations were performed for both lattice parameters and coordinates of atoms. Different k-meshes and cut-off energies were tested for the waves and augmentation waves, respectively. Tests showed a good convergence (<1 meV per atom).

3. Results

3.1. Heterogeneous nucleation competition among $Al_6(Fe,Mn)$, θ - $Al_{13}Fe_4$ and α - $Al_{15}(Fe,Mn)_3Si_2$

Fig. 2 shows the SEM-BSD images of the as-cast microstructure of Al-5Mg-2Si-0.6Mn-1.3Fe cast at 700 °C with a cooling rate of 3.5 K/s, illustrating the complex phase selection among multiple Fe-bearing intermetallic compounds. Three different types of Fe-IMCs with distinct morphologies can be easily recognized in Fig. 2a. The predominant Fe-IMC, exhibiting a Chinese script morphology, is identified as α-Al₁₅(Fe,Mn)₃Si₂, confirmed later through EBSD and TEM analysis. The average composition of α -Al₁₅(Fe,Mn)₃Si₂ is found to be 5.7 at% Si, 10.2 at% Fe and 4.6 at% Mn. The plate-like Fe-IMC (minor phase) is identified as θ -Al₁₃Fe₄ later with EBSD. A small amount of Si (2.6 at%) and Mn (2.2 at%) are incorporated into 0-Al13Fe4, but the crystal structure remains unchanged. A few Fe-IMCs particles with coarse branch spacing and a Chinese script morphology were identified as Al₆(Fe,Mn) later through EBSD and TEM analysis. Unlike the other Fe-IMCs, no Si was detected in Al₆(Fe,Mn), which is a distinctive characteristic of this phase. Notably, the majority of Al₆(Fe,Mn) particles solidified at the very edge of the sample, where the cooling rate is higher, as shown in Fig. 2b. Fig. 2c reveals that the Al₆(Fe,Mn) exhibit a hollow morphology, which corresponds to the structure reported in [35].

Further SEM investigation shows that three different types of primary Fe-IMCs: α -Al₁₅(Fe,Mn)₃Si₂, Al₆(Fe,Mn) and θ -Al₁₃Fe₄ can solidify



Fig. 2. SEM-BSD images of the as-cast microstructure of Al-5Mg-2Si-0.6Mn-1.3Fe cast at 700 °C with a cooling rate of 3.5 K/s, showing the multiple phase selection of Fe-bearing intermetallic compounds. (a) Central region of the sample showing predominant α -Al₁₅(Fe,Mn)₃Si₂ with Chinese script morphology, minor θ -Al₁₃Fe₄ with needle/plate-like morphology, and trace Al₆(Fe,Mn) with hollowed Chinese script morphology. (b) Edge region of the sample showing dominant Al₆(Fe,Mn) with hollowed Chinese script morphology and α -Al₁₅(Fe,Mn)₃Si₂ with Chinese script morphology and α -Al₁₅(Fe,Mn)₃Si₂ with Chinese script morphology. (c) Magnified view of the Al₆(Fe,Mn) from the green dotted area in (b), revealing its hollowed Chinese script morphology.

and initiate the formation of the same Fe-IMCs in the subsequent binary eutectic. The results are shown in Fig. 3. Fig. 3a shows that the compact α -Al₁₅(Fe,Mn)₃Si₂ nucleates the binary eutectic α -Al₁₅(Fe,Mn)₃Si₂ with Chinese script morphology. Fig. 3b reveals that the hollowed Al₆(Fe,Mn) needles nucleate the binary eutectic (Al₆(Fe,Mn) + α -Al), also exhibiting a Chinese script/hollow morphology. Fig. 3c presents that the plate-like θ -Al₁₃Fe₄ nucleates the binary eutectic (θ -Al₁₃Fe₄ + α -Al), maintaining a plate-like morphology.

3.2. Phase transformation between $Al_6(Fe,Mn)/\theta - Al_{13}Fe_4$, $\theta - Al_{13}Fe_4/\alpha - Al_{15}(Fe,Mn)_3Si_2$ and $Al_6(Fe,Mn)/\alpha - Al_{15}(Fe,Mn)_3Si_2$

However, upon closer examination, several phase transformations between these Fe-IMCs were observed. Fig. 4a shows that the compacted primary α -Al₁₅(Fe,Mn)₃Si₂ has actually transformed from primary θ -Al₁₃Fe₄. Fig. 4b displays that the plate-like primary θ has transformed into α at the surface, thereby nucleating the Chinese script binary



Fig. 3. SEM-BSD images of the as-cast microstructure of Al-5Mg-2Si-0.6Mn-1.3Fe alloy cast at 700 °C with a cooling rate of 3.5 K/s, showing that each type of selected primary Fe-containing compounds can serve as a nucleation site for the same phase in the following solidified binary eutectic (BE) structure. (a) Primary α-Al₁₅(Fe,Mn)₃Si₂ with a compact morphology nucleating Chinese script BE-α-Al₁₅(Fe,Mn)₃Si₂. (b) Hollowed primary Al₆(Fe,Mn) nucleated the Chinese script Al₆(Fe,Mn). (c) Needle-/plate-like primary θ-Al₁₃Fe₄ initiating the formation of θ-Al₁₃Fe₄ in the binary eutectic. (Note: α denotes α-Al₁₅(Fe, Mn)₃Si₂, θ represents θ-Al₁₃Fe₄.).

eutectic- α . Fig. 4c presents that the solidified primary Al₆(Fe,Mn) has transformed into a double-phase structure of α -Al₁₅(Fe,Mn)₃Si₂ and α -Al, which subsequently nucleated the binary eutectic α -Al₁₅(Fe, Mn)₃Si₂.

The 3D morphology of these characterizations is presented in Fig. 5. Fig. 5a demonstrates that when small-sized θ particles transform into α and are fully covered by α particles, the phase transformation phenomenon is easily to be covered without careful observation. The details of this challenge have been well explained in our previous publication with SEM, EBSD and CT analyses [13]. This highlights the challenge in understanding the difficulty of the formation of Fe-IMCs. Fig. 5b shows the typical plate-like structure of the θ phase, with tiny steps/defaults on the plates. Some α -Al₁₅(Fe,Mn)₃Si₂ particles can be observed to nucleate on these plates, likely due to the phase transformation from θ to α occurring on these surfaces. Fig. 5c presents Al₆(Fe,Mn) needles that have transformed into α -Al₁₅(Fe,Mn)₃Si₂ and α -Al double phases at the surface, which then nucleated the following binary α -Al₁₅(Fe,Mn)₃Si₂.

Fig. 2b shows that at the edge of the Tp-1 sample, $Al_6(Fe,Mn)$ solidifies as the dominating Fe-IMC. The potential phase transformation in these $Al_6(Fe,Mn)$ rich area was investigated using EBSD mapping, shown in Fig. 6. The phase mapping in Fig. 6b reveals two different types of



Fig. 4. SEM-BSD images of the as-cast microstructure of Al-5Mg-2Si-0.6Mn-1.3Fe cast at 700 °C with a cooling rate of 3.5 K/s, showing transformation pathways of primary Fe-IMCs and their role in eutectic nucleation. (a) Primary θ -Al₁₃Fe₄ transformed into compact primary α -Al₁₅(Fe,Mn)₃Si₂ which subsequently nucleated the binary eutectic α -Al₁₅(Fe,Mn)₃Si₂. (b) Needle/plate-like θ -Al₁₃Fe₄ partially transformed at the surface into α -Al₁₅(Fe,Mn)₃Si₂ and acted as a nucleation site for the eutectic α -Al₁₅(Fe,Mn)₃Si₂. (c) Primary Al₆(Fe, Mn) transformed into a dual-phase region comprising α -Al₁₅(Fe,Mn)₃Si₂.

phase transition: Al₆(Fe,Mn) (pink) to α -Al₁₅(Fe,Mn)₃Si₂ (green), and Al₆(Fe,Mn) (pink) to θ -Al₁₃Fe₄ (blue). A portion of the Al₆(Fe,Mn) remains untransformed.

However, compared to the distinct phase transition characterization between $Al_6(Fe,Mn)$ and α - $Al_{15}(Fe,Mn)_3Si_2$ (Figs. 4c and 5c), the phase transformation between Al₆(Fe,Mn) and θ -Al₁₃Fe₄ is less apparent and difficult to observe under SEM. The Al₆(Fe,Mn) particle identified for the $Al_6(Fe,Mn)/\theta$ - $Al_{13}Fe_4$ phase transition in Fig. 6b was re-examined with SEM, and the results are shown in Fig. 7. Fig. 7a shows no visible phase transformation characterization, like that observed between Al₆(Fe,Mn) and α -Al₁₅(Fe,Mn)₃Si₂. However, the SEM-line scanning spectrum in Fig. 7b reveals a composition variation from left to right, with increasing Fe, decreasing Mn and no or very small increases in Si concentration. The composition of different types of Fe-IMC in this study, shown in Table 1, reveals that, compared to $Al_6(Fe,Mn)$, θ - $Al_{13}Fe_4$ has a much higher Fe concentration, lower Mn and can incorporate up to 2.6 at% Si. The examination results from the EBSD mapping (Fig. 5) and the SEM-EDS line scanning (Fig. 7) demonstrate that phase transition from Al₆(Fe,Mn) to θ -Al₁₃Fe₄ happened.

The phase transitions between Al₆(Fe,Mn)/\alpha-Al₁₅(Fe,Mn)₃Si₂, and



Fig. 5. SEM images of the as-cast microstructure of Al-5Mg-2Si-0.6Mn-1.3Fe alloy cast at 700 °C with a cooling rate of 3.5 K/s, showing the 3-dimensional (3D) morphology and interconnectivity of Fe-IMCs. (a) Primary α -Al₁₅(Fe, Mn)₃Si₂ particle connected to eutectic α -Al₁₅(Fe,Mn)₃Si₂ with Chinese script. (b) Plate-like θ -Al₁₃Fe₄ with stepped surfaces connected to compact/Chinese script α -Al₁₅(Fe,Mn)₃Si₂. (c) Hollow needle-like Al₁₅(Fe,Mn)₃Si₂.

 θ -Al₁₃Fe₄/ α -Al₁₅(Fe,Mn)₃Si₂ were compared under SEM-BSD examination, as shown in Fig. 8. Fig. 8a shows that the primary Al₆(Fe,Mn) particle transformed into α -Al₁₅(Fe,Mn)₃Si₂ and α -Al double phases at the surface, while the shape of the original Al₆(Fe,Mn) particle remains unchanged. Notably, the transformed double phases exhibit a lamellar morphology rather than the randomly distributed, nano-sized, or rod-like structures reported in [23,24]. The lamellar plates are aligned perpendicular to the interface (orange frame). The phase transformation can be defined as:

 $\label{eq:Liquid} \mbox{Liquid} + \mbox{Al}_6(\mbox{Fe},\mbox{Mn}) \rightarrow \mbox{α-Al}_{15}(\mbox{Fe},\mbox{Mn})_3\mbox{Si}_2 + \mbox{α-Al}.$

Fig. 8b shows that the θ -Al₁₃Fe₄ transformed into α -Al₁₅(Fe,Mn)₃Si₂ but retained its original size. No lamellar morphology can be observed in this transformed structure. Instead, a few randomly distributed α -Al dots are seen within the transformed α -Al₁₅(Fe,Mn)₃Si₂. The phase



Fig. 6. The EBSD mapping of the Al₆(Fe,Mn-rich area located at the edge of the TP-1 sample, showing two different types of phase transition: Al₆(Fe,Mn) $\rightarrow \alpha$ -Al₁₅(Fe,Mn)₃Si₂, and Al₆(Fe,Mn) $\rightarrow \theta$ -Al₁₃Fe₄. (a) SEM image of the mapped area. (b) Phase map identifying the constituent intermetallic phases. (c) Phase map overlaied with image quality (IQ) contrast, and (d) inverse pole figure (IPF) map.

transformation can be defined as:

Liquid + θ -Al₁₃Fe₄ $\rightarrow \alpha$ -Al₁₅(Fe,Mn)₃Si₂ + α -Al.

Details on the phase transformation between $\theta\text{-Al}_{13}Fe_4$ and $\alpha\text{-Al}_{15}(Fe,Mn)_3Si_2$ have been reported previously [13]. Therefore, this study will focus on the phase transformation between Al_6(Fe,Mn) and $\alpha\text{-Al}_{15}(Fe,Mn)_3Si_2$.

3.3. Nature of phase transformation from Si-free $Al_6(Fe, Mn)$ to Si-rich α - $Al_{15}(Fe,Mn)_3Si_2$

The interface of the phase formation between Al₆(Fe, Mn) and α -Al₁₅(Fe,Mn)₃Si₂ were examined using TEM, and the results are shown in Fig. 9. Fig. 9a presents the bright field TEM image of a FIB sample, showing the interface between the Al₆(Fe,Mn) and the transformed lamellar structure consisting of α -Al₁₅(Fe,Mn)₃Si₂ and α -Al. The selected area electron diffraction (SAED) patterns for α -Al₁₅(Fe,Mn)₃Si₂, Al₆(Fe, Mn) and α -Al, viewed along their low zone directions, are displayed in Fig. 9b, c and d. To investigate the orientation relationship between Al₆(Fe,Mn) and α -Al₁₅(Fe,Mn)₃Si₂, these two Fe-IMCs were carefully examined along different zone axes within the limitations of TEM operation (α and β tilt angles). No specific orientation relationship could be found between Al₆(Fe,Mn) and α -Al₁₅(Fe,Mn)₃Si₂, which is different to the other types of phase transformation between Fe-IMCs [23,24].

The interface between α -Al₁₅(Fe,Mn)₃Si₂ and α -Al was also investigated using TEM. The results are shown in Fig. 10. Fig. 10 a is the bright field TEM image displaying the interface between the transformed lamellar α -Al₁₅(Fe,Mn)₃Si₂ and α -Al when α -Al₁₅(Fe,Mn)₃Si₂ is viewed along the [1 0 0] zone direction. Fig. 10b shows the absence of a specific orientation relationship between α -Al₁₅(Fe,Mn)₃Si₂ and α -Al. Although



Fig. 7. (a) SEM line scan across a hollowed Al_6 (Fe,Mn) particle showing compositional variation, and (b) corresponding EDS spectrum profile from left to right, showing an increase in Fe content and a decrease in Mn content along the scan path.

 Table 1

 The average composition (at%) of different types of Fe-IMCs in this study.

Fe-IMCs		Al	Fe	Mn	Si
Al ₆ (Fe,Mn)	SEM-	86.48	9.27	4.25	ND (non-
	EDS	± 0.5	± 0.4	\pm 0.2	detected)
Al ₆ (Fe,Mn)	TEM-	88.87	7.42	3.73	ND
	EDS	± 0.4	± 0.3	\pm 0.2	
Primary	TEM-	79.5	10.2	4.6	$\textbf{5.7} \pm \textbf{0.2}$
α-Al ₁₅ (Fe,	EDS	± 0.6	± 0.5	\pm 0.2	
Mn) ₃ Si ₂					
Binary eutectic	TEM-	79.1	8.9	5.7	$\textbf{6.3} \pm \textbf{0.2}$
α-Al ₁₅ (Fe,	EDS	± 0.4	\pm 0.4	\pm 0.2	
$Mn)_3Si_2$					
Ternary eutectic	TEM-	84.95	13.1	0.75	1.2 ± 0.05
α-Al ₁₅ (Fe,	EDS	± 0.4	± 0.5	\pm 0.0	
Mn) ₃ Si ₂					
θ-Al ₁₃ Fe ₄	TEM-	78.6	18.7	2.2	2.6 ± 0.1
	EDS	± 0.4	± 0.5	± 0.1	

 α -Al₁₅(Fe,Mn)₃Si₂ is typically reported as (1 1 0) faceted intermetallic compound [36], in this samples, no faceted surface can be observed at between the α -Al₁₅(Fe,Mn)₃Si₂ and α -Al, instead of some diffusion trace observed at the interface as shown in Fig. 10b. The α -Al was then tilted and further investigated under different zone directions, but still, no specific orientation relationship between α -Al₁₅(Fe,Mn)₃Si₂ and α -Al could be found. Additionally, when viewed along the [1 1 0] zone direction of α -Al, some needle-like precipitates were observed in the α -Al originating from the lamellar structure (Fig. 10c). These precipitates may be the result of solutes rejected during the phase transformation

between Al_6(Fe,Mn) and $\alpha\text{-Al}_{15}(Fe,Mn)_3Si_2,$ balancing the composition at the interface.

3.4. Computational results on the stability of Al_6 (Fe, Mn), θ - $Al_{13}Fe_4$ and α - Al_{15} (Fe, Mn)₃Si₂

To assess the relative stability of different Fe-IMCs, the formation energy (ΔE_f) per M (M = Fe or Mn) atom of (Al_{1-x}Si_x)_z(Fe_{1-y}Mn_y) is defined by the following equation:

$$\Delta E_f = E\{(Al_{1-x}Si_x))_z(Fe_{1-y}Mn_y)\} - \{z[(1-x)E(Al) + xE(Si)] + (1-y)E(Fe^*) + yE(Mn^*)\}$$
(1)

Here, x, y, z are compositional parameters, representing the fraction of Si, Mn and Fe in the intermetallic compound in relation to the elemental solids (α -Al and Si) and solute solution of Fe, Mn in Al matrix. Equ. 1 also indicated that the impurity Si solution at the Al sublattice and Mn at the Fe sublattice, respectively.

Here, $E\{(Al_{1-x}Si_x)\}_z(Fe_{1-y}Mn_y)\}$, E(Al), E(Si), $E(Fe^*)$ and $E(Mn^*)$ represent the calculated total-valence electron energies for $(Al_{1-x}Si_x))_z(Fe_{1-y}Mn_y)$, elemental Al, Si, and the dilute solution energy of Fe and Mn in the Al matrix. A negative value of ΔE_f indicates that the formation of $(Al_{1-x}Si_x))_z(Fe_{1-y}Mn_y)$ is favoured. The unit of ΔE_f is eV/M (M = Fe_{1-x}Mn_x). At temperature T = 0 K and pressure p = 0 Pa, the enthalpy difference is equal to the energy difference, e.g. $\Delta H = \Delta E_f$, when the zero-point vibration contribution is neglected.

First-principles' calculations were firstly performed for the dilute solution of Mn, Fe and Si in the Al matrix. A supercell of $3a_0 \times 3a_0 \times 3a_0$



Fig. 8. SEM-BSD images showing the phase transformation behaviour of primary Fe-IMCs. (a) A primary Al₆(Fe,Mn) particle transforming at the surface into a dual-phase region of α-Al₁₅(Fe,Mn)₃Si₂ and α-Al. The transformed phases exhibit a lamellar morphology, with plates oriented perpendicular to the interface (highlighted by the orange frame), and (b) θ-Al₁₃Fe₄ transforming into α-Al₁₅(Fe,Mn)₃Si₂ while largely retaining its original size, with only a few α-Al dots embedded within the newly formed α-Al₁₅(Fe,Mn)₃Si₂.



Fig. 9. (a) Bright field TEM image from a FIB-prepared sample showing the interface between primaey $Al_6(Fe_3Mn)$ and the transited lamellar (α -Al_{15}(Fe, Mn)_3Si_2 + α -Al). Selected area electron diffraction (SAED) patterns obtained from: (b) α -Al_{15}(Fe,Mn)_3Si_2 with the incident electron beam aligned along the [1 0 0] zone axis, (c) α -Al with the incident electron beam aligned along the [1 0] zone axis, and (d) $Al_6(Fe_3Mn)$ with the incident electron beam aligned along the along the [0 0 1] zone axis.

(where a_0 is the lattice parameter of Al) was employed for these calculations. The calculated solution energy, $\Delta E(M^*)$, for Fe, Mn and Si solution in Al were -0.266 eV/M, -0.348 eV/M and 0.431 eV/M, respectively. These values are in good agreement with previous



Fig. 10. (a) Bright field TEM image showing the interface between the transformed lamellar α -Al_{15}(Fe,Mn)_3Si_2 and α -Al phases. (b) High-resolution TEM (HRTEM) image of the α -Al_{15}(Fe,Mn)_3Si_2 / \alpha-Al interface, viewed along the [1 0 0] zone axis of α -Al_{15}(Fe,Mn)_3Si_2, revealing diffusion features at the interface. (c) HRTEM image of needle-like precipitate within the α -Almatrix, viewed along the [1 1 0] zone axis, along with corresponding fast Fourier transformation (FFT) patterns from both the α -Al and the needle-like phase.

calculations [33,34] using the same approach. The high energy cost of Si solution in Al, caused usage of the bulk Si energy as the reference in Equ. 1.

A. Si stabilizes the α-Al₁₅(Fe, Mn)₃Si₂ phase

The structural model of α -Al₁₅(Fe, Mn)₃Si₂ phase was proposed by Cooper in 1967 [37], building upon their earlier work on the α -Al₁₅(Fe, Mn)₃Si₂ phase [38]. This phase consists of 11 different atomic species, including two types of transition metals and nine types of Al(Si) atoms, with the chemical formula (Al,Si)₁₁₄(Fe, Mn)₂₄. In Cooper's model, an averaged mixing of Fe/Mn atoms was assumed, although no specific discussion regarding the distribution of Si atoms was provided [37]. This structural model has been widely used for analysis of the cubic α -Al₁₅(Fe, Mn)₃Si₂ phase. Therefore, the space group Pm $\overline{3}$ used in the Cooper model represented the 'averaged' structure. In practice, Al/Si or Fe/Mn mixing caused symmetry broken of the systems.

Based on the Cooper model and the current experimental results, we firstly investigated the distribution of Mn within the α phase for the assumed Al_{4.75}(Fe_{2/3}Mn_{1/3}) composition. The computational analysis revealed that the formation energies associated with Mn occuping various Fe sites, as per Cooper's notation [37], are

moderate. The calculated lattice parameters and formation energy for α -Al_{4.75}(Fe_{2/3}Mn_{1/3}) are displayed in Table 3. Notably, the computed formation energy for the Si-free α -Al_{4.75}(Fe_{2/3}Mn_{1/3}) phase is -877 meV/M.

Structural modelling was conducted for configurations with varying Si contents at the different Al sites. The calculations demonstrated that the α phase with the experimental composition, (Al_{0.94}Si_{0.06})_{4.75}(Fe_{2/3}Mn_{1/3}) (Table 1), exhibits the highest stability, with Si partially occupying the Al4 and Al7 sites in Cooper's notation [37]. It is also notable that the experimentally observed chemical composition is notably different from that in the formula, indicating variation of the chemical composition of this phase on preparation conditions. The formation energy of this configuration is –939 meV/M, significantly lower than that of the Si-free α -Al_{4.75}(Fe_{2/3}Mn_{1/3}) phase (-877meV/M). This result indicates that Si stabilizes the α -Al₁₅(Fe, Mn)₃Si₂ phase.

B. The potency for Si doping in Al₆(Fe,Mn)

A previous study reported that the formation energy and lattice parameters of the Al₆(Fe,Mn) phase exhibited moderate changes with increasing Mn content [26]. In the present work, calculations were performed for Al₆(Fe_{0.6875}Mn_{0.3125}) using a $2a_0 \times 2b_0 \times c_0$ supercell, where a_0 , b_0 and c_0 represent the lattice parameters of the conventional cell. This formulation closely aligns with the experimental composition (Table 1). The calculated results, including lattice parameters and formation energy, are presented in Table 3 alongside two related compositions (x(Mn) = 0.25 and x(Mn) = 0.50) for comparison.

The calculated formation energy of Al₆(Fe_{0.6875}Mn_{0.3125}) according to Equ. 1 is -919 meV/M, where M represents Fe_{1-x}Mn_x. This energy lies between those of the two neighbouring compositions. Additionally, the calculations yielded a formation energy of 918 meV/M for Al₆(Fe_{2/3}Mn_{1/3}), which was used for comparison with the cubic α -Al₁₅(Fe, Mn)₃Si₂ phase. The results are consistent with those reported in the previous study [26].

Calculations were also performed to evaluate Si incorporation at the Al sites in Al₆(Fe_{0.6875}Mn_{0.3125}). The results indicated a high energy cost (greater than 0.28 eV) for substituting a single Al atom with Si in this phase. This finding suggests that Si incorporation in Al₆(Fe,Mn) is unlikely due to the significant energy penalty associated with such substitution.

Overall, the calculations revealed that the formation energy of Al₆(Fe_{2/3}Mn_{1/3}) (-0.918 eV/M) is lower than that of the Si-free α -Al_{4.75}(Fe_{2/3}Mn_{1/3}) phase (-877 meV/M), but higher than the Si doped α -(Al_{0.94}Si_{0.06})_{4.75}(Fe_{2/3}Mn_{1/3}) (-939meV/M). These results highlight the critical role of Si stabilization in driving the phase transition from Al₆(FeMn) to α -Al₁₅(Fe, Mn)₃Si₂.

C. Energetics of Si and Mn addition into $\theta\text{-Al}_{13}\text{Fe}_4$

A commonly accepted crystal structure of θ -Al₁₃Fe₄, as determined by Grin, *et al.* using the single crystal diffraction method [39], will be

Table 2

Comparation between the measured lattice parameters of Fe-IMCs in this study and the literature reported.

Phase	а	b	c	Angle	
α-Al ₁₅ (Fe,Mn) ₃ Si ₂ (Primary)	12.618			90°	This work, TEM
α-Al ₁₅ (Fe,Mn) ₃ Si ₂ (Binary Eutectic)	12.27			90°	This work, TEM
α-Al ₁₅ (Fe,Mn) ₃ Si ₂ (Ternary Eutectic)	12.7			90°	This work, TEM
α-Al ₁₅ (Fe,Mn) ₃ Si ₂	12.56			90°	[37]
θ -Al ₁₃ Fe ₄ α -Al	15.492 4.12	8.078	12.47	β = 107.69° 90°	[39] This work, TEM

Table 3

Calculated results for chosen compositions of the Al₆(Fe, Mn) and α -(Al, Si)_{4.75}(Fe, Mn) phases (lattice parameters and formation energies). The lengths of the *a* and *b*-axis are normalized to the primitive cell. a^o and b^o represent the nominated values. \overline{a} represents the average value.

Compound	lattice Parameters (Å)	Δ <i>E</i> (meV/ M)	Remarks
$Al_6(Fe_{0.75}Mn_{0.25})$	a = 7.46 [26] (calc.) b = 6.47 c = 8.78	-926	Mn/Fe random distribution Replacing one
$Al_6(Fe_{0.6875}Mn_{0.3125})$	$a^{o} = 7.46$, This work (calc.) $b^{o} = 6.46$, c = 8.79	-919	Al by Si costs over 0.28 eV, indicating
Al ₆ (Fe _{0.6667} Mn _{0.3333})	-	-918	unlikeness at
$Al_6(Fe_{0.50}Mn_{0.50})$	a = 7.49 [26] (calc.) b = 6.47 c = 8.78	-914	ambient conditions.
α -Al _{4.75} (Fe _{2/3} Mn _{1/3})	$\overline{a} = 12.64$	-877	Mn at Fe 1 sites
$\begin{array}{c} \alpha\text{-}(Al_{0.94}Si_{0.06})_{4.75}(Fe_{2/} \\ {}_{3}Mn_{1/3}) \end{array}$	\overline{a} = 12.60 This work (calc.) a = 13.03 this work(exp.) a = 12.56 [37] (exp.)	-939	Mn at Fe 1 sites Si prefers at Al7, Al4 sites

utilized in this study to investigate the stability of the θ -Al₁₃Fe₄ phase. Experimental results have demonstrated the incorporation of Si and Mn into the θ -Al₁₃Fe₄ structure. This section will explore the compositional variations (Si and Mn) in the θ phase and the corresponding stability changes, as well as the phase transitions associated with these variations.

The formation energy of θ -Al₁₃(Fe_{0.90}Mn_{0.10})₄ corresponding to the experimental composition, is approximately -0.920 meV/M [26]. This suggests that at the formation temperature (1000 K), Mn can replace Fe atoms, forming ternary θ -Al₁₃(Fe_{1-x}Mn_x)₄ phase due to the kinetical factors [26]. Under Mn-poor conditions, θ -phase is more stable than the Al₆(Fe,Mn) [26]. However, when the Mn content in Al_y(Fe_{1-x}Mn_x) exceeds 9 at%, Al₆(Fe_{1-x}Mn_x) becomes more stable. This can be attributed to the effects of compositional segregation on phase selection. Therefore, the Al₆(Fe,Mn) phase is selected in Mn-rich regions, while the θ -Al₁₃Fe₄ phase is favored in Mn-poor regions.

Additionally, the effect of Si incorporation on the stability variation of θ -Al₁₃Fe₄ on was also investigated [21]. Si substitution at the Wyckoff 4i sites (Al9) enhances the stability of θ -Al₁₃Fe₄. The formation energy of Si-doped θ -Al₁₃(Fe_{0.90}Mn_{0.10})₄ structure is approximately –925 meV/M. This value is lower than that of Al₆(Fe_{2/3}Mn_{1/3}) (-0.918 eV/M), but higher than that of α -(Al_{0.94}Si_{0.06})_{4.75}(Fe_{2/3}Mn_{1/3}) (-939meV/M). In summary, the first-principles calculations established the following stability order (from low to high): α -Al_{4.75}(Fe_{2/3}Mn_{1/3}) < θ -(Al_{0.97}Si_{0.03})₁₃(Fe_{0.90}Mn_{0.10})₄ < α -(Al_{0.94}Si 0.06)_{4.75}(Fe_{2/3}Mn_{1/3}). Si doping stabilizes both the θ - and α -phases. This stability relation aids in understanding the experimental observations.

4. Discussion

4.1. Phase competition among θ -Al₁₃Fe₄, Al₆(Fe,Mn), and α -Al₁₅(Fe, Mn)₃Si₂

The solidification behaviour of the Al-5Mg-2Si-0.6Mn-1.3Fe alloy reveals a complex competition among Fe-IMCs, influenced by intrinsic and external factors. The phase diagram (Fig. 1) predicted that α -Al₁₅(Fe,Mn)₃Si₂ is the equilibrium primary phase due to its lowest formation energy among the Fe-IMCs. The calculated sequence involves solidification stages starting with primary α -Al₁₅(Fe,Mn)₃Si₂ followed by eutectic transformations producing α -Al₁₅(Fe,Mn)₃Si₂ and α -Al, and ending with ternary eutectic transitions that include α -Al₁₅(Fe,Mn)₃Si₂, α -Al, and Mg₂Si.

 $L \rightarrow \alpha \text{-Al}_{15}(\text{Fe},\text{Mn})_3\text{Si}_2 \qquad (\text{P-IMC}).....$

and

 $L \rightarrow \alpha - Al_{15} (Fe_{5}Mn)_{3} Si_{2} \quad (TE-IMC) \quad + \alpha Al \quad + Mg_{2}Si_{2}Si_{2} Si_{2}Si_{2} Si_{2}Si_{2} Si_{2}Si_{2$

However, experiments demonstrate the prior formation of nonequilibrium phases, θ -Al₁₃Fe₄ and Al₆(Fe,Mn), which undergo transformations into equilibrium α -Al₁₅(Fe,Mn)₃Si₂. This deviation highlights the significant role of various intrinsic and external influences.

Compositional differences among the Fe-IMCs which relative to the energetic stability play a critical role in the phase formation and phase transition competition. Experimental results (Fig. 10) reveal that θ -Al₁₃Fe₄ contains moderate levels of Mn (~2.6 at%) and Si (~2.6 at%), while Al₆(Fe,Mn) is Si-free with slightly higher Mn content (~4 at%). Conversely, α -Al₁₅(Fe,Mn)₃Si₂ incorporates high levels of Si (~5.7 at%) and Mn (~4.6 at%). First-principles calculations show that Mn substitution for Fe and Si replacement of Al are energetically favourable for both θ -Al₁₃Fe₄ and α -Al₁₅(Fe,Mn)₃Si₂, enhancing their stability. The transformation mechanism from the Si-free Al₆(Fe,Mn) to Si-rich phases such as α -Al₁₅(Fe,Mn)₃Si₂ remains poorly understood. While Al₆(Fe,Mn) is characterized by the absence of silicon within its crystal structure, the transition to Si-containing phases suggests a significant compositional and structural reorganization. The precise mechanisms driving the Si uptake and the atomic-scale dynamics of this transformation have yet to be fully elucidated, leaving a critical gap in understanding the evolution of Si-free to Si-rich phases in Fe-IMC systems.

The relationship between composition and crystal structure plays a critical role in determining phase formation and phase transformations of Fe-IMCs in aluminium alloys. The incorporation of alloying elements such as Si and Mn into each Fe-IMC affects their energetic preference for specific atomic sites, which in turn alters the lattice parameters along particular crystallographic axes [21,27]. This preferential substitution modifies the internal strain and symmetry within the crystal structure. As the lattice parameter variations approach critical thresholds, referred to as transition points, the crystal undergoes a structural transformation into a different type of Fe-IMC. 0-Al13Fe4 has a monoclinic crystal structure (C 1 2/m 1 (12)) with lattice parameters of a = 15.492 Å, b= 8.078 Å, and c= 12.47 Å [39]. Al₆(Fe,Mn) features an orthorhombic structure (Cmcm (63)), with *a*= 7.498 Å, *b*= 6.495 Å, and *c*= 8.837 Å [40]. In contrast, α -Al₁₅(Fe,Mn)₃Si₂ has a body-centred cubic or simple cubic structure with a lattice parameter of a = 12.56 Å [37,38]. The phase transition between them is anticipated to be straightforward due to the similarity between the lattice parameters of θ and α phases. Specifically, the *c*-axis length of θ closely matches the *a*-axis length of α , while 1.5 times the *b*-axis length of θ aligns with the α lattice constant. Conversely, the transition from $Al_6(Fe,Mn)$ to θ appears easier than Al₆(Fe,Mn) to α due to their crystallographic compatibility. For instance, Si incorporation into θ -Al₁₃Fe₄ replaces certain Al atoms, resulting in noticeable changes in the c-axis parameter, while Mn substitution similarly impacts the Fe lattice sites. Such compositional effects serve as key drivers for phase transitions between θ-Al₁₃Fe₄, Al₆(Fe,Mn), and α-Al₁₅(Fe,Mn)₃Si₂, emphasizing the intricate relationship between alloying, lattice parameters, and crystal structure evolution. Further symmetry work are required to understand the complex relationship in variation between composition, lattice parameters and crystal structures.

The variation of the phase selection due to the phase competition at the SS1, resulted in the compositional variation within α -Al₁₅(Fe, Mn)₃Si₂, as illustrated in Tables 1–2 and Fig. 11. During SS1, the equilibrium primary phase in the Al-5Mg-2Si-0.6Mn-1.3Fe alloy is predicted to incorporate the highest Mn and Si concentrations due to the abundance of these elements in the liquid melt. However, the observed Mn concentration (4.6 at%) and Si concentration (5.7 at%) in α α -Al₁₅(Fe, Mn)₃Si₂ were lower than the Mn (5.7 at%) and Si (6.3 at%) levels present in the binary eutectic. This discrepancy arises due to the formation of non-equilibrium phases, θ -Al₁₃Fe₄ and Al₆(Fe,Mn), which contain



Fig. 11. Variation in Mn and Si concentrations across three types of Fe-IMCs, showing the compositional changes during solidification stages and phase transformation. Note: PT1 represents the phase transformation type 1, where θ -Al₁₃Fe₄ transforms to α -Al₁₅(Fe, Mn)₃Si₂, resulting in increased Si and Mn concentrations; PT2 represents the phase transformation type 2, where θ -Al₆(Fe,Mn) to α -Al₁₅(Fe, Mn)₃Si₂, leading to a significant increase in Si and a slight rise of Mn concentration; SS2 refers to the second solidification stage (binary eutectic stage); and SS3 corresponds to the third solidification stage (ternary eutectic stage). The first solidification stage involves the formation of the primary Fe-IMCs.

significantly lower Mn and Si concentrations, thus depleting these elements before α -Al₁₅(Fe,Mn)₃Si₂ solidification. Additionally, the reduced solubility of Mn and Si in aluminium at lower temperatures, especially at the binary eutectic, leads to the rejection of excess Mn and Si to the grain boundaries, resulting in localized enrichment in α -Al₁₅(Fe,Mn)₃Si₂. Subsequently, during SS2 and SS3, as alloying elements are consumed, the α -Al₁₅(Fe,Mn)₃Si₂ in the ternary eutectic solidifies with further diminished Mn and Si content.

The heterogeneous nucleation difficulty is one of the most important reasons that contributes to the phase selection of non-equilibrium Fe-IMCs. Without considering the incorporation of impurities or alloying elements, the basic constituting alloying elements of θ -Al₁₃Fe₄, Al₆(Fe, Mn), and α -Al₁₅(Fe,Mn)₃Si₂ are Al and Fe, Al, Fe, and Mn, and Al, Fe, Mn, and Si, respectively. Heterogeneous nucleation of these Fe-IMCs requires different atomic species to occupy specific atomic positions, meaning that the more constituent elements involved, the more difficult the heterogeneous nucleation process becomes [12,14]. The experiments revealed a wide variety of Fe-IMC formations, which depend on casting conditions, particularly undercooling and cooling rates. It has been reported that the undercooling sequence for the heterogeneous nucleation of Fe-IMCs is: α -Al₁₅(Fe,Mn)₃Si₂ > Al₆(Fe,Mn)> θ -Al₁₃Fe₄. Nucleation of α -Al₁₅(Fe,Mn)₃Si₂ requires a relatively large undercooling, up to tens of Kelvin, while θ -Al₁₃Fe₄ nucleates at undercoolings of less than 10 Kelvin [14]. The casting process, which typically involves high cooling rates (3.5 K/s in this study), is non-equilibrium, leading to complicated phase selection for Fe-IMCs. During the solidification process, the melt continues to cool before reaching the nucleation temperature of the equilibrium α -Al₁₅(Fe,Mn)₃Si₂. As a result, other Fe-IMCs, such as Al₆(Fe,Mn) and 0-Al₁₃Fe₄, which require smaller nucleation undercoolings, have a higher likelihood of nucleating and growing. Theoretically, θ -Al₁₃Fe₄ has a much higher chance of nucleating and remaining in the studied alloy as a non-equilibrium phase due to its significantly lower nucleation undercooling requirements.

The thermodynamic stability of these three different types of Fe-IMCs varies with changes in composition, particularly the concentration and incorporation of Mn and Si. The first-principles calculations in 3.4 demonstrated that the formation of Al_6 (Fe,Mn) is favoured in the Mn-rich area, while the formation of θ -Al₁₃Fe₄ is preferred in the Mnpoor area. Si incorporation into these Fe-IMCs also plays a critical role in phase transitions. The segregation of Si on the surface of the Si-free Al₆(Fe,Mn) phase promotes phase transitions towards the Si-favorable phases, θ -Al₁₃Fe₄ and α -Al₁₅(Fe,Mn)₃Si₂.

Cooling rates also determine the spatial distribution of Fe-IMCs. θ -Al₁₃Fe₄ primarily forms at the slower-cooled sample centre, while Al₆(Fe,Mn) nucleates at faster-cooled edges. Experimental results showed that θ -Al₁₃Fe₄, which requires smaller nucleation undercooling, primarily forms at the centre of the sample where the cooling rate is lower. In contrast, Al₆(Fe,Mn), which requires a larger nucleation undercooling, predominantly forms at the edges of the sample where the cooling rate is higher. This observation indicates that higher cooling rates enhance the heterogeneous nucleation of Fe-IMCs requiring larger nucleation undercoolings. It is reported that [13], although under a very slow cooling rate, 0.01 K/s, the phase competition still existed. The non-equilibrium phase (mainly θ) was selected firstly and then transformed into equilibrium α .

Theoretically, θ -Al₁₃Fe₄ has a higher likelihood of nucleating and persisting in Al-alloys as a non-equilibrium phase due to its significantly lower nucleation undercooling requirements. This behaviour has been supported by several studies [13,23,24]. However, experimental results (Fig. 2) demonstrated that the majority of Al₆(Fe,Mn) solidified at the edges of the sample, where cooling rates were higher. First-principles calculations further revealed that increased Mn concentrations stabilize Al₆(Fe,Mn), while Si stabilizes α -Al₁₅(Fe,Mn)₃Si₂. Thus, it can be inferred that the combined effects of higher Mn content, lower Si content, and higher cooling rates (at the sample edge) contributed to the formation of Al₆(Fe,Mn) in this study.

The presence of the selected non-equilibrium Fe-IMCs: Al₆(Fe,Mn) and θ -Al₁₃Fe₄, becomes unstable as the temperature continues to decrease in the following solidification stages in the studied alloy. Consequently, further phase transformations occur. The mechanism of the phase transition between θ -Al₁₃Fe₄ and α -Al₁₅(Fe,Mn)₃Si₂ has been thoroughly explained in previous work [13]. In this study, we focus on new observations of phase transformations between Al₆(Fe,Mn)/ θ and Al₆(Fe,Mn)/ α , which will be discussed here.

4.2. Mechanism of phase transition from $Al_6(Fe,Mn)$ (Si-free) to α - $Al_{15}(Fe,Mn)_3Si_2$ (high Si)

The phase transformation between $Al_6(Fe,Mn)$ and α - $Al_{15}(Fe,Mn)$ Mn)₃Si₂ is a diffusive process driven by changes in composition. This transformation aligns with most reported phase transitions among different Fe-IMCs, which are typically influenced by the diffusion of Si [23,24]. During the growth of primary Al₆(Fe,Mn), alloying elements in the liquid are rejected to the surface of the Al₆(Fe,Mn). Certain elements such as Si and Mg, which are not the constitute components, may accumulate at the surface of the Al₆(Fe,Mn). It has been reported that Mg segregation occurs at the surface of eutectic Al₆(Fe,Mn) in Al-1.4Fe-0.7Mn-*x*Mg (*x* varied from 0.5 to 3.0 wt%) alloys [35]. Si, as an alloying element that cannot incorporate into Al₆(Fe,Mn), may also segregate at its surface. Experimental results have shown that Al₆(Fe, Mn) is unfavourable for both Mg and Si incorporation. However, there is a distinct difference between the segregation behaviours of Si and Mg, driven by their interactions with the Al₆(Fe,Mn) crystal. Si exhibits strong interactions with Fe and Mn, whereas Mg shows weak interactions with all atoms in Al₆(Fe,Mn). These interactions can be quantified by the heat of mixing values, which highlight the strength of bonding between different elements. The sequence of heat of mixing values for Si-Fe, Si-Mn, Si-Al, Mg-Fe, Mg-Mn, and Mg-Al is as follows: Si-Mn ($\Delta H_{Si-Mn}^{mix} = -45 \text{ kJ/mol}$) > Si-Fe ($\Delta H_{Si-Fe}^{mix} = -35 \text{ kJ/mol}$) > Si-Al $(\Delta H_{SI-Al}^{mix} = -19 \text{ kJ/mol}) > \text{Mg-Al} (\Delta H_{Mg-Al}^{mix} = -2 \text{ kJ/mol}) > \text{Mg-Mn}$ ($\Delta H_{Mg-Mn}^{mix} = 10 \text{ kJ/mol}$) > Mg-Fe ($\Delta H_{Mg-Fe}^{mix} = 18 \text{ kJ/mol}$) [41]. This explains why the diffusion driving force for Si into Al₆(Fe,Mn) is greater than that for Mg. Another reason for the absence of observed Mg segregation on primary Al₆(Fe,Mn) in this study could be the higher formation temperature of primary Al₆(Fe,Mn) compared to the reported binary eutectic Al_6 (Fe,Mn) [35]. At higher temperatures, the solubility of Mg in liquid aluminium is increased, reducing the likelihood of Mg segregation during the solidification process.

The mechanism of this type of phase transformation is illustrated in Fig. 12. Following the formation of hollowed primary $Al_6(Fe,Mn)$, Si becomes enriched at the surface of the $Al_6(Fe,Mn)$. As the temperature decreases, $Al_6(Fe,Mn)$ becomes thermodynamically unstable. This instability drives the diffusion of Si from surface segregation into the $Al_6(Fe,Mn)$, a process that becomes energic favourable. This diffusion triggers structural changes, where the incorporation of Si and the redistribution of Fe and Mn lead to Al atoms being rejected from the core into surrounding regions enriched with Si (Fig. 12b).

Consequently, the transformation of Al₆(Fe,Mn) to α -Al₁₅(Fe,Mn)₃Si₂ is accompanied by the formation of an α -Al phase. This results in a lamellar morphology between α -Al₁₅(Fe,Mn)₃Si₂ and α -Al. Simultaneously, small amounts of Fe, Mn, and even Si remain in the transformed α -Al, contributing to the subsequent formation of needle-like precipitates, as shown in Fig. 9c. Al₆(Fe,Mn) is a phase with zero tolerance for Si. The composition difference in Si concentration between Al₆(Fe, Mn) and α -Al₁₅(Fe,Mn)₃Si₂ is significant, reaching 5.7 at% (Table 1). This indicates that a high Si concentration is required for Si to incorporate into Al₆(Fe,Mn) before the formation of the new α -Al₁₅(Fe, Mn)₃Si₂ phase. Consequently, the phase transformation process between



Fig. 12. Schematic diagram illustrating the phase transition mechanism of: Liquid + Al₆(Fe,Mn) $\rightarrow \alpha$ -Al₁₅(Fe,Mn)₃Si₂ + α -Al. (a) TheHollowed structure of Al₆(Fe,Mn), (b) Si enrichment at the surface of Al₆(Fe,Mn), and (c) phase transformation from Al₆(Fe,Mn) to α -Al₁₅(Fe,Mn)₃Si₂, with the simultaneous precipitation of α -Al to compensate for the compositional difference.

 $Al_6(Fe,Mn)$ and $\alpha\text{-}Al_{15}(Fe,Mn)_3Si_2$ is considered to be much slower than transformations involving phases with smaller compositional differences, such as Al_{13}/Al_{15} .

Phase transformations between Al₆(Fe,Mn) and α-Al₁₅(Fe,Mn)₃Si₂ observed in this study occurred without a specific orientation relationship, which can be attributed to several factors related to the nature of the phases and the transformation mechanisms. First, both Al₆(Fe,Mn) and α -Al₁₅(Fe,Mn)₃Si₂ have complex crystal structures. Transformations between phases with distinct and intricate structures often result in atomic arrangements that do not align in a manner that maintains a specific orientation relationship. Second, the transformation between Al₆(Fe,Mn) and α -Al₁₅(Fe,Mn)₃Si₂ is primarily driven by changes in thermodynamic stability rather than crystallographic constraints. In such cases, the emerging phase adopts a configuration that achieves stability, often without retaining any orientation relationship with the parent phase. Third, the lattice parameters of Al₆(Fe,Mn) and α -Al₁₅(Fe, Mn)₃Si₂ are significantly different. Maintaining a specific orientation under such conditions may be energetically unfavourable, further encouraging the formation of randomly oriented α -Al₁₅(Fe,Mn)₃Si₂.

4.3. Mechanism of phase competition and transition between $Al_6(Fe,Mn)$ and θ - $Al_{13}Fe_4$

It is well established that the Fe-IMCs exhibit excellent solubility for multiple alloying elements, typically Si and various 3*d* transition metals such as Mn, Cr, and others. The composition of the Fe-IMCs examined in this study (Table 1) indicate that θ -Al₁₃Fe₄ incorporates both Si and Mn. However, only limited amounts of Si and Mn can be doped into θ -Al₁₃Fe₄ without altering its crystal structure.

The experimental results demonstrated that both Al₆(Fe,Mn) and θ -Al₁₃Fe₄ are selected as primary phases in different regions of the sample during solidification process. The first-principles calculations conducted in this study provided crucial insights into the energetics and the role of Si stabilization in the formation of Fe-IMCs. The results indicate that the Al₆(Fe,Mn) phase preferentially forms in Mn-rich areas, whereas θ -Al₁₃Fe₄ phase is more likely to form in Mn-poor areas. The presence of Si enhances the formation capability of the θ -Al₁₃Fe₄ phase. Previous first-principles calculations on the Mn/Fe alloying effects on the relative stability of Al₆(Fe,Mn) and θ -Al₁₃Fe₄ revealed that the θ -phase is more stable at low Mn content (x < 0.08). In contrast, the Al₆(Fe,Mn) phase becomes more stable as Mn content increases (x > 0.08). This finding correlates with the observed formation of these two primary phases in regions with different Mn concentrations.

In this study, Al₆(Fe,Mn) undergoes phase transformations into both θ -Al₁₃Fe₄ and α -Al₁₅(Fe,Mn)₃Si₂. The transformation from Al₆(Fe,Mn) to α -Al₁₅(Fe,Mn)₃Si₂ requires significantly higher Si concentrations and a slight increase in Fe and Mn, compared to the transformation into θ -Al₁₃Fe₄. However, the diffusion of Si plays a more critical role in phase transformations among Fe-IMCs [23,24]. As a result, although α -Al₁₅(Fe, Mn)₃Si₂ is the equilibrium phase in the studied alloy, regions with lower Si concentrations are more likely to favour the transformation from Al₆(Fe,Mn) to θ -Al₁₃Fe₄, as this requires less Si diffusion.

5. Summary

This study presents a novel perspective on the competitive interactions and phase transformations among multiple Fe-bearing intermetallic compounds (Fe-IMCs): θ -Al₁₃Fe₄, Al₆(Fe,Mn) and α -Al₁₅(Fe, Mn)₃Si₂ in an Al-5Mg-2Si-0.6Mn-1.3Fe alloy cast at 700°C with a cooling rate of 3.5 K/s. It provides the first comprehensive observation of phase competition during both the liquid and solidification stages, emphasizing the influence of composition, nucleation dynamics, and cooling rates.

Key findings from this research include:

- 1. Nucleation Competition: The study reveals that heterogeneous nucleation competition occurs at temperatures higher than α -Al so-lidification. Non-equilibrium phases, such as θ -Al₁₃Fe₄ and Al₆(Fe, Mn), nucleate preferentially due to their lower nucleation barriers compared to the equilibrium α -Al₁₅(Fe,Mn)₃Si₂ phase.
- Spatial Distribution of Phases: θ-Al₁₃Fe₄ forms in regions with slower cooling (e.g., the central part of the sample), while Al₆(Fe,Mn) is more prevalent in faster-cooled regions (e.g., the sample edges).
- 3. Phase Transformation Pathways: Three distinct phase transformation mechanisms were identified during solidification:
- Liquid $+ \theta$ -Al₁₃Fe₄ $\rightarrow \alpha$ -Al₁₅(Fe,Mn)₃Si₂ $+ \alpha$ -Al (irregular morphology): Fe diffusion out and Si diffusion in.
- Liquid (Fe, Si) + Al₆(Fe,Mn) \rightarrow θ -Al₁₃Fe₄: Fe and Si diffusion in with slight Mn diffusion out.
- Liquid $+ Al_6(Fe,Mn) \rightarrow \alpha Al_{15}(Fe,Mn)_3Si_2 + \alpha Al$ (lamellar structure): Driven by Si diffusion in.
- 4. Lamellar-Structure Formation: The transformation from Al₆(Fe,Mn) to α -Al₁₅(Fe,Mn)₃Si₂ follows well-understood mechanisms, forming a distinctive lamellar structure. Notably, no clear orientation relationship was observed between Al₆(Fe,Mn) and α -Al₁₅(Fe,Mn)₃Si₂ in contrast to the θ -Al₁₃Fe₄ to α -Al₁₅(Fe,Mn)₃Si₂ transformation.
- 5. Impact of Compositional Variations: Si and Mn concentrations significantly influence phase formation, with higher Si α -Al₁₅(Fe, Mn)₃Si₂ and higher Mn favouring Al₆(Fe,Mn).

CRediT authorship contribution statement

Zhongyun Fan: Supervision, Funding acquisition. **Changming Fang:** Writing – review & editing, Investigation. **Zhongping Que:** Writing – review & editing, Writing – original draft, Visualization, Validation, Supervision, Software, Resources, Project administration, Methodology, Investigation, Funding acquisition, Formal analysis, Conceptualization.

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Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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