A Novel Pairwise Domain-Adaptation-Assisted Dual-Task Learning Approach to Co-Prediction of Robotic Machining Efficiency and Quality in New Parameter Spaces

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Abstract-Accurate prediction of material removal depth and averaged surface roughness is crucial for evaluating the performance of robotic belt grinding (RBG). Nevertheless, the machining parameters of RBG across different spaces exhibit various data distributions, which often results in prediction shifts on unseen machining parameters when using conventional approaches. In this article, we introduce a pairwise domain adaptation-assisted dual-task learning (PW-DA-DTL) method for co-predicting material removal depth and averaged surface roughness with regard to new RBG machining parameter spaces. The multi-gate mixture-of-experts method is employed as the foundational framework for dual-task learning, effectively capturing and modeling the relationships between material removal depth and average surface roughness by leveraging their inherent task interdependencies. The pairwise domain adaptation strategy is put forward to simultaneously enhance sample diversity and mitigate cross-domain data distribution discrepancy between the existing and new RBG machining parameter spaces. Comparative experiments are presented to demonstrate the effectiveness and superiority of the proposed PW-DA-DTL method.

Index Terms—Material removal depth, averaged surface roughness, domain adaptation, dual-task learning, robotic belt grinding.

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I. INTRODUCTION

Robotic Belt Grinding (RBG) has been recognized as an effective technique for finishing machining and difficult-tomachine materials, owing to its high flexibility, extensive operating space and cost-effectiveness [1], [2]. Efficient and precise manufacturing is an enduring objective of RBG, which could be achieved by enhancing material removal ability and workpiece surface quality simultaneously [3], [4]. Material removal depth (MRD) and averaged surface roughness (denoted as R_a), representing material removal capability and surface quality respectively, are widely recognized as key indicators for understanding and evaluating the performance of RBG. As a critical element in the closed-loop manufacturing process, accurate prediction of MRD and R_a is vital for machining parameter optimization and quality control, ultimately enabling an efficient and precise RBG manufacturing process [5]–[9].

Over the last few decades, numerous machine learning methods have been developed to individually predict MRD and R_a [1], [4], [10]. Nevertheless, these methods commonly require training separate models, neglecting the potential correlation between MRD and R_a . Serving as a promising technique, multi-task supervised learning (such as the shared-bottom method, the tensor factorization method and the multi-gate mixture-of-experts (MMoE) method) is designed to enhance the learning ability on multiple learning tasks by exploiting knowledge across tasks. Among these multi-task supervised learning methods, MMoE stands out for its capability to balance the correlation and discrepancy across tasks with a few training parameters [11], [12], making it feasible for dual-task prediction of MRD and R_a .

On the other hand, conventional multi-task supervised learning methods usually adhere to the typical assumption that the training and testing data follow an independent and identically distributed (i.i.d.) pattern [5], [13]. In fact, the machining parameters across different spaces often exhibit diverse data distributions, leading to prediction shifts on unseen machining parameters when applying conventional multi-task supervised learning methods to new machining parameter spaces [14]. In this situation, there is a clear need to develop advanced multi-task supervised learning methods capable of addressing the challenges posed by inconsistent data distributions across different RBG machining parameter spaces.

Serving as a cutting-edge technique, transfer learning al-

lows for the relaxation of constraint that the training and testing data must be i.i.d. when applying conventional multitask supervised learning methods [15]–[18]. Among numerous transfer learning methods, deep transfer learning has received much attention from both academia and industry owing to its exceptional feature extraction ability and remarkable effectiveness [19]. Notably, two dominant paradigms in deep transfer learning are fine-tuning-based methods and deep domain adaptation-based (DDA) methods, with the latter being widely recognized for its proficiency in quantifying cross-domain distribution discrepancies [20]–[22]. A seemingly reasonable idea is to exploit DDA methods to alleviate data distribution discrepancy between existing and new RBG machining parameter spaces, thereby facilitating accurate co-prediction of MRD and R_a for new machining parameters.

In general, the predictive performance of DDA methods depends heavily on the availability of sufficient samples in both the source and target domains [23], [24]. Nevertheless, collecting and annotating RBG data in the new machining parameter space is prohibitively expensive [25], resulting in only a limited number of labeled samples available for DDA model training. The lack of target domain samples may lead to ineffective training and insufficient alignment of data distributions between the training and testing data when using DDA methods [26]–[28]. Therefore, it becomes essential to develop a novel domain adaptation strategy capable of eliminating distribution discrepancy between training and testing data, even when only few testing samples are available.

Based on the above discussions, the aim of this article is to accurately predict MRD and Ra in the new machining parameter space of RBG. Due to the lack of labeled target domain samples, conventional DDA methods face significant challenges in handling the data imbalance problem, which leads to insufficient alignment of data distributions between the source and target domains. To tackle this issue, a pairwise domain adaptation-assisted dual-task learning (PW-DA-DTL) method is put forward in this article, where a novel pairwise DA strategy is developed for co-predicting material removal depth and averaged surface roughness with regard to new machining parameters of RBG. Specifically, the MMoE method, a representative DTL technique, is employed to improve the prediction performance by balancing the intrinsic correlation and discrepancy between MRD and Ra. Additionally, a pairwise DA strategy is designed to simultaneously augment target domain samples and align data distributions across the two domains. The proposed PW-DA-DTL method offers a feasible solution for accurately evaluating various RBG machining parameters, enabling reliable selection and optimization of machining parameters in the RBG manufacturing process.

The main contributions of this article can be summarized in the following four aspects.

- 1) A novel PW-DA-DTL method is proposed for accurately co-predicting MRD and R_a in new RBG machining parameter spaces.
- 2) A pairwise DA strategy is put forward to enhance the data distribution alignment within the source and target domains under data imbalance.
- 3) The MMoE method is employed to effectively balance the intrinsic correlation and discrepancy between the

MRD and R_a prediction tasks.

4) The proposed PW-DA-DTL method is successfully validated on an RBG platform for co-predicting MRD and R_a. Comparative experiments demonstrate the effectiveness and advantages of the proposed PW-DA-DTL method over five benchmark methods."

The remaining sections of this article are organized as follows. The background of multi-task learning, domain adaptation and problem description are presented in Section II. In Section III, the proposed PW-DA-DTL method and its overall loss function is introduced. Additionally, the proposed method for co-predicting MRD and R_a of RBG, as well as three evaluation metrics are provided. The self-developed experimental platform and the experimental settings are described in Section IV. Experimental results and analysis of the MRD and R_a co-prediction are provided and discussed in Section V. Finally, the conclusions are drawn, and the possible future topics are addressed in Section VI.

II. PRELIMINARY

A. Background of Multi-Task Learning

Multi-task learning (MTL) aims to improve the overall learning ability by leveraging the shared knowledge and relationships among tasks. Given l learning tasks $\{\mathcal{T}^i\}_{i=1}^l$, in which all the learning tasks or a subset of them are related but not identical, MTL is dedicated to enhancing the learning of a model for \mathcal{T}^i by leveraging the knowledge across the l tasks.

A common form of MTL is multi-task supervised learning (MTSL), where each task involving learning the mapping function from the feature space to the label space [29]. In MTSL, each task \mathcal{T}^i contains n_i labeled samples $\{(x_j^i, y_j^i)\}_{j=1}^{n_i}$, where x_j^i lies in a *d*-dimensional feature space \mathcal{X} and y_j^i is the corresponding label in a label space \mathcal{Y} . To goal of MSTL is to simultaneously train l functions $\{f^i(X)\}_{i=1}^l$ for the l learning tasks leveraging the labeled samples across tasks.

In certain scenarios, multi-task supervised learning (MTSL) employs feature transformation techniques to enhance learning performance, collectively known as feature transformation-based multi-task supervised learning (FT-MTSL). In FT-MTSL, different tasks share identical or similar feature representations, which are derived from linear or nonlinear transformation function $h(\cdot)$, the original feature representations for each learning task are transformed as $\{h(x_j^i)\}_{j=1}^{n_i}$. Then, the transformed feature representations are fed into MTSL for the simultaneous training of l functions $\{f^i(h(X))\}_{i=1}^{l}$ with respect to the l learning tasks.

B. Background of Domain Adaptation

Domain adaptation (DA) is a transfer learning technique that enhances model performance in a target domain (with limited or no labeled samples) by leveraging knowledge from a related but different source domain (with abundant labeled samples) [19], [30]. In the context of transfer learning, a domain \mathcal{D} is composed of a *d*-dimensional feature space \mathcal{X} and a marginal probability distribution P(X), denoted as $\mathcal{D} = \{\mathcal{X}, P(X)\}$,

with $X \in \mathcal{X}$. For a given source domain $\mathcal{D}^s = \{\mathcal{X}^s, P(X^s)\}$ and a target domain $\mathcal{D}^t = \{\mathcal{X}^t, P(X^t)\}$, the two domains are different if they have different feature spaces or marginal distributions (i.e., $\mathcal{X}^s \neq \mathcal{X}^t \lor P(X^s) \neq P(X^t)$).

In the context of the domain \mathcal{D} , the task \mathcal{T} is defined by a label space \mathcal{Y} and a prediction function f(X), represented as $\mathcal{T} = \{\mathcal{Y}, f(X)\}$. Specifically, the prediction function is denoted as $f(X) : X \to Y$, where $Y \in \mathcal{Y}$. Inspired by [19], [30], f(X) can be chosen as the conditional probability distribution P(Y|X). For a given source task $\mathcal{T}^s = \{\mathcal{Y}^s, f(X^s)\}$ and a target task $\mathcal{T}^t = \{\mathcal{Y}^t, f(X^t)\}$, two tasks are different if they have different label spaces or conditional distributions (i.e., $\mathcal{Y}^s \neq \mathcal{Y}^t \lor P(Y^s|X^s) \neq P(Y^t|X^t)$).

Given *n* labeled samples $\{(x_i^s, y_i^s)\}_{i=1}^n$ from the source domain \mathcal{D}^s , *m* labeled samples $\{(x_j^t, y_j^t)\}_{j=1}^m$ and *p* unlabeled samples $\{x_j^t\}_{j=m+1}^{m+p}$ from the target domain \mathcal{D}^t , the objective of DA is to learn a target prediction function $f(x_j^t) : x_j^t \to y_j^t$, $(j = m + 1, \cdots, m + p)$, aimed at handling the unlabeled target domain samples with low predicted error, under the assumptions that the feature spaces and label spaces are identical (i.e., $\mathcal{X}^s = \mathcal{X}^t \land \mathcal{Y}^s = \mathcal{Y}^t$), while the marginal and conditional distributions are different (i.e., $P(X^s) \neq P(X^t) \land P(Y^s | X^s) \neq P(Y^t | X^t))$.

C. Problem Description

1) FT-MTSL for MRD and R_a Co-Prediction in RBG: In the RBG manufacturing process, MRD and R_a are closely related to the machining parameters (such as normal force, robotic feed speed, belt linear speed and equivalent radius of abrasive grains). During the training process of FT-MTSL, xrepresents the machining parameters and y consists of MRD and R_a . $h(\cdot)$ is a nonlinear function that maps the raw data x into a shared feature space. The objective of FT-MTSL for MRD and R_a co-prediction is to learn a prediction on the unlabeled samples leveraging the knowledge across two tasks.

2) DA-Assisted FT-MTSL for MRD and R_a Co-Prediction in RBG: Due to the discrepancy among various machining parameter spaces, the data distributions are different between the source dataset (i.e., samples with existing machining parameters) and the target dataset (i.e., samples with new machining parameters). Given the source dataset (which contains n labeled samples) and the target dataset (which has m labeled samples and p unlabeled samples), the objective of the DAassisted FT-MTSL method for MRD and R_a co-prediction is to learn a target prediction on the unlabeled target domain samples with low expected error.

III. METHODS

In this section, the MMoE method, the developed DA strategy and the proposed DA-based dual-task learning method are introduced in detail. Furthermore, three evaluation metrics on MRD and R_a prediction of RBG are presented.

A. MMoE

The MMoE is designed to explicitly model relationship and difference among tasks. The output of the k_{th} $(k = 1, \dots, l)$

task in the MMoE method is calculated as follows:

$$y^{k} = h_{t}^{k} \left(\sum_{i=1}^{s} g_{i}^{k}(x) f_{i}(x) \right),$$
 (1)

where x represents the input data or its transformed features, s is the number of expert networks, and $f_i(\cdot)$ denotes the mapping function of the i_{th} expert network. $g^k(x) =$ softmax $(W_g^k x)$ is the output of the k_{th} gating network, where $W_g^k \in \mathbb{R}^{s \times d}$ is the weight matrix and d represents the dimension of x. $h_t^k(\cdot)$ denotes the mapping function of the k_{th} tower network, and y^k corresponds to the output of the tower network. The schematic structure of MMoE method is illustrated in Fig. 1.

Remark 1: Compared to the conventional shared-bottom method [31], MMoE is able to model the relationships of tasks in a weighted manner by determining how the separations resulting from different gating networks overlap. If the provided tasks are less related, sharing expert networks would be penalized, and the gating networks for these tasks would learn to select different expert networks instead [11].



Fig. 1. The schematic structure of MMoE method. Dual-task learning is taken as a representative case.

B. The Developed DA Strategy

1) Maximum Mean Discrepancy: This article utilizes the empirical maximum mean discrepancy (MMD) to characterize the distribution differences between the source and target domains [32], [33]. Leveraging the MMD, the distribution discrepancies between the source and target domains are computed by mapping the original data into a reproducing kernel Hilbert space (RKHS). In comparison to other distance functions, such as the Kullback–Leibler divergence, MMD serves as a non-parametric distance measurement among data distributions, circumventing the calculations of intermediate density [34]. The empirical MMD of marginal distribution between the source and target domains is defined as the following form:

$$D\left(X^{s}, X^{t}\right) = \left\|\frac{1}{n}\sum_{i=1}^{n}\phi\left(x_{i}^{s}\right) - \frac{1}{m}\sum_{j=1}^{m}\phi\left(x_{j}^{t}\right)\right\|_{\mathcal{H}}^{2}, \quad (2)$$

where $\phi(\cdot)$ represents a mapping from the original space into the RKHS, and $\|\cdot\|_{\mathcal{H}}^2$ denotes the squared norm of "·" in the RKHS.

According to the reproducing property of the RKHS, the kernel trick (i.e., $k(x_i, x_j) = \langle \phi(x_i), \phi(x_j) \rangle_{\mathcal{H}}$, where x_i and x_j represent two random samples; $\langle \cdot, \cdot \rangle_{\mathcal{H}}$ is the inner dot in the RKHS) is employed to unfold (2) as the following form:

$$D\left(X^{s}, X^{t}\right) = \frac{1}{n^{2}} \sum_{i=1}^{n} \sum_{i'=1}^{n} k\left(x_{i}^{s}, x_{i'}^{s}\right) + \frac{1}{m^{2}} \sum_{j=1}^{m} \sum_{j'=1}^{m} k\left(x_{j}^{t}, x_{j'}^{t}\right) - \frac{2}{mn} \sum_{i=1}^{n} \sum_{j=1}^{m} k\left(x_{i}^{s}, x_{j}^{t}\right)$$
(3)

In this article, the Gaussian kernel is adopted as the kernel function [32], which is defined as follows:

$$k(x_i, x_j) = \exp\left(-\|x_i - x_j\|^2 / (2\sigma^2)\right),$$
 (4)

where σ is a hyperparameter that represents the width of Gaussian kernel.

2) The Pairwise DA Strategy: In this article, considering that only a limited number of labeled target domain samples (even as few as one sample) are available, a pairwise DA strategy is developed to alleviate the insufficient alignment of data distributions between the source and target domains based on the MMD method. The pairwise DA strategy is designed to augment labeled target domain samples by pairing them with the source domain samples in a recurrent manner. Notably, given n labeled samples in the source domain and mlabeled samples in the target domain $(m \ll n), m \times n$ targetsource pairs are created through the recurrent pairing of target and source domain samples. Simultaneously, $n \times n$ sourcesource pairs are generated by recurrently pairing among source domain samples, with a random selection of $m \times n$ sourcesource pairs to align with the number of target-source pairs. In Fig. 2, two kinds of sample pairs (denoted as target-source pairs and source-source pairs) are simultaneously input into a feature transformation network (which is a designed artificial neural network), and the transformed features are merged for DA using the target-source data and the source-source data.

After the DA, the transformed features are fed into the MMoE (Section III-A) for the supervised dual-task learning. The supervised training manner can alleviate model bias caused by the imbalanced labels between the source and target domains, thereby enhancing the reliability of the proposed method. The structure of the proposed PW-DA-DTL method is shown in Fig. 2.

Remark 2: The pairwise strategy can be considered as a form of data augmentation method, where a limited number of target domain samples are expanded by recurrent grouping of target and source domain samples. In contrast to conventional data augmentation methods, such as generative adversarial network (GAN) [35], synthetic minority oversampling technique (SMOTE) [36] and adaptive synthetic (ADASYN) algorithm [37], the proposed pairwise strategy can increase the sample size using few samples, even as few as one sample. Compared to the sample replication method, the proposed pairwise strategy can significantly improve the diversity of augmented target domain samples by integrating the limited number of target domain samples with sufficient source domain samples. The pairwise strategy, combined with supervised learning [38],

[39], simultaneously alleviates model bias and improves the generalization capability of the proposed method.



Fig. 2. The pairwise DA strategy and the structure of PW-DA-DTL method. $m \times n$ target-source pairs and source-source pairs are generated for training the PW-DA-DTL method.

3) Domain Loss: The domain loss is the MMD between the merged features of target-source pairs and source-source pairs. The calculation of domain loss (which corresponds to (2)) is transformed as follows:

$$L_{d} = D\left(\left[h\left(X^{s}\right), h\left(X^{s}\right)\right], \left[h\left(X^{t}\right), h\left(X^{s}\right)\right]\right)$$

$$= \left\|\frac{1}{n^{2}} \sum_{i=1}^{n} \sum_{i'=1}^{n} \phi\left(\left[h\left(x_{i}^{s}\right), h\left(x_{i'}^{s}\right)\right]\right)$$

$$+ \frac{1}{m^{2}} \sum_{j=1}^{m} \sum_{j'=1}^{m} \phi\left(\left[h\left(x_{j}^{t}\right), h\left(x_{j'}^{t}\right)\right]\right)$$

$$- \frac{2}{mn} \sum_{i=1}^{n} \sum_{j=1}^{m} \phi\left(\left[h\left(x_{i}^{s}\right), h\left(x_{j}^{t}\right)\right]\right)\right\|_{\mathcal{H}}^{2}, \quad (5)$$

where $[\cdot, \cdot]$ represents the concatenation of two vectors, and $h(\cdot)$ is a feature transformation network that maps the input data to a shared feature space.

4) Loss Function: The overall loss function of the proposed PW-DA-DTL method is depicted as follows:

$$L = L_r + \lambda L_d, \tag{6}$$

where L_r is the regression loss (which is computed by the mean square error (MSE)) of both labeled source and target domain samples. L_d denotes the domain loss (5) between

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the merged features of target-source pairs and source-source pairs. The parameter λ serves as a penalty term that balances between the regression loss and the domain loss. The PW-DA-DTL method is trained by simultaneously minimizing the regression loss and the domain loss.

The training process of the proposed PW-DA-DTL method is presented in Algorithm 1.

Algorithm	1:	The	training	process	of	the p	roposed	
PW-DA-DTL method								
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Input: Labeled source domain samples $\{(x_i^s, y_i^s)\}_{i=1}^n$; labeled target domain samples $\{(x_j^t, y_j^t)\}_{j=1}^m$. **Output:** Model weights θ . Initialize θ and the number of training epoch N; Construct the target-source pairs $[X^t, X^s]$ and the source-source pairs $[X^s, X^s]$;

for 1: N do

Obtain [h (X^s), h (X^s)] and [h (X^t), h (X^s)];
 Calculate the MMD using (5);
 Predict y^k for dual tasks using (1);
 Run the Adam optimization algorithm to minimize (6) and update the weights θ.
 end

C. PW-DA-DTL for Co-Predicting MRD and R_a in RBG

In this article, the PW-DA-DTL method is applied for co-predicting MRD and R_a in RBG. The training process of PW-DA-DTL method unfolds in two main stages. First, existing and new machining parameters in RBG are recurrently paired to form target-source pairs and source-source pairs. Subsequently, these pairs are input into the feature transformation network for both DA and supervised dual-task model training. To be specific, the pairwise outputs of the feature transformation network are utilized for MMD calculation, and the pairwise outputs are simultaneously fed into MMoE for the supervised training.

D. Evaluation Metrics

Three evaluation metrics (i.e., the root mean square error (RMSE), the mean absolute percentage error (MAPE) and the coefficient of determination (R^2)) are employed to assess the performance of MRD and R_a co-prediction. It should be mentioned that the RMSE is applied to calculate the deviation between the predicted and observed values, the MAPE is utilized to measure the ratio of the absolute error to the observed values, and the R^2 coefficient is used to assess the correlation between the predicted and observed values. The aforementioned three evaluation metrics are formulated by

RMSE =
$$\sqrt{\frac{1}{p} \sum_{i=1}^{p} (y_i - \hat{y}_i)^2},$$
 (7)

MAPE =
$$\frac{1}{p} \sum_{i=1}^{p} \left| \frac{y_i - \hat{y}_i}{y_i} \right| \times 100\%,$$
 (8)

$$R^{2} = 1 - \sum_{i=1}^{p} \left(\hat{y}_{i} - y_{i} \right)^{2} / \sum_{i=1}^{p} \left(y_{i} - \frac{1}{p} \sum_{i=1}^{p} y_{i} \right)^{2}, \quad (9)$$

where y_i and \hat{y}_i represent the observed MRD/R_a and the predicted MRD/R_a, respectively; and p is the number of testing samples.

IV. EXPERIMENTAL DATA AND MODEL TRAINING

A. Experimental Platform

As shown in Fig. 3(a)-(b), the developed RBG system comprises an industrial robot (ABB IRB4400-60/1.96) equipped with a six-dimensional force sensor (ATI Omega 160) and an abrasive belt grinder. In the abrasive belt grinder, ceramic alumina abrasive belts $(3M^{TM}Cubitron^{TM} \text{ II } 726 \text{ A})$ with four equivalent radius of grains are chosen as the machining tools due to their substantial material removal capacity and exceptional resistance to clogging. The experimental workpiece is a unidirectional carbon fiber-reinforced composite (CFRP) T300 with dimensions of $200 \times 100 \times 10 \text{ mm}^3$, which has been widely utilized in aerospace and automotive industries. In this work, four key controlled parameters (namely, normal force F_n , robotic feed speed V_w , belt linear speed V_s and equivalent radius of abrasive grains \tilde{R}) are adjusted to investigate the MRD and R_a of RBG.

Followed by the offline system calibration and robot path planning, an orthogonal grinding experiment with different parallel grinding paths (see Fig. 3(c)) are carried out using four key machining parameters. The measurement of MRD is performed using a self-developed measuring system with an accuracy of 1 μ m and a sampling frequency of 4.33 kHz. The measurement of R_a is deployed by using a digital surface roughness tester (see Fig. 3(d)). To ensure the reliability of measurement data, the final measurement results are derived by calculating the average value of cross-sectional removal profile centers in the stable grinding area (see Fig. 3(c)).



Fig. 3. (a) The developed experimental platform of RBG. (b) The RBG system with an enlarged view of grinding process. (c) The schematic grinding paths as well as the central measurement positions of MRD and R_a . (d) The developed measuring system for obtaining MRD and R_a .

B. Dataset

In this article, the controlled machining parameters are normal force F_n , robotic feed speed V_w , belt linear speed

 V_s and equivalent radius of abrasive grains \hat{R} . Five different values are chosen for F_n (10 N, 20 N, 30 N, 40 N and 50 N), V_s (10 mm/s, 20 mm/s, 30 mm/s, 40 mm/s and 50 mm/s) and V_w (5.24 m/s, 9.42 m/s, 13.61 m/s, 17.8 m/s and 21.99 m/s), while four different values are chosen for \hat{R} (30.5 µm, 40 µm, 60 µm and 90 µm). The controlled machining parameters as well as their chosen values are recorded in Table I.

 TABLE I

 The controlled parameters and their chosen values

Controlled Parameters	Values
Normal force F_n	10, 15, 20, 25, 30 N
Robotic feed speed V_w	10, 15, 20, 25, 30 mm/s
Belt linear speed V_s	5.24, 9.42, 13.61, 17.8, 21.99 m/s
Equivalent radius of abrasive grains \widetilde{R}	30.5, 40, 60, 90 µm

After a random combination of four controlled machining parameters, an orthogonal grinding experiment with 80 sets of parameters is carried out for evaluating the performance of RBG, and the corresponding MRD and R_a are measured as the labels. Two different validation experiments are carried out according to the values of F_n and V_w , respectively. To validate the capability of the proposed PW-DA-DTL method for unseen machining parameters, the training dataset and the testing dataset are split in a cross-validation manner based on the values of F_n and V_w . Taking the validation experiment on F_n as an example, samples with a specific value of F_n are chosen as the testing dataset and the remaining samples are taken as the training dataset in each cross-validation iteration.



Fig. 4. The training process of (a) the proposed PW-DA-DTL method and (b) the MMoE method.

C. Training and Testing Process

Fig. 4(a) visualizes the training process of the proposed PW-DA-DTL method for MRD and R_a co-prediction of RBG. In this article, only one labeled target domain sample, which is randomly selected from the target dataset, is applied for training the PW-DA-DTL method in the hope of alleviating the dependence on target domain samples. The weights of the PW-DA-DTL method are copied from the pre-trained MMoE method (Fig. 4(b)), and the DA is deployed to further reduce the domain discrepancy between the target-source pairs and the source-source pairs. The regression loss L_r is the MSE for the labeled source domain samples and the labeled target domain sample, and the domain loss L_d is obtained by computing the MMD of merged features between the target-source pairs and the source-source pairs. The total loss L (which is the weighted summation of the regression loss and the domain loss) is minimized by the Adam optimizer in the training process.

The testing process is carried out by feeding the target data of four machining parameters to the trained PW-DA-DTL model, and the corresponding output is the co-predicted MRD and R_a. Five benchmark DTL methods (i.e., the MMoE method (Fig. 4(b)), the shared-bottom method, the one-gate mixture-of-experts (OMoE) method [11], the customized sharing experts (CSE) method [40] and the customized gate control (CGC) method [40]) are trained from scratch using the Adam optimizer. It is noteworthy that the shared-bottom method shares a similar architecture with the MMoE method, differing only in the replacement of the MMoE layer with a single task-shared expert network. The OMoE method focuses on using a single shared gating network to select the appropriate experts instead of the multiple gating networks employed in the MMoE method. The CSE method introduces the taskspecific expert networks into the shared-bottom method. The CGC method integrates task-shared and task-specific experts through multiple gating networks. The testing processes of the aforementioned benchmark DTL methods are carried out by feeding the target data to the trained models.

D. Network Architecture and Parameter Setting

In the experiment, the network input is the target-source pair or source-source pair of controlled machining parameters with a size of 2×4 . To learn the shared knowledge between the MRD and Ra, two fully connected layers (i.e., FC1 and FC2), whose neurons are both set to be 8, are utilized for transforming features. The merge layer is designed to merge the transformed features of paired data for the sake of reducing the domain discrepancy between target-source pairs and source-source pairs. Motivated by [11], the number of experts is set to be 4 for balancing the computational burden and learning ability. The number of gates and towers is both 2, which is consistent with the number of tasks. The number of neurons in the expert layer, gate layer and tower layer are set to be 4. The parameters of PW-DA-DTL are listed in Table II. It should be noted that all five benchmark methods share the same parameter settings as the PW-DA-DTL method in terms of input layer, FC1, FC2 and output layer. Additionally, the standard MMoE method, the OMoE method, the CGC method and the PW-DA-DTL method utilize the same number of expert networks and identical parameter configurations for the tower networks.

In the proposed PW-DA-DTL method, σ in (4) and λ in (6) are empirically set to be 0.1 and 0.01, respectively. The learning rate is set to be 0.001. Owing to the weights transfer from the standard MMoE method, the training epoch is set to

TABLE II The parameters of the proposed PW-DA-DTL network Architecture

Layer	Number	Neurons	Output size
Input	-	-	2×4
FC1	1	8	2×8
FC2	1	8	2×8
Merge	1	-	1×16
Gate in MMoE	2	4	$2 \times 1 \times 4$
Expert in MMoE	4	4	$4 \times 1 \times 4$
Tower in MMoE	2	4	$2 \times 1 \times 1$
Output A	-	-	2×1
Output B	-	-	2×1

be 100. In the five benchmark methods, the training epoch is set to be 2000.

V. RESULTS AND DISCUSSION

In this section, the co-prediction results of the MRD and R_a for RBG are presented. Specifically, two scenarios considering new normal force F_n and robotic feed speed V_w are evaluated, respectively. Furthermore, the PW-DA-DTL method is compared with five benchmark methods in terms of the prediction accuracy.

A. Case 1: Co-Prediction of MRD and R_a with New Normal Force

In this experiment, the MRD and R_a co-prediction results of the proposed PW-DA-DTL method with different testing F_n (10 N, 15 N, 20 N, 25 N and 30 N) are displayed in Fig. 5. The left figure shows the correlation between the predicted MRD and the observed MRD, and the right figure shows the correlation between the predicted R_a and the observed R_a . The two figures both showcase the consistency between the predicted values and the the observed values. To showcase the effectiveness of the PW-DA-DTL method, the predicted MRD and R_a under new F_n using different methods are shown in Fig. 6. The curves indicate that the prediction results of PW-DA-DTL (denoted as PW-DA-MMoE in figures) method are more closely to the actual labels, which demonstrates the effectiveness of the proposed method.



Fig. 5. The MRD and $\rm R_a$ co-prediction results of the proposed PW-DA-DTL method considering various new normal forces.

Table III presents the evaluation metrics for MRD and R_{a} co-prediction using the proposed PW-DA-DTL method and

five benchmark methods. The results for various F_n values indicate that the PW-DA-DTL method outperforms five benchmark methods in most cases. To provide a comprehensive comparison of the co-prediction methods, the average results across different F_n values (denoted as "All") are presented. On the one hand, the MMoE method exhibits superior coprediction performance for new F_n values compared to the shared-bottom method (which uses a single task-shared expert network), the CSE method (which combines task-shared and task-specific expert networks), the OMoE method (which employs a single task-shared gating network with multiple task-shared expert networks), and the CGC method (which utilizes multiple task-specific gating networks, task-shared expert networks, and task-specific expert networks). The results showcase that the introduced MMoE method (which integrates multiple task-specific gating networks with task-shared expert networks) is effective in balancing the correlation and discrepancy between the MRD and R_a prediction tasks.

On the other hand, ablation experiments for new F_n values reveal that the proposed PW-DA-DTL method significantly improves co-prediction accuracy compared to the standard MMoE method. The results for both MRD and R_a predictions demonstrate the effectiveness of the pairwise DA strategy in aligning data distributions between the source and target domains, even with just one labeled target domain sample. The proposed PW-DA-DTL method enables manufacturers to accurately co-predict MRD and R_a in new F_n spaces without extensive data collection, which facilitates machining parameter optimization and quality control in RBG.



Fig. 6. The predicted MRD and R_a under new F_n using the shared-bottom method, the MMoE method and the proposed PW-DA-DTL method. For the convenience of the result presentation, prediction results are sorted in ascending order according to actual labels and displayed every 3 samples. Methods with significantly poor performance, including CSE, OMoE, and CGC, are excluded from the figure.

B. Case 2: Co-Prediction of MRD and R_a with New Robotic Feed Speed

In this section, the MRD and R_a co-prediction results of the proposed PW-DA-DTL method with different V_w (10 mm/s, 15 mm/s, 20 mm/s, 25 mm/s and 30 mm/s) are displayed in Fig. 7. The left figure illustrates the correlation between the predicted MRD and the observed MRD, and the right figure shows the correlation between the predicted R_a and the observed R_a . Both figures demonstrate a significant consistency between the predicted and observed values. The predicted MRD and R_a under new V_w using different methods are displayed in

TABLE III THE MRD AND R_a co-prediction performance for various new Normal forces using different methods

$F_{\rm c}$ (N)	Mathad	RMSE		R^2		MAPE (%)	
Γ_n (IN)	wiethou	MRD	R_a	MRD	Ra	MRD	R_a
10	Shared-Bottom	0.195	0.792	0.327	0.367	42.492	13.441
	CSE	0.211	0.699	0.208	0.507	61.402	15.067
	OMoE	0.348	0.924	/	0.137	116.930	24.510
	CGC	0.178	0.487	0.437	0.761	49.189	11.316
	MMoE	0.147	0.450	0.618	0.795	45.227	9.918
	PW-DA-MMoE	0.104	0.260	0.807	0.932	24.220	5.694
	Shared-Bottom	0.133	0.479	0.919	0.783	15.328	8.548
	CSE	0.216	0.788	0.787	0.413	21.136	21.496
15	OMoE	0.251	0.975	0.712	0.101	44.165	28.235
15	CGC	0.141	0.511	0.910	0.753	15.841	11.209
	MMoE	0.114	0.342	0.941	0.889	15.384	8.372
	PW-DA-MMoE	0.110	0.339	0.945	0.892	15.518	8.094
	Shared-Bottom	0.157	0.365	0.921	0.897	16.538	6.386
	CSE	0.182	0.854	0.896	0.437	18.469	21.842
20	OMoE	0.473	1.163	0.298	/	109.205	28.880
20	CGC	0.169	0.414	0.911	0.868	15.613	8.492
	MMoE	0.146	0.378	0.934	0.890	14.601	7.670
	PW-DA-MMoE	0.144	0.377	0.935	0.891	14.557	7.545
	Shared-Bottom	0.171	0.565	0.933	0.824	9.898	5.671
	CSE	0.231	0.923	0.880	0.531	13.946	16.347
25	OMoE	0.417	1.391	0.612	/	57.472	26.760
23	CGC	0.181	0.584	0.926	0.812	11.989	5.543
	MMoE	0.207	0.517	0.904	0.853	12.950	5.281
	PW-DA-MMoE	0.185	0.511	0.924	0.856	12.464	5.079
	Shared-Bottom	0.326	0.479	0.820	0.790	26.506	10.878
30	CSE	0.286	1.030	0.863	0.032	21.120	24.695
	OMoE	0.627	1.164	0.342	/	64.313	25.299
	CGC	0.290	0.647	0.859	0.618	24.786	14.798
	MMoE	0.238	0.425	0.905	0.835	18.444	9.486
	PW-DA-MMoE	0.230	0.429	0.911	0.832	17.908	9.431
All	Shared-Bottom	0.196	0.536	0.784	0.732	21.952	8.985
	CSE	0.225	0.859	0.727	0.384	21.215	19.889
	OMoE	0.423	1.123	0.491	0.119	78.417	26.737
	CGC	0.192	0.529	0.809	0.762	23.484	10.272
	MMoE	0.170	0.422	0.860	0.852	21.321	8.145
	PW-DA-MMoE	0.155	0.383	0.904	0.881	16.933	7.169

"/" represents a negative R^2

Fig. 8. The prediction results of both the MMoE method and the PW-DA-DTL method are closer to the actual labels compared to the shared-bottom method. Moreover, the PW-DA-DTL method exhibits smaller errors when compared with the MMoE method for most machining parameters, indicating the effectiveness of the pairwise DA strategy.



Fig. 7. The MRD and $\rm R_a$ co-prediction results of the proposed PW-DA-DTL method considering various new robotic feed speeds.

In the experiment, the evaluation metrics of MRD and R_a co-prediction using the proposed PW-DA-DTL method and

five benchmark methods are recorded in Table IV. The average results listed in Table IV (as shown in "All") highlight the advantages of the proposed PW-DA-DTL method for new V_w , which can be explained in two key aspects. Firstly, the MMoE method outperforms other benchmark methods (including Shared-Bottom, CSE, OMoE, and CGC) in copredicting MRD and R_a under new V_w values. The superiority of the PW-DA-DTL method mainly lies in the employment of the MMoE method, which makes full use of multiple taskspecific gating networks and task-shared expert networks to effectively balance task correlation and discrepancy between MRD and R_a predictions. Experimental results demonstrate that the utilization of the MMoE method enables robust modeling of intertwined grinding parameters, even when the space of V_w varies significantly.

Secondly, ablation experiments reveal that the proposed PW-DA-DTL method significantly enhances the prediction performance of the standard MMoE method for MRD prediction, even when trained with just one labeled target domain sample. In addition, the PW-DA-DTL method achieves competitive performance for R_a prediction (with MAPE = 7.094%) compared to the MMoE method (with MAPE = 7.168%). By integrating the pairwise DA strategy, the PW-DA-DTL method effectively aligns data distributions between source (existing V_w spaces) and target (new V_w spaces) domains without heavily relying on labeled target domain samples. The capability of the proposed pairwise DA strategy is particularly critical for industrial applications where acquiring labeled data for every new parameter space is prohibitively expensive and time-consuming.



Fig. 8. The predicted MRD and $\rm R_a$ under new V_w using the shared-bottom method, the MMoE method and the proposed PW-DA-DTL method.



Fig. 9. Comparison among different methods as well as various working conditions using the average MAPE metric.

TABLE IV THE MRD AND R_a co-prediction performance for various new robotic feed speeds using different methods

$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	V_w	Mathad	RMSE		R^2		MAPE (%)	
Shared-Bottom 0.427 0.319 0.670 0.921 20.977 6.300 CSE 0.435 0.695 0.658 0.626 16.870 15.003 10 OMOE 0.504 0.998 0.540 0.229 19.930 19.561 10 CGC 0.312 0.375 0.824 0.891 18.060 9.066 MMoE 0.310 0.315 0.827 0.923 12.376 7.980 PW-DA-MMoE 0.139 0.319 0.965 0.921 9.403 8.198 Shared-Bottom 0.183 0.446 0.948 0.809 22.790 10.855 CSE 0.239 0.409 0.912 0.839 22.528 11.221 15 CGC 0.175 0.279 0.952 0.925 19.353 5.662 MMoE 0.176 0.235 0.952 0.9407 16.033 5.664 PW-DA-MMoE 0.141 0.228 0.969 0.950 13.565	(mm/s)	wiethou	MRD	R_a	MRD	Ra	MRD	Ra
CSE 0.435 0.695 0.658 0.626 16.870 15.003 10 OMoE 0.504 0.998 0.540 0.229 19.930 19.561 CGC 0.312 0.375 0.824 0.891 18.060 9.066 MMoE 0.130 0.315 0.827 0.923 12.376 7.980 PW-DA-MMOE 0.139 0.965 0.921 9.403 8.198 Shared-Bottom 0.183 0.446 0.948 0.809 22.790 10.855 CSE 0.239 0.409 0.912 0.839 22.528 11.21 15 CGC 0.175 0.279 0.952 0.925 19.353 5.662 MMoE 0.161 0.228 0.969 0.950 13.565 5.485 Shared-Bottom 0.142 0.428 0.937 0.809 17.515 9.157 CSE 0.146 0.405 0.933 0.829 1.147 8.993 20 <td rowspan="3">10</td> <td>Shared-Bottom</td> <td>0.427</td> <td>0.319</td> <td>0.670</td> <td>0.921</td> <td>20.977</td> <td>6.300</td>	10	Shared-Bottom	0.427	0.319	0.670	0.921	20.977	6.300
10 OMoE 0.504 0.998 0.540 0.229 19.930 19.561 CGC 0.312 0.375 0.824 0.891 18.060 9.066 MMoE 0.310 0.315 0.827 0.923 12.376 7.980 PW-DA-MMOE 0.139 0.319 0.965 0.921 9.403 8.198 Shared-Bottom 0.183 0.446 0.948 0.809 22.790 10.855 CSE 0.239 0.409 0.912 0.839 22.528 11.221 15 OMoE 0.328 0.621 0.834 0.630 40.301 13.128 CGC 0.175 0.279 0.952 0.925 19.353 5.662 MMoE 0.176 0.235 0.952 0.947 16.033 5.664 PW-DA-MMoE 0.141 0.228 0.969 0.950 13.565 5.485 Shared-Bottom 0.142 0.428 0.937 0.809 17.515 9.157		CSE	0.435	0.695	0.658	0.626	16.870	15.003
10 CGC 0.312 0.375 0.824 0.891 18.060 9.066 MMoE 0.310 0.315 0.827 0.923 12.376 7.980 PW-DA-MMoE 0.139 0.319 0.965 0.921 9.403 8.198 Shared-Bottom 0.183 0.446 0.948 0.809 22.790 10.855 CSE 0.239 0.409 0.912 0.839 22.528 11.221 15 OMoE 0.328 0.621 0.834 0.630 40.301 13.128 CGC 0.175 0.279 0.952 0.925 19.353 5.662 MMoE 0.176 0.235 0.952 0.925 13.565 5.485 Shared-Bottom 0.142 0.428 0.937 0.809 17.515 9.157 CSE 0.146 0.405 0.933 0.829 21.147 8.993 20 OMoE 0.170 1.023 0.909 / 29.522 19.66 </td <td>OMoE</td> <td>0.504</td> <td>0.998</td> <td>0.540</td> <td>0.229</td> <td>19.930</td> <td>19.561</td>		OMoE	0.504	0.998	0.540	0.229	19.930	19.561
MMoE 0.310 0.315 0.827 0.923 12.376 7.980 PW-DA-MMoE 0.139 0.319 0.965 0.921 9.403 8.198 Shared-Bottom 0.183 0.446 0.948 0.809 22.790 10.855 CSE 0.239 0.409 0.912 0.839 22.528 11.221 15 OMoE 0.328 0.621 0.834 0.630 40.301 13.128 CGC 0.175 0.279 0.952 0.925 19.353 5.662 MMoE 0.176 0.235 0.952 0.947 16.033 5.664 PW-DA-MMoE 0.141 0.228 0.969 0.950 13.565 5.485 Shared-Bottom 0.142 0.428 0.937 0.809 17.515 9.157 CSE 0.146 0.405 0.933 0.829 21.147 8.993 20 CGC 0.128 0.458 0.948 0.781 18.813 10.409 <	10	CGC	0.312	0.375	0.824	0.891	18.060	9.066
PW-DA-MMoE 0.139 0.319 0.965 0.921 9.403 8.198 Shared-Bottom 0.183 0.446 0.948 0.809 22.790 10.855 CSE 0.239 0.409 0.912 0.839 22.528 11.221 15 OMoE 0.328 0.621 0.834 0.630 40.301 13.128 15 CGC 0.175 0.279 0.952 0.925 19.353 5.662 MMoE 0.176 0.228 0.969 0.950 13.565 5.485 Shared-Bottom 0.141 0.228 0.969 0.950 13.565 5.485 Shared-Bottom 0.142 0.428 0.937 0.809 17.515 9.157 CSE 0.146 0.405 0.933 0.829 21.147 8.993 20 OMoE 0.170 1.023 0.909 / 29.522 19.646 CGC 0.128 0.458 0.943 0.886 15.432 <		MMoE	0.310	0.315	0.827	0.923	12.376	7.980
Shared-Bottom 0.183 0.446 0.948 0.809 22.790 10.855 CSE 0.239 0.409 0.912 0.839 22.528 11.221 15 OMoE 0.328 0.621 0.834 0.630 40.301 13.128 15 CGC 0.175 0.279 0.952 0.925 19.353 5.662 MMoE 0.176 0.235 0.950 13.565 5.485 Shared-Bottom 0.142 0.428 0.937 0.809 17.515 9.157 CSE 0.146 0.405 0.933 0.829 21.147 8.993 20 OMoE 0.170 1.023 0.909 / 29.522 19.646 CGC 0.128 0.458 0.948 0.781 18.813 10.409 MMoE 0.117 0.226 0.892 13.640 6.641 Shared-Bottom 0.085 0.326 0.943 0.886 15.432 9.031 CSE </td <td></td> <td>PW-DA-MMoE</td> <td>0.139</td> <td>0.319</td> <td>0.965</td> <td>0.921</td> <td>9.403</td> <td>8.198</td>		PW-DA-MMoE	0.139	0.319	0.965	0.921	9.403	8.198
CSE 0.239 0.409 0.912 0.839 22.528 11.221 15 OMoE 0.328 0.621 0.834 0.630 40.301 13.128 CGC 0.175 0.279 0.952 0.925 19.353 5.662 MMoE 0.176 0.235 0.950 13.565 5.485 Shared-Bottom 0.142 0.428 0.969 0.950 13.565 5.485 Shared-Bottom 0.142 0.428 0.937 0.809 17.515 9.157 CSE 0.146 0.405 0.933 0.829 21.147 8.993 20 OMoE 0.170 1.023 0.909 / 29.522 19.646 CGC 0.128 0.458 0.948 0.781 18.813 10.409 MMoE 0.117 0.226 0.892 13.327 7.069 PW-DA-MMoE 0.111 0.321 0.961 0.892 20.405 10.950 25 OMoE <td></td> <td>Shared-Bottom</td> <td>0.183</td> <td>0.446</td> <td>0.948</td> <td>0.809</td> <td>22.790</td> <td>10.855</td>		Shared-Bottom	0.183	0.446	0.948	0.809	22.790	10.855
15 OMoE 0.328 0.621 0.834 0.630 40.301 13.128 CGC 0.175 0.279 0.952 0.925 19.353 5.662 MMoE 0.176 0.235 0.952 0.925 19.353 5.662 PW-DA-MMOE 0.141 0.228 0.969 0.950 13.565 5.485 Shared-Bottom 0.142 0.428 0.937 0.809 17.515 9.157 CSE 0.146 0.405 0.933 0.829 21.147 8.993 20 OMoE 0.170 1.023 0.909 / 29.522 19.646 CGC 0.128 0.458 0.948 0.781 18.813 10.409 MMoE 0.111 0.321 0.961 0.892 13.640 6.641 Shared-Bottom 0.085 0.394 0.943 0.886 15.432 9.031 CSE 0.117 0.489 0.894 0.824 20.405 10.950		CSE	0.239	0.409	0.912	0.839	22.528	11.221
15 CGC 0.175 0.279 0.952 0.925 19.353 5.662 MMoE 0.176 0.235 0.952 0.947 16.033 5.664 PW-DA-MMoE 0.141 0.228 0.969 0.950 13.565 5.485 Shared-Bottom 0.142 0.428 0.937 0.809 17.515 9.157 CSE 0.146 0.405 0.933 0.829 21.147 8.993 20 OMoE 0.170 1.023 0.909 / 29.522 19.646 CGC 0.128 0.458 0.948 0.781 18.813 10.409 MMoE 0.115 0.326 0.959 0.889 13.327 7.069 PW-DA-MMoE 0.111 0.321 0.961 0.892 13.640 6.641 Shared-Bottom 0.085 0.394 0.943 0.886 15.432 9.031 CSE 0.117 0.489 0.894 0.824 20.405 10.950	15	OMoE	0.328	0.621	0.834	0.630	40.301	13.128
MMoE 0.176 0.235 0.952 0.947 16.033 5.664 PW-DA-MMoE 0.141 0.228 0.969 0.950 13.565 5.485 Shared-Bottom 0.142 0.428 0.937 0.809 17.515 9.157 CSE 0.146 0.405 0.933 0.829 21.147 8.993 20 OMoE 0.170 1.023 0.909 / 29.522 19.646 CGC 0.128 0.458 0.948 0.781 18.813 10.409 MMoE 0.115 0.326 0.959 0.889 13.327 7.069 PW-DA-MMoE 0.111 0.321 0.961 0.892 13.640 6.641 Shared-Bottom 0.085 0.394 0.943 0.886 15.432 9.031 CSE 0.117 0.489 0.894 0.824 20.405 10.950 OMoE 0.245 1.140 0.534 0.043 56.806 28.304	15	CGC	0.175	0.279	0.952	0.925	19.353	5.662
PW-DA-MMoE 0.141 0.228 0.969 0.950 13.565 5.485 Shared-Bottom 0.142 0.428 0.937 0.809 17.515 9.157 CSE 0.146 0.405 0.933 0.829 21.147 8.993 20 OMoE 0.170 1.023 0.909 / 29.522 19.646 CGC 0.128 0.458 0.948 0.781 18.813 10.409 MMoE 0.115 0.326 0.959 0.889 13.327 7.069 PW-DA-MMoE 0.111 0.321 0.961 0.822 13.640 6.641 Shared-Bottom 0.085 0.394 0.943 0.886 15.432 9.031 CSE 0.117 0.489 0.894 0.824 20.405 10.950 25 OMoE 0.245 1.140 0.534 0.043 56.806 28.304 CGC 0.127 0.722 0.875 0.616 17.285 18.190 <td></td> <td>MMoE</td> <td>0.176</td> <td>0.235</td> <td>0.952</td> <td>0.947</td> <td>16.033</td> <td>5.664</td>		MMoE	0.176	0.235	0.952	0.947	16.033	5.664
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$		PW-DA-MMoE	0.141	0.228	0.969	0.950	13.565	5.485
$ \begin{array}{c ccccc} CSE & 0.146 & 0.405 & 0.933 & 0.829 & 21.147 & 8.993 \\ 0MoE & 0.170 & 1.023 & 0.909 & / & 29.522 & 19.646 \\ CGC & 0.128 & 0.458 & 0.948 & 0.781 & 18.813 & 10.409 \\ MMoE & 0.115 & 0.326 & 0.959 & 0.889 & 13.327 & 7.069 \\ PW-DA-MMOE & 0.111 & 0.321 & 0.961 & 0.892 & 13.640 & 6.641 \\ \hline Shared-Bottom & 0.085 & 0.394 & 0.943 & 0.886 & 15.432 & 9.031 \\ CSE & 0.117 & 0.489 & 0.894 & 0.824 & 20.405 & 10.950 \\ 25 & OMoE & 0.245 & 1.140 & 0.534 & 0.043 & 56.806 & 28.304 \\ CGC & 0.127 & 0.722 & 0.875 & 0.616 & 17.285 & 18.190 \\ MMoE & 0.078 & 0.331 & 0.953 & 0.919 & 13.111 & 6.585 \\ PW-DA-MMOE & 0.075 & 0.344 & 0.957 & 0.913 & 12.985 & 6.638 \\ \hline Shared-Bottom & 0.162 & 0.775 & 0.615 & 0.652 & 19.396 & 12.498 \\ CSE & 0.177 & 0.833 & 0.539 & 0.598 & 24.458 & 12.863 \\ OMoE & 0.234 & 2.190 & 0.193 & / & 53.534 & 44.450 \\ CGC & 0.187 & 0.807 & 0.483 & 0.623 & 27.116 & 12.406 \\ MMoE & 0.114 & 0.648 & 0.809 & 0.757 & 14.443 & 8.542 \\ PW-DA-MMOE & 0.112 & 0.655 & 0.814 & 0.752 & 14.293 & 8.507 \\ \hline Shared-Bottom & 0.200 & 0.472 & 0.823 & 0.815 & 19.222 & 9.568 \\ CSE & 0.223 & 0.566 & 0.787 & 0.743 & 21.082 & 11.806 \\ OMoE & 0.296 & 1.194 & 0.602 & 0.301 & 40.019 & 25.018 \\ CGC & 0.186 & 0.528 & 0.816 & 0.767 & 20.125 & 11.147 \\ MMoE & 0.159 & 0.371 & 0.900 & 0.887 & 13.858 & 7.168 \\ PW-DA-MMOE & 0.116 & 0.373 & 0.933 & 0.886 & 12.777 & 7.094 \\ \hline \end{array}$		Shared-Bottom	0.142	0.428	0.937	0.809	17.515	9.157
20 OMoE 0.170 1.023 0.909 / 29.522 19.646 CGC 0.128 0.458 0.948 0.781 18.813 10.409 MMoE 0.115 0.326 0.959 0.889 13.327 7.069 PW-DA-MMoE 0.111 0.321 0.961 0.892 13.640 6.641 Shared-Bottom 0.085 0.394 0.943 0.886 15.432 9.031 CSE 0.117 0.489 0.894 0.824 20.405 10.950 25 OMoE 0.245 1.140 0.534 0.043 56.806 28.304 CGC 0.127 0.722 0.875 0.616 17.285 18.190 MMoE 0.078 0.331 0.953 0.919 13.111 6.585 PW-DA-MMoE 0.075 0.344 0.957 0.913 12.985 6.638 Shared-Bottom 0.162 0.775 0.615 0.652 19.396 12.498 <		CSE	0.146	0.405	0.933	0.829	21.147	8.993
20 CGC 0.128 0.458 0.948 0.781 18.813 10.409 MMoE 0.115 0.326 0.959 0.889 13.327 7.069 PW-DA-MMoE 0.111 0.321 0.961 0.892 13.640 6.641 Shared-Bottom 0.085 0.394 0.943 0.886 15.432 9.031 CSE 0.117 0.489 0.894 0.824 20.405 10.950 OMoE 0.245 1.140 0.534 0.043 56.806 28.304 CGC 0.127 0.722 0.875 0.616 17.285 18.190 MMoE 0.078 0.331 0.953 0.919 13.111 6.585 PW-DA-MMoE 0.075 0.344 0.957 0.913 12.985 6.638 Shared-Bottom 0.162 0.775 0.615 0.652 19.396 12.498 CSE 0.177 0.833 0.539 0.598 24.458 12.863	20	OMoE	0.170	1.023	0.909	/	29.522	19.646
MMoE 0.115 0.326 0.959 0.889 13.327 7.069 PW-DA-MMoE 0.111 0.321 0.961 0.892 13.640 6.641 Shared-Bottom 0.085 0.394 0.943 0.886 15.432 9.031 CSE 0.117 0.489 0.894 0.824 20.405 10.950 25 OMoE 0.245 1.140 0.534 0.043 56.806 28.304 CGC 0.127 0.722 0.875 0.616 17.285 18.190 MMoE 0.075 0.344 0.957 0.913 12.985 6.638 PW-DA-MMoE 0.075 0.615 0.652 19.396 12.498 CSE 0.177 0.833 0.539 0.598 24.458 12.863 30 CGC 0.187 0.807 0.483 0.623 27.116 12.406 MMoE 0.114 0.648 0.809 0.757 14.443 8.542 PW-	20	CGC	0.128	0.458	0.948	0.781	18.813	10.409
PW-DA-MMoE 0.111 0.321 0.961 0.892 13.640 6.641 Shared-Bottom 0.085 0.394 0.943 0.886 15.432 9.031 CSE 0.117 0.489 0.894 0.824 20.405 10.950 25 OMoE 0.245 1.140 0.534 0.043 56.806 28.304 25 CGC 0.127 0.722 0.875 0.616 17.285 18.190 MMoE 0.078 0.331 0.953 0.919 13.111 6.585 PW-DA-MMOE 0.075 0.615 0.652 19.396 12.498 CSE 0.177 0.833 0.539 0.598 24.458 12.863 30 CGC 0.187 0.807 0.483 0.623 27.116 12.406 MMoE 0.114 0.648 0.809 0.757 14.443 8.542 PW-DA-MMoE 0.112 0.655 0.814 0.752 14.293 8.507 <td></td> <td>MMoE</td> <td>0.115</td> <td>0.326</td> <td>0.959</td> <td>0.889</td> <td>13.327</td> <td>7.069</td>		MMoE	0.115	0.326	0.959	0.889	13.327	7.069
Shared-Bottom 0.085 0.394 0.943 0.886 15.432 9.031 CSE 0.117 0.489 0.894 0.824 20.405 10.950 25 OMoE 0.245 1.140 0.534 0.043 56.806 28.304 25 CGC 0.127 0.722 0.875 0.616 17.285 18.190 MMoE 0.078 0.331 0.953 0.919 13.111 6.585 PW-DA-MMOE 0.075 0.344 0.957 0.913 12.985 6.638 Shared-Bottom 0.162 0.775 0.615 0.652 12.3985 6.638 30 OMoE 0.234 2.190 0.193 / 53.534 44.450 CGC 0.187 0.807 0.483 0.623 27.116 12.406 MMoE 0.114 0.648 0.809 0.757 14.443 8.542 PW-DA-MMoE 0.112 0.655 0.814 0.752 14.293		PW-DA-MMoE	0.111	0.321	0.961	0.892	13.640	6.641
CSE 0.117 0.489 0.894 0.824 20.405 10.950 25 OMoE 0.245 1.140 0.534 0.043 56.806 28.304 CGC 0.127 0.722 0.875 0.616 17.285 18.190 MMoE 0.078 0.331 0.953 0.919 13.111 6.585 PW-DA-MMoE 0.075 0.344 0.957 0.913 12.985 6.638 Shared-Bottom 0.162 0.775 0.615 0.652 19.396 12.498 CSE 0.177 0.833 0.539 0.598 24.458 12.863 30 OMoE 0.234 2.190 0.193 / 53.534 44.450 CGC 0.187 0.807 0.483 0.623 27.116 12.406 MMoE 0.112 0.655 0.814 0.752 14.293 8.507 Shared-Bottom 0.200 0.472 0.823 0.815 19.222 9.568		Shared-Bottom	0.085	0.394	0.943	0.886	15.432	9.031
25 OMoE 0.245 1.140 0.534 0.043 56.806 28.304 CGC 0.127 0.722 0.875 0.616 17.285 18.190 MMoE 0.078 0.331 0.953 0.919 13.111 6.585 PW-DA-MMoE 0.075 0.344 0.957 0.913 12.985 6.638 Shared-Bottom 0.162 0.775 0.615 0.652 19.396 12.486 30 CSE 0.177 0.833 0.539 0.598 24.458 12.863 30 CGC 0.187 0.807 0.483 0.623 27.116 12.406 MMoE 0.114 0.648 0.809 0.757 14.443 8.542 PW-DA-MMoE 0.112 0.655 0.814 0.752 14.293 8.507 Shared-Bottom 0.200 0.472 0.823 0.815 19.222 9.568 CSE 0.223 0.566 0.787 0.743 21.082		CSE	0.117	0.489	0.894	0.824	20.405	10.950
2.5 CGC 0.127 0.722 0.875 0.616 17.285 18.190 MMoE 0.078 0.331 0.953 0.919 13.111 6.585 PW-DA-MMoE 0.075 0.344 0.957 0.913 12.985 6.638 Shared-Bottom 0.162 0.775 0.615 0.652 19.396 12.498 CSE 0.177 0.833 0.539 0.598 24.458 12.863 OMoE 0.234 2.190 0.193 / 53.534 44.450 CGC 0.187 0.807 0.483 0.623 27.116 12.406 MMoE 0.112 0.655 0.814 0.752 14.293 8.507 Shared-Bottom 0.200 0.472 0.823 0.815 19.222 9.568 CSE 0.223 0.566 0.787 0.743 21.082 11.806 MMoE 0.194 0.602 0.301 40.019 25.018 CGC 0	25	OMoE	0.245	1.140	0.534	0.043	56.806	28.304
MMoE 0.078 0.331 0.953 0.919 13.111 6.585 PW-DA-MMoE 0.075 0.344 0.957 0.913 12.985 6.638 Shared-Bottom 0.162 0.775 0.615 0.652 19.396 12.498 CSE 0.177 0.833 0.539 0.598 24.458 12.863 30 CGC 0.187 0.807 0.483 0.623 27.116 12.406 MMoE 0.114 0.648 0.809 0.757 14.443 8.542 PW-DA-MMoE 0.112 0.655 0.814 0.752 14.293 8.507 Shared-Bottom 0.200 0.472 0.823 0.815 19.222 9.568 CSE 0.223 0.566 0.787 0.743 21.082 11.806 AIII OMoE 0.296 1.194 0.602 0.301 40.019 25.018 CGC 0.186 0.528 0.816 0.767 20.125 11.47	23	CGC	0.127	0.722	0.875	0.616	17.285	18.190
PW-DA-MMoE 0.075 0.344 0.957 0.913 12.985 6.638 Shared-Bottom 0.162 0.775 0.615 0.652 19.396 12.498 CSE 0.177 0.833 0.539 0.598 24.458 12.863 30 OMoE 0.234 2.190 0.193 / 53.534 44.450 CGC 0.187 0.807 0.483 0.623 27.116 12.408 MMoE 0.114 0.648 0.809 0.757 14.443 8.542 PW-DA-MMoE 0.112 0.655 0.814 0.752 14.293 8.507 Shared-Bottom 0.200 0.472 0.823 0.815 19.222 9.568 CSE 0.223 0.566 0.787 0.743 21.082 11.806 OMoE 0.296 1.194 0.602 0.301 40.019 25.018 CGC 0.186 0.528 0.816 0.767 20.125 11.147		MMoE	0.078	0.331	0.953	0.919	13.111	6.585
Shared-Bottom 0.162 0.775 0.615 0.652 19.396 12.498 CSE 0.177 0.833 0.539 0.598 24.458 12.863 30 OMoE 0.234 2.190 0.193 / 53.534 44.450 CGC 0.187 0.807 0.483 0.623 27.116 12.406 MMoE 0.114 0.648 0.809 0.757 14.443 8.542 PW-DA-MMoE 0.112 0.655 0.814 0.752 14.293 8.507 Shared-Bottom 0.200 0.472 0.823 0.815 19.222 9.568 CSE 0.223 0.566 0.787 0.743 21.082 11.806 OMoE 0.296 1.194 0.602 0.301 40.019 25.018 CGC 0.186 0.528 0.816 0.767 20.125 11.147 MMoE 0.159 0.371 0.900 0.887 13.858 7.168		PW-DA-MMoE	0.075	0.344	0.957	0.913	12.985	6.638
CSE 0.177 0.833 0.539 0.598 24.458 12.863 30 OMoE 0.234 2.190 0.193 / 53.534 44.450 CGC 0.187 0.807 0.483 0.623 27.116 12.406 MMoE 0.114 0.648 0.809 0.757 14.443 8.542 PW-DA-MMoE 0.112 0.655 0.814 0.752 14.293 8.507 Shared-Bottom 0.200 0.472 0.823 0.815 19.222 9.568 CSE 0.223 0.566 0.787 0.743 21.082 11.806 OMoE 0.296 1.194 0.602 0.301 40.019 25.018 CGC 0.186 0.528 0.816 0.767 20.125 11.147 MMoE 0.159 0.371 0.900 0.887 13.858 7.168 PW-DA-MMoE 0.116 0.373 0.933 0.886 12.777 7.094	30	Shared-Bottom	0.162	0.775	0.615	0.652	19.396	12.498
30 OMoE 0.234 2.190 0.193 / 53.534 44.450 CGC 0.187 0.807 0.483 0.623 27.116 12.406 MMoE 0.114 0.648 0.809 0.757 14.443 8.542 PW-DA-MMoE 0.112 0.655 0.814 0.752 14.293 8.507 Shared-Bottom 0.200 0.472 0.823 0.815 19.222 9.568 CSE 0.223 0.566 0.787 0.743 21.082 11.806 OMoE 0.296 1.194 0.602 0.301 40.019 25.018 CGC 0.186 0.528 0.816 0.767 20.125 11.147 MMoE 0.159 0.371 0.900 0.887 13.858 7.168 PW-DA-MMoE 0.116 0.373 0.933 0.886 12.777 7.094		CSE	0.177	0.833	0.539	0.598	24.458	12.863
S0 CGC 0.187 0.807 0.483 0.623 27.116 12.406 MMoE 0.114 0.648 0.809 0.757 14.443 8.542 PW-DA-MMoE 0.112 0.655 0.814 0.752 14.293 8.507 Shared-Bottom 0.200 0.472 0.823 0.815 19.222 9.568 CSE 0.223 0.566 0.787 0.743 21.082 11.806 OMoE 0.296 1.194 0.602 0.301 40.019 25.018 CGC 0.186 0.528 0.816 0.767 20.125 11.147 MMoE 0.159 0.371 0.900 0.887 13.858 7.168 PW-DA-MMoE 0.116 0.373 0.933 0.886 12.777 7.094		OMoE	0.234	2.190	0.193	/	53.534	44.450
MMoE 0.114 0.648 0.809 0.757 14.443 8.542 PW-DA-MMoE 0.112 0.655 0.814 0.752 14.293 8.507 Shared-Bottom 0.200 0.472 0.823 0.815 19.222 9.568 CSE 0.223 0.566 0.787 0.743 21.082 11.806 OMoE 0.296 1.194 0.602 0.301 40.019 25.018 CGC 0.186 0.528 0.816 0.767 20.125 11.147 MMoE 0.159 0.371 0.900 0.887 13.858 7.168 PW-DA-MMoE 0.116 0.373 0.933 0.886 12.777 7.094		CGC	0.187	0.807	0.483	0.623	27.116	12.406
PW-DA-MMoE 0.112 0.655 0.814 0.752 14.293 8.507 Shared-Bottom 0.200 0.472 0.823 0.815 19.222 9.568 CSE 0.223 0.566 0.787 0.743 21.082 11.806 All OMoE 0.296 1.194 0.602 0.301 40.019 25.018 CGC 0.186 0.528 0.816 0.767 20.125 11.147 MMoE 0.159 0.371 0.900 0.887 13.858 7.168 PW-DA-MMoE 0.116 0.373 0.933 0.886 12.777 7.094		MMoE	0.114	0.648	0.809	0.757	14.443	8.542
Shared-Bottom 0.200 0.472 0.823 0.815 19.222 9.568 CSE 0.223 0.566 0.787 0.743 21.082 11.806 All OMoE 0.296 1.194 0.602 0.301 40.019 25.018 CGC 0.186 0.528 0.816 0.767 20.125 11.147 MMoE 0.159 0.371 0.900 0.887 13.858 7.168 PW-DA-MMoE 0.116 0.373 0.933 0.886 12.777 7.094		PW-DA-MMoE	0.112	0.655	0.814	0.752	14.293	8.507
CSE 0.223 0.566 0.787 0.743 21.082 11.806 All OMoE 0.296 1.194 0.602 0.301 40.019 25.018 CGC 0.186 0.528 0.816 0.767 20.125 11.147 MMoE 0.159 0.371 0.900 0.887 13.858 7.168 PW-DA-MMoE 0.116 0.373 0.933 0.886 12.777 7.094	All	Shared-Bottom	0.200	0.472	0.823	0.815	19.222	9.568
All OMoE 0.296 1.194 0.602 0.301 40.019 25.018 CGC 0.186 0.528 0.816 0.767 20.125 11.147 MMoE 0.159 0.371 0.900 0.887 13.858 7.168 PW-DA-MMoE 0.116 0.373 0.933 0.886 12.777 7.094		CSE	0.223	0.566	0.787	0.743	21.082	11.806
CGC 0.186 0.528 0.816 0.767 20.125 11.147 MMoE 0.159 0.371 0.900 0.887 13.858 7.168 PW-DA-MMoE 0.116 0.373 0.933 0.886 12.777 7.094		OMoE	0.296	1.194	0.602	0.301	40.019	25.018
MMoE 0.159 0.371 0.900 0.887 13.858 7.168 PW-DA-MMoE 0.116 0.373 0.933 0.886 12.777 7.094		CGC	0.186	0.528	0.816	0.767	20.125	11.147
PW-DA-MMoE 0.116 0.373 0.933 0.886 12.777 7.094		MMoE	0.159	0.371	0.900	0.887	13.858	7.168
		PW-DA-MMoE	0.116	0.373	0.933	0.886	12.777	7.094

"/" represents a negative R^2

Fig. 9 shows the comparison results among six methods (Shared-Bottom, CSE, OMoE, CGC, MMoE, and PW-DA-DTL) performed on two case studies, where the average MAPE is adopted as the evaluation metric for MRD and R_a prediction. Across both case studies, experimental results highlight the superiority of the proposed PW-DA-DTL method over selected benchmark methods (including Shared-Bottom, CSE, OMoE, and CGC) in co-predicting MRD and Ra for new RBG machining parameter spaces. Notably, the integration of the pairwise DA strategy enables improving the performance of the standard MMoE method under data scarcity in new machining parameter spaces. The findings underscore the practical value of the proposed method for industrial applications, where rapid adaptation to new machining parameter spaces is critical for maintaining precision and reducing operational costs.

VI. CONCLUSION

In this article, a novel PW-DA-DTL method has been introduced for MRD and R_a co-prediction with regard to unseen spaces of RBG machining parameters. The MMoE, a dual-task learning technique, has been employed to simultaneously predict MRD and R_a by balancing their cor-

relation and discrepancy. A pairwise DA strategy has been developed to significantly strengthen the labeled samples in target domain, thereby effectively reducing the cross-domain distribution discrepancy. The proposed PW-DA-DTL method has been tested on a self-developed RBG system with various grinding parameters. Experimental results have demonstrated that the proposed PW-DA-DTL method exhibits significant superiority in MRD and R_a co-prediction of RBG compared to five benchmark methods.

In the future, we aim to: 1) develop novel evolutionary computation methods to optimize the machining parameters in RBG on the basis of the PW-DA-DTL model [41], [42]; 2) compare different distance functions of domain adaptation for MRD and R_a co-prediction in RBG [43]–[45]; 3) adopt various filtering and signal processing methods to pre-process the RBG dataset [46]–[48]; and 4) apply our PW-DA-DTL method to other multi-task learning applications such as medical engineering, path planning and object detection [49], [50].

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