

Linear Contraction Behavior of Low-Carbon, Low-Alloy Steels During and After Solidification Using Real-Time Measurements

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A technique for measuring the linear contraction during and after solidification of low-alloy steel was developed and used for examination of two commercial low-carbon and low-alloy steels. The effects of several experimental parameters on the contraction were studied. The solidification contraction behavior was described using the concept of rigidity in a solidifying alloy, evolution of the solid fraction, and the microstructure development during solidification. A correlation between the linear contraction properties in the solidification range and the hot crack susceptibility was proposed and used for the estimation of hot cracking susceptibility for two studied alloys and verified with the real casting practice. The technique allows estimation of the contraction coefficient of commercial steels in a wide range of temperatures and could be helpful for computer simulation and process optimization during continuous casting.

DOI: 10.1007/s11661-013-2089-9

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I. INTRODUCTION

THE continuous casting (CC) process is the most common route to produce primary and semi-finished steel products for subsequent processing. Although the process has been continually improved since its emergence, the ongoing increase in casting speeds and demanding dimensions of slabs still causes casting defects such as uneven shell growth, surface marks, surface and internal cracks and breakouts to mention but a few. The CC process involves complicated phenomena like heat and mass transport, solidification and shell formation, structure development, evolution of thermophysical and thermomechanical properties, etc., a better understanding of which are essential for treating those defects and increasing productivity of the CC technology.^[1–3]

Hot cracking is one of the prevalent problems in CC practice of low-carbon and low-alloy steels. It forms when stresses and strains built up during solidification exceed strength and ductility developed in the solidifying material. It is well accepted that such conditions are most likely to occur at high solid fractions where solid grains have essentially formed a *coherent* dendritic network capable

of transferring stresses but films of liquid still remain at grain boundaries, thereby weakening the material and making it vulnerable to cracking if the material is exposed to tension.^[4] A systematic treatment of the crack formation process requires knowledge of structure formation within the solidification range, mushy zone coherency, and rigidity, solidification shrinkage, feeding of growing solid along with its thermal contraction, which are all interrelated phenomena.

The term “coherency” has not been always used in the same meaning by researchers through hot cracking studies. The obtained values of coherency temperature and fraction solid depend on the type of testing and on grain structure.^[5] In the context of solidification shrinkage and contraction testing, terminology used in literature to describe structure and mechanical behavior of mushy zone is mostly suited for equiaxed and mixed morphologies—usually observed in aluminum alloys.^[6–8] However, the microstructure is predominantly columnar dendritic during initial solidification inside a CC mold just below the meniscus.^[9] Thus, to avoid ambiguity arising from morphology-related physical and mechanical behavior of a solidifying shell, it is worthwhile to specify some features of the mushy zone with the columnar dendritic morphology.

The complex mechanics of the solidifying shell (including the mushy zone being in constant contact with a growing solid layer) can be attributed to its structure composed of multiple regions; each with different morphologies and mechanical responses to a transverse tension,^[10] i.e.,

- (a) region of easy feeding;
- (b) region of restricted interdendritic flow due to densification of dendritic network and liquid film formation;
- (c) region of liquid droplets in the grains and liquid films/pockets at the grain boundaries;

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Manuscript submitted May 21, 2013.



(d) region of liquid droplets in the grains and at the boundaries; and
 (e) solidified metal.

During initial solidification in CC, the stresses in the solidifying shell can be caused by both external and internal origins. An important example of the latter is the tensile stress due to solidification shrinkage and thermal contraction within the mushy zone and in the underlying solid. Being exposed to the tensile stress applied perpendicular to dendrite axis—grown along thermal gradient direction—the mushy zone in a polycrystalline solidifying alloy in regions (a) and (b) has essentially no shear strength because of the presence of interdendritic and intergranular liquid films. The dendrite trunks start to pose resistance to tensile forces when dendrite arms coalesce (transition b to c), transforming continuous liquid films into isolated liquid droplet within each grain. The temperature at which this takes place is usually referred to as zero strength temperature (ZST).^[11] However, upon the film-to-drop transition at grain boundaries (from c to d) a temperature is reached, conventionally called as *rigidity point*, at which a continuous dendritic network forms throughout the solid. At macroscopic level, a dramatic change in the solid strength occurs; the mushy zone behaves like a *coherent and rigid* solid since then and the material is capable of retaining its shape and transferring stresses. At microstructure level, dendrite arms from neighboring grains start coalescing or *bridging* to each other (*i.e.*, upper bridging temperature, $T_{b,upper}$) normally at high solid fractions while there are still some liquid pockets or droplets at the grain boundaries which weaken the solidifying metal. The so-called bridging process continues until last droplets turn to solid upon further cooling by lower bridging temperature ($T_{b,lower}$) beyond which the solid acquires its full shear strength. However, the lower bridging temperature ($T_{b,lower}$) may be well below the equilibrium solidus temperature depending on alloy system, solute redistribution in liquid and solid phases, dendrite morphology, and grain boundary energy.^[12] This would increase vulnerability of the solidifying shell to hot cracking during solidification because it extends the film-to-drop morphological transition during which the material exhibits low ductility and moderate strength; and any opening in boundaries induced by developed thermal strain cannot be compensated by liquid flow due to limited permeability of mushy zone in this region.^[4,5]

Novikov^[8] defined a vulnerable part of the solidification interval (VPSI), bounded between a temperature (or solid fraction) at which the stresses begin to build up and the solidus temperature. Based on the above argument, for a polycrystalline solidifying alloy with columnar dendritic morphology, one can designate VPSI with the upper and lower temperatures of the bridging process for the dendritic grains. Therefore, VPSI is demarcated between the rigidity point—where the material sensibly develops strength and transfers force, hence the stresses being built up from that moment on—and the solidus temperature (equilibrium or non-equilibrium depending on solidification conditions). But the question is how to

determine the rigidity point for the given alloy. Novikov^[8] also suggested to measure the so-called “linear shrinkage” (more correctly “linear contraction”) of the alloy during solidification and set the upper boundary of VPSI as the temperature at which the linear shrinkage (or rather linear thermal contraction) starts.

The solidification shrinkage is the volumetric change upon transformation from fully liquid to fully solid state in the solidification range due to the density difference between liquid and solid phases and the temperature dependence of density for the constituent phases. The linear thermal contraction in the solidification range, being a part of the total solidification shrinkage, commences only when a rigid skeleton of interconnected solid phase forms throughout the shell at a temperature known as the linear contraction onset temperature $T_{linear,onset}$. Above this temperature, the mushy zone behaves like a fluid (regions a and b) and any volumetric changes can be compensated if additional melt is supplied by a metallic head otherwise the melt level in the mold descends (the so-called surface sink). But in the CC mold, because of continuous supply of the melt, the volumetric solidification shrinkage does not appear until $T_{linear,onset}$ is reached, hence is not measurable. Below $T_{linear,onset}$, the linear contraction appears as changes in linear dimensions of the solid shell. Therefore, one can measure it as the displacement of casting walls with respect to the mold. These effects were previously demonstrated for aluminum alloys.^[7]

The temperature dependency of density causes the metal to continue thermal contraction of the shell after solidification completion. In addition to mechanical effects on the solidifying shell highlighted above, the thermal contraction results in topological changes at metal/mold interface, which continuously and noticeably reduces heat extraction rate across the interface. The linear contraction is reported to be the major factor bringing about air-gap formation that decreases the cooling rate during CC.^[13] The gap formation, in turn, can affect shell thickness and the microstructure formation processes.

A special method was originally proposed by Novikov^[8] to measure the linear shrinkage/contraction and pre-shrinkage expansion upon solidification. Its background idea was based on simultaneous measurement of displacement and temperature of the solidifying alloy under controlled solidification conditions. This method was further developed and applied successfully for studying the contraction behavior of binary and commercial aluminum alloys during and after solidification.^[6,7]

In the case of iron and steel, major thermal contraction/expansion studies were performed by dilatometer measurements at low and medium temperatures.^[14] At higher temperatures (austenite-to- δ -ferrite transformations up to melting point) density measurement was adopted as a measure of thermal expansion. Also, some theoretical calculations and models have been reported.^[15,16]

In context of casting and solidification, attention was mostly paid to hot mechanical testing; for example, Instron-type hot tensile testers to assess the metal strength during melting or solidification^[17] and submerged split-chill tensile (SSCT) apparatus for the *in situ*

204 measurement of tensile forces during shell formation.^[18]
 205 In the latter, the effect of shrinkage of the shell can be
 206 indirectly evaluated in terms of thermal stress and crack
 207 length in solidified shell.^[19] Meng *et al.*^[20] proposed a
 208 framework to simulate the shrinkage at sub-solidus
 209 temperatures. However, the Instron-type testers require
 210 careful control of dendrite growth direction during
 211 tensile tests, whereas SSCT testers need precise control
 212 of uniform shell growth around the mold. Difficulties
 213 involved in the control result in the scatter and
 214 inaccuracy of the observed data.^[9]

215 Therefore, a study directly dealing with thermal
 216 contraction behavior of iron and steel during and after
 217 solidification under casting conditions would be signif-
 218 icant. This article describes the development of an
 219 experimental technique for measuring contraction of
 220 solidifying steel, and the analysis of the contraction
 221 behavior of low-alloy steels during and after solidifica-
 222 tion. In this regard, design requirements are first
 223 reviewed, the results of the contraction measurements
 224 for two commercial steel grades are given; the correla-
 225 tion of contraction with solidification development and
 226 the effect of steel grade are discussed. Finally, experi-
 227 mental results obtained using the developed technique
 228 are applied to the analysis of crack susceptibility and
 229 sub-solidus contraction.

230

II. EXPERIMENTAL

231 Almost all designs reported in literature for measure-
 232 ment of linear contraction during solidification—used
 233 for low melting point alloys—consist of common
 234 features such as a casting cavity with stationary and
 235 moving walls, a cooling medium to yield high cooling
 236 rates comparable to casting conditions and simulta-
 237 neous measurements of temperature and displacement.

238 The experimental setup used in this study for mea-
 239 surement of the linear contraction upon solidification is
 240 based on the idea introduced by Novikov^[8] and further
 241 developed by Eskin *et al.*,^[6,7] and is shown in

242 Figure 1(a). The mold is made of graphite because of
 243 its high thermal conductivity and low friction properties.
 244 The mold cavity is embedded between two T-shaped
 245 geometries at both ends of the casting, as shown in
 246 Figure 1(b); one as stationary and the other as linear
 247 moving wall whose movement is measured by a dis-
 248 placement sensor. Also, a thermocouple measures tem-
 249 perature of the solidifying metal at a reference point
 250 which is discussed below.

251 The solidification in the cavity should be in a manner
 252 that two solidifying sections—having initiated from the
 253 either casting ends—meet, or bridge, at the central
 254 section of the casting. In this way, the contraction of the
 255 casting is controlled by conditions at the hot spot (*i.e.*,
 256 the temperature measurement point). After bridging
 257 occurs at the hot spot ($T_{\text{linear,onset}}$), the thermal con-
 258 traction of the casting manifests itself as the *linear*
 259 displacement of the moving wall, being measured by the
 260 displacement sensor.

261 The T-shaped geometries at both heads perform a
 262 dual thermal-mechanical function. First, due to the
 263 thinner section compared to the main cavity, the melt
 264 here solidifies faster than the rest of the mold, hence
 265 these T-shaped cavities act as freezing initiators provid-
 266 ing the desirable solidification pattern. Second, the
 267 stationary T-head restrains the sample on its end during
 268 solidification whereas the loose T-head (*i.e.*, the moving
 269 wall) is attached to and moves with the solidifying metal
 270 as a result of sample shrinkage and contraction.

271 The cross section of the main cavity used in experi-
 272 ments is 25×10 mm with a gage length of 100 mm as
 273 shown in Figure 1(b). The dimensions of the mold were
 274 chosen according to Novikov *et al.*^[21] who showed that
 275 these dimensions made the measured property not scale-
 276 dependent.

277 The moving wall design and displacement measure-
 278 ment mechanism are essential in the contraction setup.
 279 In earlier experiments with aluminum alloys, a linear
 280 variable differential transformer (LVDT) was used to
 281 measure the displacement of the moving wall. The
 282 LVDT was attached to the moving wall from outside
 283 and aligned with the longitudinal axis of the mold as

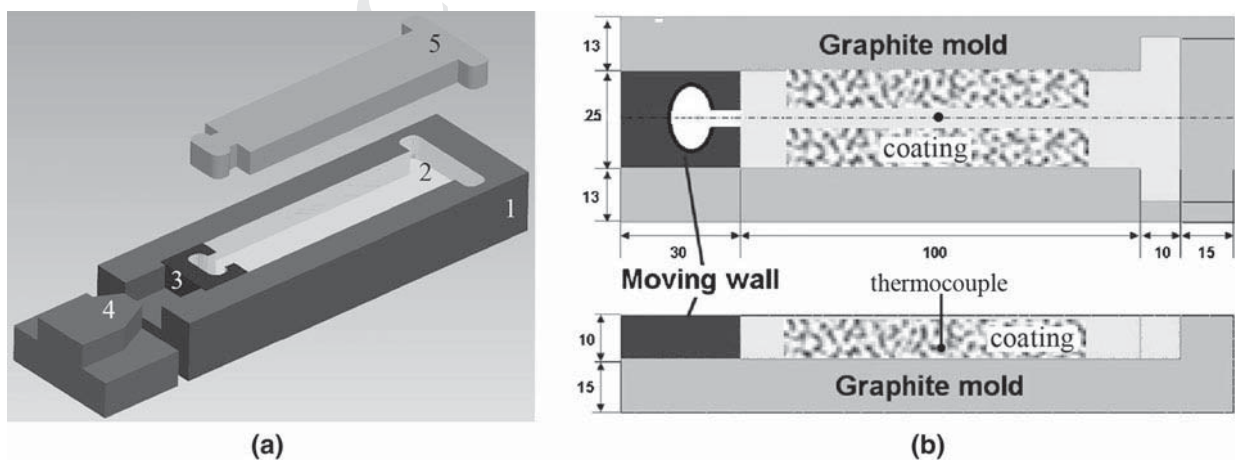


Fig. 1—Experimental setup (a): mold (1), cavity (2), moving block (3), displacement sensor (4), and casting/sample (5), and drawing of the mold and coating scheme (b) where dimensions are in mm.

284 reported in Reference 7. On the inner side the moving
 285 wall was connected to the sample by a threaded metallic
 286 rod. But the application of such method in the case of
 287 liquid steel, due to very high temperatures, becomes very
 288 limited. The metallic rod cannot be used for the
 289 connection due to its dissolution in the molten steel.
 290 The conduction of heat through the moving block
 291 results in intrinsic thermal expansion of connecting arm
 292 of the LVDT that brings about erroneous reading. To
 293 overcome these problems, a T-shaped cavity was made
 294 in the moving wall similar to that in the mold and a
 295 *contactless* laser displacement sensor was used for
 296 measurements. The linear displacement is measured by
 297 a μ -Epsilon model ILD1401-5 laser sensor, which is
 298 accurate to 3 μ m or 0.003 pct under dynamic conditions.
 299 For reproducibility of measurements within the accu-
 300 racy range, each series of experimental conditions has
 301 been tested at least twice and the average values are
 302 reported. The combination of contactless displacement
 303 sensor and low friction graphite/graphite contact pro-
 304 vides minimum impact of friction and drag on the
 305 measured contraction.

306 The temperature was measured by 0.35-mm-thick
 307 B-type thermocouples with an open tip that enables
 308 quick response to the changing temperature. The ther-
 309 mocouple is placed along centerline at central section of
 310 the cavity, close to bottom; the distance between the
 311 thermocouple tip and the bottom of the mold being
 312 about 1.5 mm. Lower distances may result in problems
 313 with filling the gap between the thermocouple tip and
 314 the mold bottom. Accuracy of temperature measure-
 315 ments is within 2 K (-271°C). During the experiments,
 316 the temperature and displacement are recorded simul-
 317 taneously by a computerized data acquisition system
 318 (National Instrument interface and Labview software).

319 In addition to design considerations, heat-transfer
 320 conditions during solidification play an important role
 321 in achieving the desired freezing pattern and hence
 322 accurate and reproducible measurements. Heat transfer
 323 can be conditioned by selecting a refractory coating and
 324 its application scheme. The effect of heat-transfer
 325 conditioning on the freezing pattern was previously
 326 studied through computation and measurement of
 327 temperature distribution, using a grid of thermocouples
 328 inside the mold under different configurations, *i.e.*, bare
 329 and refractory-coated mold surfaces.^[7,22] Computer
 330 simulation of solidification of the casting in the exper-
 331 imental mold shows that the bridging of two almost
 332 solidified sections occurs at the central section very close
 333 to the bottom of casting.^[6,23] However, without proper
 334 mold conditioning, transverse thermal gradient due to
 335 cooling effect of side walls leads to the curvature of
 336 solidification fronts and makes the bridging at the
 337 central section happen first close to the side walls instead

of the centerline, *i.e.*, the thermocouple location. In this
 case, the measured temperature would not reflect the
 real temperature at which the contraction starts.

Therefore, the refractory coating should be applied in
 such a scheme that facilitates decreasing of transverse
 thermal gradient while increasing the longitudinal gra-
 dient and maintaining the vertical gradient for solid
 structure formation. If so, it is more likely to make two
 progressing solidification fronts flatter and meet first at
 the thermocouple location. Figure 1(b) depicts the
 optimum coating scheme in which the middle part of
 the mold is coated by a thick layer of zirconium oxide as
 a low conductivity paint. The rest of the surface of the
 cavity is coated by a thin layer of boron nitride as a high
 conductivity paint to prevent carbon pickup by the
 liquid steel.

Two commercial low-carbon, low-alloy steel grades
 used in this study were normally cast at the Direct Sheet
 Plant in IJmuiden, Tata Steel Mainland Europe. The
 chemical compositions of the alloys are given in Table I.
 The alloys were re-melted in an induction melting
 furnace under protective argon atmosphere. The liquid
 steel was deoxidized prior to pouring, then cast at a
 temperature of 1903 K (1630 $^\circ\text{C}$) to fill the entire mold
 cavity especially the gap between the thermocouple and
 the mold bottom. The cooling rate in the experiments
 was 10 to 12 K/s which is comparable to casting
 conditions in CC practice.

An example of the primary data, *i.e.*, temperature and
 displacement *vs* time, is shown in Figure 2. The cooling
 curve is then processed to obtain characteristic solidifi-
 cation temperatures and cooling rate during experi-
 ments. Also, the displacement data are reconstructed to
 find temperature dependency of the contraction during
 solidification and further cooling in solid state which is
 discussed in detail later. From such correlation, the
 linear solidification contraction, the onset temperature
 of linear contraction, and the linear thermal contraction
 coefficient (TCC) at sub-solidus temperatures can be
 estimated.

The linear contraction is determined as follows:


$$\varepsilon_s = [(L_s - L_i)/L_s] \times 100, \quad [1]$$

where L_s is the initial length of the sample at the
 measurement *start* (*i.e.*, the cavity gage length of
 100 mm) and L_i is the final length of the sample
 corresponding to the measurement *instant*. For example,
 if the amount of the accumulated strain during solidifi-
 cation is of interest, L_i denotes the instantaneous length of
 the sample as the solidus temperature is reached.

Evolution of dissolved gas in the melt during solidifi-
 cation can result in some expansion prior to appearance of
 shrinkage, called pre-shrinkage expansion, which should
 be taken into account for calculation of the solidification

Table I. Chemical Composition of the Studied Steel Grades

Steel Grade	C (Wt Pct)	Mn (Wt Pct)	V (Wt Pct)	Nb (Wt Pct)	N (ppm)
LCAK	0.045	0.22	—	—	—
HSLA	0.045	0.8	0.13	0.013	130

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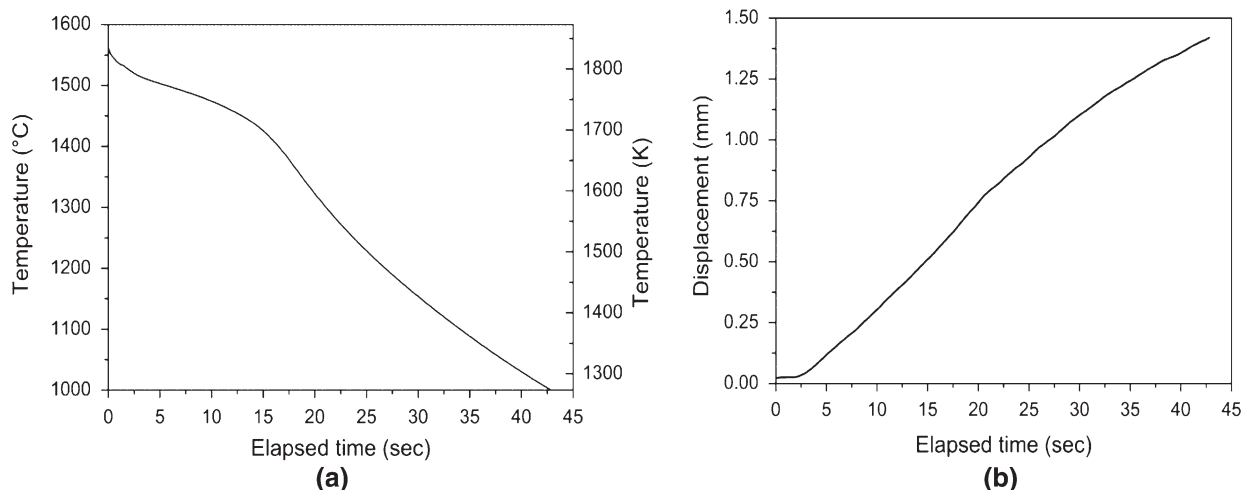


Fig. 2—Cooling curve (a) and displacement measurement (b) of HSLA-grade sample.

391 contraction as observed in aluminum alloy solidifica- 430
 392 tion.^[7,8] The occurrence of the pre-shrinkage expansion 431
 393 depends on alloy system, solidification conditions, and 432
 394 structure formation during solidification. In contrast to 433
 395 solidification of aluminum alloys, low-carbon steels in 434
 396 this study have much narrower freezing range and solidify 435
 397 predominantly with columnar grain morphology under 436
 398 CC conditions. In addition, the liquid steels in these 437
 399 experiments were deoxidized prior to casting. As a 438
 400 combination of these factors, no pre-shrinkage expansion 439
 401 was observed in the experiments. 440

402 The experimental materials were also analyzed using a 441
 403 high-temperature differential scanning calorimeter 442
 404 (instrument model: Setsys[®] TG DSC) to understand 443
 405 phase transformation sequence of the steel upon solid- 444
 406 ification and subsequent cooling as well as to determine 445
 407 the characteristic temperatures. The TG-DSC rod was 446
 408 calibrated in temperature by using a palladium standard 447
 409 material and measuring its melting temperature. The 448
 410 onset of the melting peak was determined at 1826.9 K 449
 411 (1553.9 °C) whereas the literature gives 1827.8 450
 412 (1554.8 °C). Then, all measured temperatures on the 451
 413 samples curves were corrected according to the differ- 452
 414 ence noticed between the measured and the literature 453
 415 temperatures. It has to be noticed that there is no 454
 416 method for the temperature calibration in the cooling 455
 417 mode. In fact there is always a difference between the 456
 418 melting temperature and the crystallization temperature 457
 419 for a metallic standard material due to undercooling. As 458
 420 a consequence the temperature calibration obtained 459
 421 during the heating mode was also used during the 460
 422 cooling mode. In addition, to calculate evolution of 461
 423 solid fraction during solidification under equilibrium 462
 424 and non-equilibrium conditions, solidification paths of 463
 425 the studied steel grades were simulated using Thermo- 464
 426 Calc[®] software (database TCFE6).^[23] 465

427 III. RESULTS AND DISCUSSION 466

428 In this section, the effect of some design and process- 467
 429 ing parameters on the measurements are reviewed 468
 469

first—whereby the experimental technique was im- 430
 proved in terms of better heat-transfer conditions, 431
 desirable freezing pattern of the sample, and correct 432
 temperature reading. After that, the contraction behav- 433
 ior of the studied steel grades is analyzed using the 434
 results of the experimental technique. Then, an effort is 435
 made to explain hot crack susceptibility of these steel 436
 grades based on their contraction behavior and micro- 437
 structure formation during solidification. A note on the 438
 linear thermal contraction after the end of solidification 439
 is given finally. 440

441 A. Test Verification and Effect of Parameters 442

In practice, experimental results of the contraction 442
 measurements in the given method can be affected by a 443
 number of parameters such as the gage length of the 444
 mold, mass of the casting, dragging effects (mold friction 445
 and other opposing forces), and, particularly, heat- 446
 transfer modifiers (refractory coatings, *etc.*) inside the 447
 mold. 448

It was shown that the variation of the gage length 449
 from 100 to 50 mm does not affect the measured 450
 contraction.^[7] The casting mass, parameterized as height 451
 of the sample assuming the same gage length, can affect 452
 the results through altering thermal gradients, freezing 453
 pattern, and mechanical and flow properties of the 454
 solidifying metal.^[24] In this study, with decreasing level 455
 of the melt from 15 to 10 mm, the amount of contraction 456
 accumulated during solidification reduced. This 457
 would originate from inhomogeneity across a vertical 458
 section of the solidifying metal. In other words, in a 459
 thicker sample, different layers of the section are 460
 experiencing different stages of solidification; having 461
 different amounts of solid and contracting at different 462
 rates, *etc.*, which may induce additional measured 463
 contraction during solidification. Although a higher 464
 level of the melt in the experimental mold could imitate 465
 liquid metal head in CC mold, its effects would be a 466
 combination of thermal and mechanical interactions 467
 between the liquid metal and the solidifying shell. In a 468
 severe case, it can unbalance the thermal gradients 469

470 within the sample and affect heat-transfer conditions.
 471 Therefore, for the sake of establishing more homogeneity
 472 across the sample and balanced thermal gradients,
 473 the lower metal level, 10 mm, was adopted for main
 474 tests of this study.

475 Opposing forces arising from the friction between the
 476 sliding parts of the mold can influence the measured
 477 contraction. It was reported that, for aluminum alloys,
 478 the amount of linear contraction during solidification
 479 considerably decreases as a result of such forces while
 480 the temperature of the contraction onset is not affected
 481 that much.^[6] In contrast, our experimental results show
 482 that the steel is almost insensitive to the friction effects
 483 which could be attributed to a higher strength of steel.
 484 However, low friction sliding contact, enough clearance
 485 between moving parts, and using a contactless displacement
 486 sensor are effective measures to minimize the friction
 487 and dragging effects.

488 As it is noted in Experimental, the coating should
 489 regulate heat-transfer conditions in the experimental
 490 mold so that the bridging of the almost solidified
 491 sections occurs close to the thermocouple location. Such
 492 freezing pattern can be examined through observation
 493 of the solidification structure or computer simulation.
 494 Figure 3 shows the longitudinal section of the sample
 495 through its longitudinal symmetry plane which also
 496 encompasses the thermocouple position. Figure 4
 497 depicts the mosaic image reconstructed from tens of
 498 micrographs of the HSLA sample through the annotated
 499 section in Figure 3. Columnar dendritic structure
 500 can be clearly seen at the vicinity of mold walls under
 501 local thermal gradients. At regions far from the mold
 502 walls, the structure transits from columnar to mixed

503 dendrites due to decreasing thermal gradients. The
 504 solidification process can be described as follows: just
 505 after mold filling, solidification starts at the right end of
 506 the sample into strong cooling effect of T-junction and
 507 in the T-opening of the moving head, then progresses
 508 toward the central section, *i.e.*, the left side of the
 509 micrograph in Figure 4. However, in the middle part of
 510 sample at this section, the effect of vertical thermal
 511 gradient becomes more pronounced due to bottom
 512 cooling of the mold which facilitates the primary
 513 dendrites to be aligned closer to the vertical direction.
 514 Therefore, the local thermal gradient, determining the
 515 freezing pattern and structure formation during solidi-
 516 fication, is a combination of two parts; the vertical
 517 component along which the primary dendrites grow
 518 bottom-up and the longitudinal component which
 519 prioritizes the freezing sequence along the sample
 520 longitudinal axis so that T-heads are the first and the
 521 centerline is the last section to solidify. Such pattern
 522 causes the central section to be the hot spot of the
 523 sample. The existence of a shrinkage cavity in the central
 524 section of the sample verifies the described pattern and is
 525 in agreement with results of computer simulation of heat
 526 transfer in the experimental mold.^[6,25]

527 Figure 5(a) shows an idealized representation of
 528 solidification configuration around centerline based on
 529 the described freezing pattern and Figure 5(b) illustrates
 530 the observed micrograph of HSLA sample very close to
 531 the centerline where the thermocouple (TC) is located.
 532 As soon as the rigidity temperature (solid fraction) is
 533 reached in the lowermost layer of the sample, the
 534 bridging starts and the dendritic grains at either sides of
 535 the centerline coalesce together and the sample starts to
 536 retain its shape and behave like a coherent solid from
 537 that moment on. Recalling that one end of the sample is
 538 constrained and the other is fixed to the free-moving
 539 head, the thermal contraction of the solidifying metal at
 540 the hot spot results in drawing of the free, already
 541 solidified section which is attached to the moving head
 542 whose position is being registered. Therefore, the
 543 rigidity point stands for the temperature of linear
 544 contraction onset and the magnitude of the movement
 545 is a measure of the linear thermal contraction.

546 Notwithstanding differences in scales and spatial
 547 orientation, the solidification configuration of melt in
 548 the experimental mold in this study and the initial
 549 solidification of strand in a CC mold display several
 550 thermal, physical, and mechanical similarities. For
 551 example, the contraction of the sample in the experi-
 552 mental mold can simulate the free contraction of

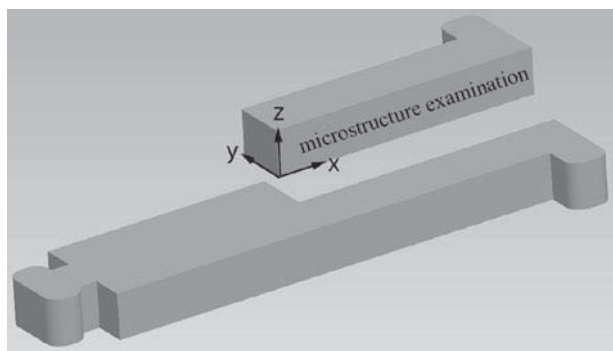


Fig. 3—Sample sectioning for micrograph examination of freezing (the coordinate system x : longitudinal, y : transverse, and z : vertical direction).

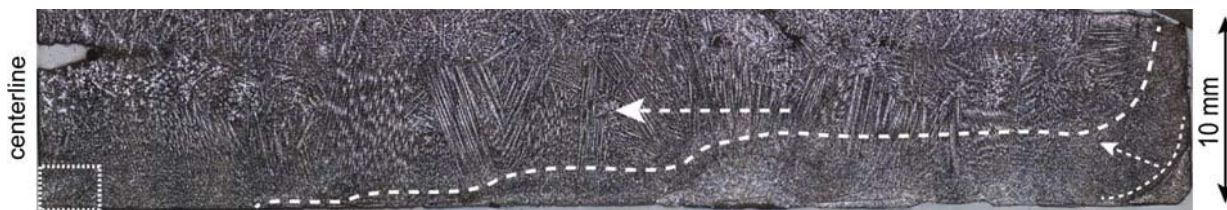


Fig. 4—The reconstructed picture of micrographs along the symmetry ($x-z$) plane of the sample shown in Fig. 3. Arrows show the freezing progression within the sample. The dotted rectangle (where thermocouple is located) is shown in Fig. 5(b).

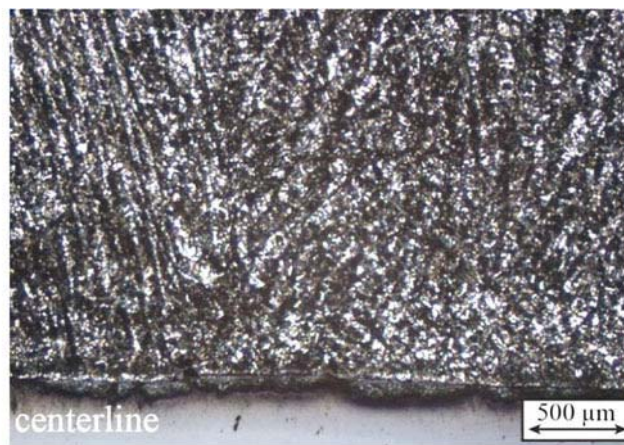
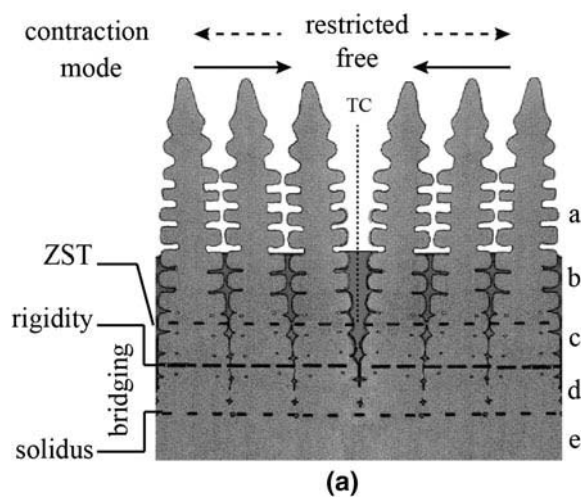


Fig. 5—Idealized representation of two (symmetric) dendritic grains with a grain boundary (a), microstructure of the HSLA sample at the vicinity of mold close to the central section (b). Properties of regions a through e are mentioned in Section I.

553 solidifying shell over the wide face of a CC mold as the
 554 strand moves inside the mold along casting direction,
 555 which results in separation of the strand from the CC
 556 mold narrow faces and in the air-gap formation.^[20] The
 557 gap formation causes the rise of surface temperature and
 558 weakening of the shell with a risk for crack formation.
 559 ^[1,2] To accommodate this shrinkage and contraction,
 560 the narrow faces of a CC mold are tapered.^[20]
 561 Alternatively, if thermal contraction (quantified as the
 562 corresponding thermal strain) of the solidifying shell is
 563 restricted by any means, a tensile thermal stress is
 564 developed in the shell which is applied perpendicular to
 565 the growth direction of the solid and causes the opening
 566 of the dendrites during solidification and cracking.
 567 These modes are depicted in Figure 5(a) with arrows
 568 over the dendrites.

569 B. Solidification Analysis

570 The understanding of contraction phenomena needs
 571 supplementary information about material behavior
 572 upon solidification and subsequent cooling, *i.e.*, phase
 573 transformation sequence of the alloys and evolution of
 574 the solid fraction during solidification should be known.
 575 The phase transformation sequence of the given steel
 576 grades was calculated using the ThermoCalc[®] software.
 577 To determine the transformation temperatures for
 578 conditions closer to the experimental conditions, the
 579 steel samples were analyzed using DSC with a rate of
 580 20 K/s. The onsets of peaks on heating and on cooling
 581 were used as characteristic temperatures. Since the
 582 primary output of DSC measurement for temperature
 583 difference is in μV , this is what reported in this paper as
 584 the heat flow values were not of interest in these
 585 experiments. The lower temperature limit in this study
 586 was chosen as 1273 K (1000 °C) because the strand
 587 surface temperature exiting the CC mold is reported to
 588 be around this temperature.^[20]

589 Figure 6 gives examples of the calculated pseudo-
 590 binary phase diagram of a low-alloy steel system and

591 also the corresponding DSC results. HSLA steel, as
 592 marked off in Figure 6(a), solidifies fully in the δ -ferrite
 593 mode. Upon subsequent cooling, δ -ferrite transforms to
 594 austenite (γ) completely in the solid state and MnS
 595 precipitates at lower temperatures. To concur with that,
 596 DSC results, as shown in Figure 6(b), display typical
 597 curve of δ -ferrite solidification in the HSLA steel. The
 598 HSLA steel shows liquidus and solidus temperatures of
 599 1801 K and 1777 K (1528 °C and 1504 °C), respec-
 600 tively. Similarly, LCAK-grade steel also exhibits
 601 δ -ferrite solidification mode, with 1806 K (1533 °C)
 602 liquidus and 1782 K (1509 °C) solidus temperatures,
 603 followed by δ/γ transformation upon further cooling in
 604 the solid state but with different transformation tem-
 605 peratures. The temperatures related to the start and end
 606 of these phase transformations for the studied steel
 607 grades are summarized in Table II based on the phase
 608 diagram calculations and the experimental measure-
 609 ments.

610 The evolution of fraction of solid, required for
 611 characterization of the linear contraction onset, was
 612 calculated using ThermoCalc[®] under two different
 613 conditions. At higher cooling rates, at which non-
 614 equilibrium effects become more important, the Scheil
 615 model was used to estimate the extreme non-equilib-
 616 rium solidification conditions (the solidus temperature
 617 and the evolution of solid fraction). In practice, the
 618 solidification would occur under intermediate condi-
 619 tions. In the Scheil approximation, δ -ferrite was the
 620 solid phase forming during solidification and carbon
 621 and interstitial components were considered as fast-
 622 diffusing elements. The results of the calculated solid
 623 fractions in the equilibrium and Scheil solidification
 624 modes can be seen in Figure 7 for both steels. It is
 625 noteworthy that there is a slight difference in the
 626 solidification paths of the LCAK steel under two
 627 conditions supposedly due to its lower alloy content
 628 while for the HSLA steel the DSC-measured solidus is
 629 closer to the calculated temperature in the equilibrium
 630 curve.

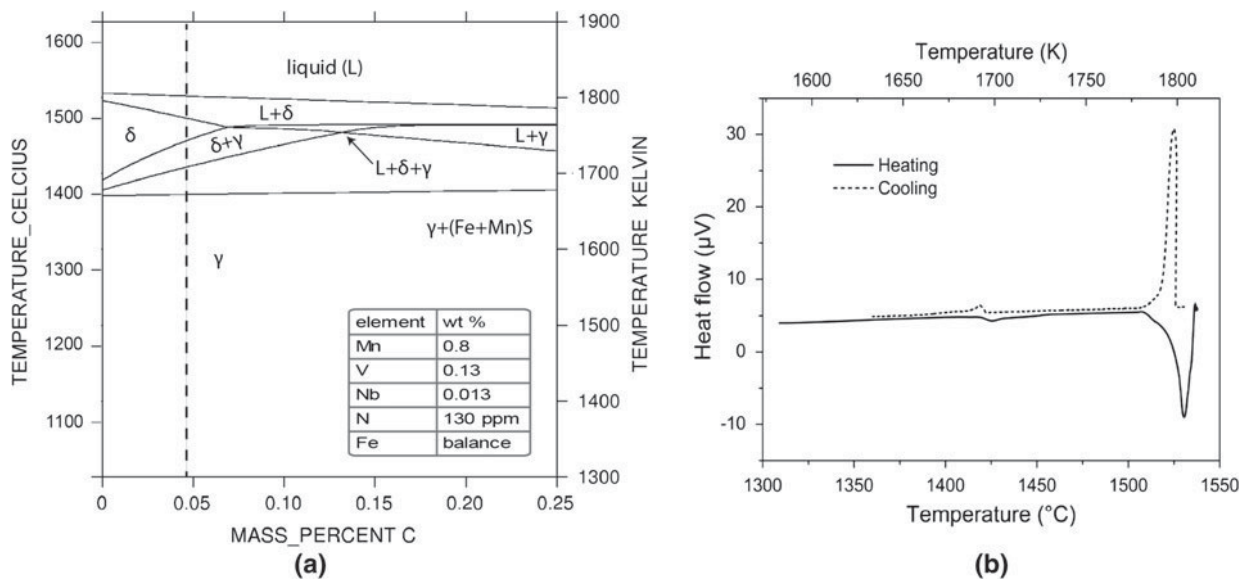


Fig. 6—Calculated phase diagram (a) of low-alloy steel of the indicated chemical composition showing transformation path of the HSLA steel (dashed line) upon solidification and cooling; the corresponding DSC measurement (b) for the HSLA steel showing δ -solidification mode and δ/γ transformation in solid.

Table II. Transformation Temperatures [K-(°C)] in the Studied Steels

Transformation	HSLA Phase Diagram [K (°C)]	HSLA Experimental [K (°C)]	LCAK Phase Diagram [K (°C)]	LCAK Experimental [K (°C)]
$L \rightarrow L + \delta$	1802 (1529)	1801 (1528)	1807 (1534)	1805 (1532)
$L + \delta \rightarrow \delta$	1780 (1507)	1777 (1504)	1784 (1511)	1780 (1507)
$\delta \rightarrow \delta + \gamma$	1739 (1466)	1716 (1443)	1734 (1461)	1729 (1456)
$\delta + \gamma \rightarrow \gamma$	1706 (1433)	1691 (1418)	1702 (1429)	1697 (1424)

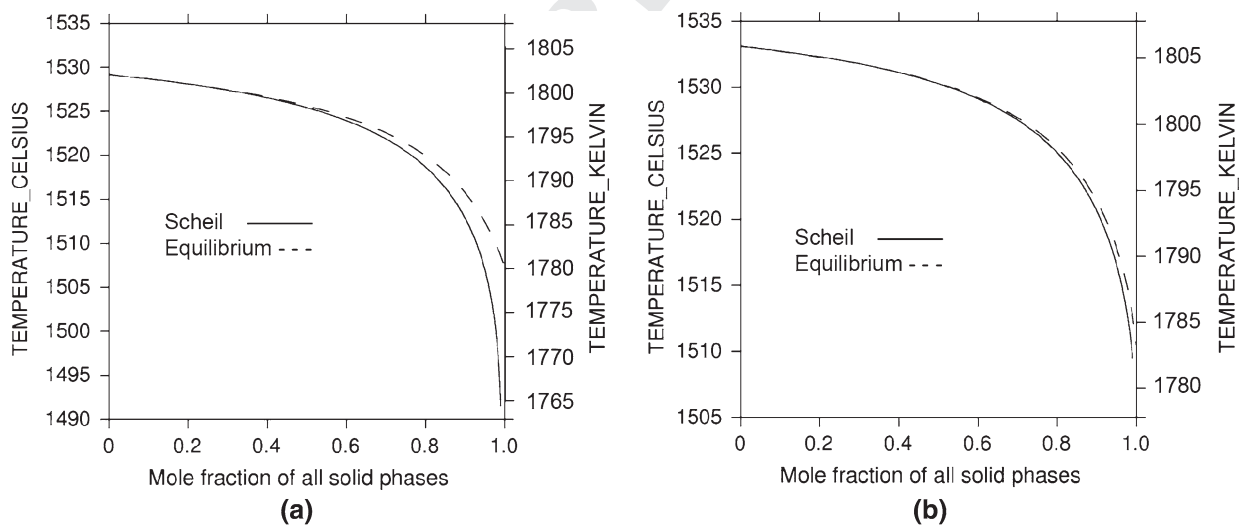


Fig. 7—Calculated evolution of solid fraction in the HSLA (a) and the LCAK steel, (b) during δ -solidification under equilibrium and Scheil conditions.

31 C. Thermal Contraction During Solidification

32 As the next step, the volumetric shrinkage occurring
 33 during solidification of δ -ferrite was calculated using
 34 volume and density change data based on measurements
 35 and model given in References 15, 16. This volume

change, mainly resulting from the density difference
 between liquid steel and δ -ferrite, develops over the
 solidification range. Total solidification shrinkage accu-
 mulated between the liquidus and the solidus for HSLA
 and LCAK is about 3.5 pct.

641 However, this average 3-D shrinkage first shows up as
 642 the decrease in melt level in the mold (surface sink)
 643 before the metal retains its rigidity and the sample can
 644 contract uniformly (linearly). Therefore, the volume
 645 solidification shrinkage is much larger than the linear
 646 thermal contraction and cannot be used for assessment
 647 of hot tearing susceptibility or geometry changes during
 648 CC.^[20] The temperature dependency of the linear
 649 contraction of the studied low-carbon and low-alloy
 650 steel is shown in Figure 8 and some selected accumu-
 651 lated linear contraction values are summarized in
 652 Table III. Our measurements show that the linear
 653 contraction developed upon solidification of HSLA
 654 and LCAK grades are about 0.13 and 0.18 pct,
 655 respectively. Although no relevant values have been
 656 yet reported for steel, one may consider the thermal
 657 contraction in the solidification range of an Al-Cu alloy
 658 as a benchmark. For example, during solidification of
 659 an Al-4 wt pct Cu alloy, linear contraction values of 0.16
 660 to 0.22 pct have been reported at low friction forces
 661 while this alloy has about 5.3 pct volume contraction
 662 upon solidification.^[6]

663 The important parameter derived from the experi-
 664 mental results is the temperature at which the linear
 665 contraction starts. For the HSLA grade, the linear
 666 contraction onset temperature ($T_{\text{linear,onset}}$) is about
 667 1790 K (1517 °C). This value is indeed a measure of
 668 temperature or solid fraction at which the bridging
 669 between the solidified sections starts and a rigid

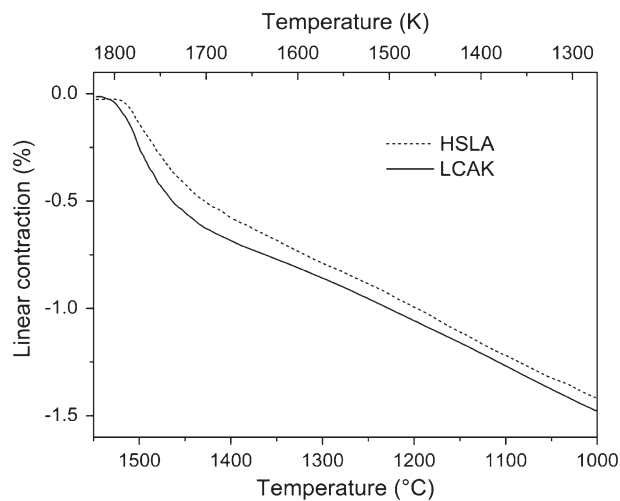


Fig. 8—Reconstructed contraction curves of the HSLA and the LCAK steel grades. Important values are summarized in Table III.

dendritic network forms. It was pointed out for other
 alloy systems that this temperature is independent of the
 friction force and known as a characteristic temperature
 of an alloy.^[6] Referring to the calculated solid fraction
 developing during solidification of the HSLA steel
 (Figure 7(a)), the linear solidification contraction onset
 corresponds to a solid fraction of 0.83 to 0.87 depending
 on solidification conditions. Shin *et al.*^[26] explored the
 tensile strength of *in situ* solidifying Fe-(0.06 to 0.6) wt
 pct C-1 pct Mn steels near their solidus temperatures
 using Instron-type high-temperature tensile strength
 tester. They found that the solid fraction (f_s) at ZST
 for these alloys is about 0.6 to 0.8 as the fraction in
 which dendrite arms start to interact to resist tension.
 These values are close to the measured values in this
 investigation. The difference could be due to the fact
 that for a polycrystalline metal ZST is reached at higher
 temperature (or lower solid fraction) which is shown in
 Figure 5(a). It is even possible that the temperature of
 contraction onset lies between the temperatures of
 equilibrium and non-equilibrium solidus—as it is the
 case of most aluminum alloys—in which the bridging of
 dendritic network and, in turn, the rigidity happen at
 very high solid fractions.

It can be readily seen that HSLA and LCAK exhibit
 quite similar contraction behaviors because their solidi-
 fication mode and phase transformation sequence are
 very close except that their transformation temperatures
 and phase compositions are different. The linear solidi-
 fication contraction of the LCAK steel commences at
 1801 K (1528 °C) which is higher than that of the HSLA
 steel, as the LCAK grade has the higher liquidus
 temperature. The solid fraction corresponding to the
 linear contraction onset of the LCAK steel is about 0.72
 which is a lower value with respect to the HSLA grade.
 Also, the accumulated solidification contraction of the
 LCAK steel is 0.18 pct which is larger compared with
 that of the HSLA steel.

D. Steel Grade and Crack Susceptibility

Comparing the contraction data of the studied steel
 grades, one can find a correlation between the solid
 fraction and the thermal contraction as follows: the
 lower the solid fraction at the contraction onset tem-
 perature, the larger the accumulated thermal contrac-
 tion in the solidification range. In this regard, the
 contraction behavior could provide a basis for the
 analysis of hot cracking susceptibility of these steels.
 Analysis of the evolution of solid fraction along with the
 contraction behavior reveals that although the liquidus
 temperature of the HSLA steel is lower than that of the

Table III. Summary of Contraction Values of the Studied Steels

Alloy	$T_{\text{linear,onset}}$ [K (°C)]	Solid Fraction ($T_{\text{linear/onset}}$)	Accumulated Thermal Strain (Pet) _z Down to			
			Solidification Range	δ/γ Transformation	1273 K (1000 °C)	γ -TCC (Average) 10^{-6} K^{-1}
HSLA	1790 (1517)	0.85	0.13	0.54	1.42	21 to 22
LCAK	1801 (1528)	0.71	0.18	0.65	1.49	20 to 21

720 LCAK steel by almost 5 K ($-268\text{ }^{\circ}\text{C}$), its contraction
 721 onset temperature $T_{\text{linear,onset}}$ is lower by more than
 722 10 K ($-263\text{ }^{\circ}\text{C}$) as compared to that of LCAK which
 723 corresponds to solid fractions of 0.85 and 0.72 for the
 724 HSLA and LCAK grades, respectively. In fact, LCAK
 725 steel experienced an earlier onset of thermal contraction
 726 within solidification range and, as a result, is exposed to
 727 a greater accumulated contraction, or strain, during
 728 solidification. Therefore, one can hypothesize that a
 729 higher level of strain in the LCAK steel upon solidifi-
 730 cation can cause larger level of thermal stresses and
 731 increase its susceptibility to hot cracking as compared to
 732 the HSLA steel.

733 On the other hand, structure development within the
 734 mushy zone, as described in Introduction, is also a
 735 determining factor for the rigidity point and affects the
 736 contraction behavior during solidification. The solidifi-
 737 cation microstructure of these steel grades was studied in
 738 References 27, 28. Both experimental measurements and
 739 phase field simulation show coarser columnar dendritic
 740 grains associated with the LCAK grade as compared to
 741 the HSLA steel during solidification. The coarser
 742 dendritic structure leads to an earlier interaction of
 743 dendrites and their bridging at lower solid fractions.
 744 This results in the enlargement of the VPSI in which the
 745 metal is experiencing stresses with limited ductility. Such
 746 trend agrees with the experimental results in this study.

747 In addition, hot tensile behavior of these two alloys
 748 was also investigated using *in situ* solidification^[29]
 749 whereby zero strength and zero ductility points of the
 750 alloys have been determined experimentally. The results
 751 show that brittle temperature range for LCAK is larger
 752 than that of HSLA while its fracture mode is more
 753 brittle as compared to HSLA fracture. Plant observa-
 754 tions of high-speed thin-slab casting of LCAK and
 755 HSLA steels along with statistical analyses of continu-
 756 ously cast slabs show that LCAK has yielded more
 757 defect records in terms of larger number of breakouts
 758 and cracks.^[29] So the results of tensile behavior and
 759 casting observations confirm the hypothesis of a greater
 760 hot cracking susceptibility of LCAK steel based on
 761 experimental results of the contraction study in this
 762 paper.

763 Similar to aluminum alloys,^[7,8] the analysis of con-
 764 traction behavior during solidification of steel can be
 765 utilized as a tool to predict the hot cracking suscepti-
 766 bility in CC. Our results show that the temperature of
 767 the linear contraction onset is close to the temperature
 768 at which, according to reference data, the hot cracking
 769 occurs. For example, Reference 30 reported that C-Cr
 770 steel possesses negligible ductility, hence is very suscep-
 771 tible to hot cracks, at a solid fraction of 0.8, nearly the
 772 same value as the rigidity point determined from our
 773 contraction experiments. Therefore, the rigidity concept,
 774 the linear contraction onset temperature, and the
 775 amount of the linear contraction are of both fundamen-
 776 tal and technical significance.

777 E. Thermal Contraction After Solidification

778 The contraction behavior of the solidified shell
 779 immediately after solidification affects not only stress

780 build-up within interior layers but also heat extraction
 781 process. Of special importance is δ/γ transformation
 782 during solidification and subsequent cooling. Such
 783 sequence of phase change is believed to be responsible
 784 for increasing level of defect formation and reducing
 785 heat flux during initial shell solidification and the
 786 reasons are especially attributed to volume contraction
 787 accompanying the δ/γ transformation.^[2] The magnitude
 788 of volume change upon the transformation was reported
 789 to be about 0.3 pct.^[31] In contrast to peritectic steels in
 790 which δ/γ transformation starts in the two-phase liquid-
 791 solid region and completes in the solid state,^[32] in low-
 792 carbon, low-alloy steel grades investigated in this paper,
 793 this transformation both starts and completes in the
 794 solid state and over a temperature range. So the impact
 795 of the transformation contraction on hot cracking is less
 796 pronounced here than in peritectic steels. However, the
 797 analysis of linear contraction of the just-solidified alloy
 798 during subsequent cooling can be used to explain
 799 geometrical changes of the shell below meniscus region
 800 in the CC mold.

801 The linear contraction is conventionally expressed in
 802 terms of linear thermal expansion or contraction coef-
 803 ficient—a well-known thermophysical property of the
 804 material. However, relevant reference data on the linear
 805 thermal expansion coefficients are seldom available for
 806 commercial alloys at high, sub-solidus temperatures.
 807 Moreover, those available values, usually determined by
 808 dilatometer, densitometer, lattice parameter measure-
 809 ments, *etc.*, as reviewed in Reference 14, are pertinent to
 810 nearly isothermal conditions using carefully homoge-
 811 nized samples. Efforts are even made to conduct the
 812 measurements close to equilibrium state of the alloy
 813 where removal of thermal gradients within the sample is
 814 attempted. Recalling that the real contraction condi-
 815 tions of a just-solidified bulk sample depart far from the
 816 equilibrium, knowledge of thermal expansion under
 817 conditions comparable to casting is required.

818 The developed technique can be utilized to analyze the
 819 contraction behavior of steel after solidification. The
 820 contraction of a sample at sub-solidus temperatures
 821 would be complex as different layers in the sample are
 822 undergoing different stages of solidification or cooling.
 823 The nonlinear section appearing in the sub-solidus part
 824 of the contraction curve may denote phase transforma-
 825 tion in thermocouple location. For example, upon
 826 cooling within 1733 K to 1703 K ($1460\text{ }^{\circ}\text{C}$ to $1430\text{ }^{\circ}\text{C}$)
 827 which is the range close to δ/γ transformation (see
 828 Table II), the given steel grades contract about 0.11 pct.
 829 Assuming isotropic contraction for the solid steel and
 830 multiplying this contraction (0.11 pct) by 3 to obtain
 831 volume change, one notes that the sample undergoes
 832 0.33 pct volume change over this temperature range
 833 which is close to 0.3 pct attributed to δ/γ transfor-
 834 mation.^[31] Hence, such nonlinear transitions in the con-
 835 traction curve can correspond to δ/γ transformation and
 836 denote a correlation between phase transformation and
 837 contraction behavior of the material. Although direct
 838 estimation of the TCC from the contraction curve is not
 839 straightforward within the transitory part, the magni-
 840 tude of accumulated contraction over the extended
 841 phase change interval (including both solidification and

842 solid δ/γ transformation) would be a measure of
 843 geometric changes of the solidifying shell just below
 844 meniscus. Accordingly, HSLA steel undergoes about
 845 0.54 pct linear contraction upon δ -ferrite solidification
 846 and transformation to γ -phase while LCAK experiences
 847 about 0.65 pct, *i.e.*, a larger linear contraction upon the
 848 extended phase change interval (see Table III).

849 The linear TCC of γ -phase, corresponding to the
 850 linear part of contraction curve, can be readily estimated
 851 by slope of the displacement curve according to TCC
 852 definition.^[33] Alternatively, the average TCC can be
 853 calculated by

$$\text{TCC} = [(L_{T2} - L_{T1})/L_{\text{gage}}]/(T_2 - T_1), \quad [2]$$

855 where T_2 and T_1 are the temperatures below the solidus;
 856 L_{T2} and L_{T1} are the positions read by the displacement
 857 sensor at T_2 and T_1 , respectively; and L_{gage} is the gage
 858 length of the sample. For HSLA steel, average value of 21
 859 to $22 \times 10^{-6} \text{ K}^{-1}$ was obtained for TCC in γ -phase. As
 860 also seen in Figure 8, the contraction trends of HSLA and
 861 LCAK steels in austenite phase are similar with slight
 862 difference in TCC values. In LCAK, the results show
 863 average values of 20 to $21 \times 10^{-6} \text{ K}^{-1}$ for TCC in γ -phase
 864 which is close to earlier measurements reported for ultra-
 865 low carbon (ULC) steel at the same temperature range.^[14]
 866 It follows that TCC of γ -phase of the tested low-carbon and
 867 low-alloy steels is a weak function of chemical composi-
 868 tion. Furthermore, as the strand surface temperature at the
 869 vicinity of mold exit is about 1273 K (1000 °C), the
 870 accumulated linear thermal contraction down to this
 871 temperature would be of technical significance. Our
 872 measurements show such values of 1.42 and 1.49 pct for
 873 HSLA and LCAK, respectively. Meng *et al.*^[20] simulated
 874 the shrinkage of a 0.044 pct C steel strand (continuously
 875 cast at 1.5 m/min) during solidification and cooling within
 876 the mold region where the strand surface temperature was
 877 about 1273 K (1000 °C) upon exiting the mold. The
 878 simulation predicts an accumulated linear contraction of
 879 1.4 pct which is very close to the measurements of this
 880 study. Therefore, this knowledge can be incorporated in
 881 computer simulation for mold design (*e.g.*, to accommo-
 882 date the geometric changes of the solidifying shell) and
 883 process optimization purposes.

884 IV. CONCLUSIONS

- 885 1. A technique was developed for experimental study-
 886 ing of the contraction behavior of steel during
 887 solidification.
 888 2. Using the developed technique, a better understanding
 889 of the contraction behavior of low-carbon low-alloy
 890 steels can be acquired during and after solidification
 891 under conditions comparable to those of CC practice.
 892 The method is capable of characterizing the contrac-
 893 tion of the material in terms of the temperature of the
 894 contraction onset, the amount of contraction in the
 895 solidification range, and the coefficient of thermal con-
 896 traction at sub-solidus temperatures.
 897 3. A correlation can be made among the structure for-
 898 mation, fraction of solid corresponding to the linear

contraction onset temperature, and the amount of
 the contraction accumulated in the solidification
 range. In spite of similar contraction trend due to the
 similar solidification path, LCAK and HSLA steels
 in this study exhibit rigidity at solid fraction of 0.72
 and 0.82 to 0.87, respectively. LCAK possesses a
 coarser dendritic structure and undergoes a larger
 linear contraction than HSLA during solidification.

4. Linear contraction behavior of steel during solidifi-
 cation could be a measure to reflect its hot cracking
 susceptibility. In this regard, lower solid fraction at
 rigidity point, larger VPSI and larger accumulated
 contraction during solidification could deteriorate
 the hot crack susceptibility of the alloy. The higher
 susceptibility of the studied LCAK grade, as
 observed to be more than that of the HSLA grade
 in mechanical testing and plant casting, can be
 explained through its contraction properties, *i.e.*,
 being rigid at a lower solid fraction and having a
 larger accumulated strain during solidification com-
 pared to the HSLA grade of steel.
 5. The contraction behavior of the studied steels at
 sub-solidus temperatures is a complex process but
 quite similar for the studied steels with close values
 of the TCC and in agreement with literature data.
 The technique can be used for determining the TCC
 and total contraction at high temperatures under
 casting conditions in the primary cooling zone of
 CC machine, with results being suitable for com-
 puter simulation, process design, and optimization.

ACKNOWLEDGMENTS

The work is done within the framework of the
 research program of Materials innovation institute
 (www.m2i.nl), under project M41.5.08321. The authors
 thank Dr. B. Santillana for providing useful materials
 and Mr. S. Sengo for sample preparation and optical
 microscopy.


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	MS Code :	<input type="checkbox"/> CP	<input type="checkbox"/> DISK